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# n-Cyclic Refined Neutrosophic Group Theory, An Application Of n-Cyclic Refined neutrosophic Sets

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**Abstract:** In This paper, use the term of n-cyclic refined neutrosophic sets to define n-cyclic refined neutrosophic groups. Also, we study some of their properties.

## Main Concepts

### Definition 3.1:

Let I be the neutrosophic element, which refers to indeterminacy, we define n-cyclic refining system of I by the set  $L=\{I_1, I_2, \dots, I_{n-1}\}$ , where  $I_i \neq I_j$  for all  $i \neq j$  and  $i, j < n$ .

We define a binary operation on L as follows:

. It is clear that L has a structure of the subset  $(Z_n/\{0\}, +)$ , where  $Z_n$  is the additive  $I_i I_j = I_{(i+j \bmod n)}$  group of integers modulo n.

Remark: For an easy representing, we can put  $I_i = I^i$ . i.e.  $I_1 = I^1, I_2 = I^2, \dots etc.$

### Definition 3.2:

Let  $(G, *)$  be a group, and I is the neutrosophic element with property  $I^n = I$  ;  $n \geq 2$  , with

$I^i \neq I^j$  for all  $i \neq j$  and  $i, j < n$  . We call  $M(G)=G \cup GI \cup GI^2 \cup \dots \cup GI^{n-1}$  an n-cyclic refined neutrosophic group.

It is easy to see that 2-cyclic refined neutrosophic group is the neutrosophic group.

### Remark 3.3:

The sets  $GI^k$  are groups under the binary operation  $(xI^k)(yI^k)=(xyI^k)$  ;  $k < n$  with identity  $I^k$  and each one of them must be isomorphic to G.

According to the previous operation, the inverse of  $xI^k$  is  $x^{-1}I^k$  .

### Definition 3.4:

Let  $M(G)$  be an n-cyclic refined neutrosophic group, H be a subset of  $M(G)$ . We call H an AH-subgroup if  $H=H_0 \cup H_1 I \cup H_2 I^2 \cup \dots \cup H_{n-1} I^{n-1}$ , where  $H_i$  is a subgroup of G for all i.

We call H an AHS-subgroup if  $H_0 = H_1 = \dots = H_{n-1}$ .

We call H an AH-normal if  $H_i$  is normal subgroup of G for all i.

We call H an AHS-normal if it is AHS-subgroup and AH-normal.

### Definition 3.5 :

Let  $M(G)$ ,  $M(H)$  be  $n$ ,  $m$ -cyclic refined neutrosophic groups respectively,  $f: M(G) \rightarrow M(H)$  be a map. We say that  $f$  is an AH-homomorphism if it is a homomorphism between  $G$ ,  $H$  i.e.  $f(xy) = f(x)f(y) \forall x, y \in G$  and  $f(I^k) = (I)^k$  such  $I$  is the neutrosophic element of  $H$ .

We define  $AH - Ker(f) = Ker f_G \cup Ker f_G I \cup \dots \cup Ker f_G I^{n-1}$ , we regard that  $AH - Ker(f)$  is an AHS-normal subgroup of  $M(G)$

We say that  $f$  is an isomorphism if it is a correspondence one-to-one homomorphism.

If  $H = H_0 \cup H_1 I \cup \dots \cup H_{n-1} I^{n-1}$  and  $K = K_0 \cup K_1 I \cup \dots \cup K_{n-1} I^{n-1}$  are two AH-subgroups of  $M(G)$ . We say that they are isomorphic if  $H_i \cong K_i$  for all  $i$ .

**Definition 3.6 :**

Let  $H$ ,  $K$  be two AH-subgroups of  $M(G)$ . We define

$$H_0 K_0 \cup H_1 K_1 I \cup \dots \cup H_{n-1} K_{n-1} I^{n-1}. HK =$$

**Definition 3.7 :**

Let  $M(G)$  be an  $n$ -cyclic refined neutrosophic group,  $H = H_0 \cup H_1 I \cup H_2 I^2 \cup \dots \cup H_{n-1} I^{n-1}$  be an AH-normal subgroup of  $M(G)$ . We define the corresponding AH-factor as  $M(G)/H = (G/H_0) \cup (G/H_1)I \cup \dots \cup (G/H_{n-1})I^{n-1}$ .

**Definition 3.8 :**

Let  $M(G)$  be an  $n$ -cyclic refined neutrosophic group. We define the AH-center of  $M(G)$  by

$$Z(G) \cup Z(G)I \cup \dots \cup Z(G)I^{n-1}. Z(M(G)) =$$

It is easy to see that  $Z(M(G))$  is an AHS-normal subgroup of  $M(G)$ .

**Definition 3.9 :**

Let  $M(G)$  be an  $n$ -cyclic refined neutrosophic group. We say that  $M(G)$  is abelian if  $G$  is abelian, i.e.  $M(G) = Z(M(G))$ .

$M(G)$  is said to be cyclic if  $G$  is cyclic.

**Theorem 3.10 :**

Let  $M(G)$  be an  $n$ -cyclic refined neutrosophic group. Then

- (a) If  $H$  is an AH-normal subgroup and  $M(G)$  is abelian. Then  $M(G)/H$  is abelian.
- (b) If  $M(G)$  is finite and  $H$  is an AHS-subgroup, then  $O(H)$  divides  $O(M(G)) = n O(G)$ .
- (c) If  $H$  is an AH-normal subgroup and  $M(G)$  is cyclic then  $M(G)/H$  is cyclic.

Proof:

(a) Since  $M(G)/H = (G/H_0) \cup (G/H_1)I \cup \dots \cup (G/H_{n-1})I^{n-1}$  and  $G/H_i$  is abelian for all  $i$ . Then  $M(G)/H$  is abelian.

(b) We have that  $O(H) = n O(H_0)$  and  $O(H_0)$  divides the order of  $G$  then  $O(H)$  divides  $O(M(G)) = n O(G)$ .

(c) Since  $G/H_i$  is cyclic for all  $i$ . Then  $M(G)/H$  is cyclic.

**Theorem 3.11 :**

Let  $M(G)$  be an  $n$ -cyclic refined neutrosophic group and  $H, K$  be two AH-subgroups. Then

(a)  $H \cap K$  is an AH-subgroup.

If  $H, K$  are AHS-subgroups, then  $H \cap K$  is an AHS-subgroup. (b)

(c) If  $H, K$  are AH-normal subgroups, then  $H \cap K$  and  $HK$  are AH-normal subgroups.

(d) If  $H, K$  are AHS-normal subgroups, then  $H \cap K$  and  $HK$  are AHS-normal subgroups.

Proof : Suppose that  $H = H_0 \cup H_1 I \cup \dots \cup H_{n-1} I^{n-1}$  and  $K = K_0 \cup K_1 I \cup \dots \cup K_{n-1} I^{n-1}$  then  $H \cap K = (H_0 \cap K_0) \cup (H_1 \cap K_1) I \cup \dots \cup (H_{n-1} \cap K_{n-1}) I^{n-1}$  by this argument we can easily find that the proof holds.

**Theorem 3.12 :**

Let  $M(G), M(H)$  be  $n, m$ -cyclic refined neutrosophic groups respectively, and  $f: M(G) \rightarrow M(H)$  be a homomorphism. Then

a)  $n \geq m$ .

(b) If  $K$  is an AH-subgroup of  $M(G)$  then  $f(K)$  is an AH-subgroup of  $M(H)$ .

(c) If  $K$  is an AHS-subgroup of  $M(G)$  then  $f(K)$  is an AHS-subgroup of  $M(H)$ .

(d) If  $K$  is an AH-normal subgroup of  $M(G)$  then  $f(K)$  is an AH-normal subgroup of  $f(M(G))$ .

(e) If  $K$  is an AHS-normal subgroup of  $M(G)$  then  $f(K)$  is an AHS-normal subgroup of  $f(M(G))$ .

(f)  $M(G)/\text{Ker} f \cong f(M(G))$ .

Proof :

(a) Suppose that  $n < m$  then  $I = f(I) = f(I^n) = (I)^n$  and this is a contradiction according to the definition 3.5, thus  $n \geq m$ .

(b) Suppose that  $K = K_0 \cup K_1 I \cup \dots \cup K_{n-1} I^{n-1}$ , then  $f(K) = f(K_0) \cup f(K_1) I \cup \dots \cup f(K_{n-1}) I^{n-1}$  with subgroups  $f(K_i)$  for all  $i$  of  $M(H)$ , so that  $f(K)$  is an AH-subgroup of  $M(H)$ .

(c) It is obvious that if  $K_i = K_j$ , then  $f(K_i) \cong f(K_j)$ , thus  $f(K)$  is an AHS-subgroup of  $M(H)$ .

(d), (e) hold directly from (b) and (c) and from the fact that if  $K_i$  is normal, then  $f(K_i)$  is normal.

(f) From the definition, we find  $M(G)/\text{Ker} f = (G/\text{Ker} f_G) \cup (G/\text{Ker} f_G) I \cup \dots \cup (G/\text{Ker} f_G) I^{n-1}$ ; but  $G/\text{Ker} f_G \cong f(G)$ , thus  $M(G)/\text{Ker} f \cong f(G) \cup f(G) I \cup \dots \cup f(G) I^{n-1} = f(M(G))$ .

**Theorem 3.13 :**

Let  $M(G)$  be an  $n$ -cyclic refined neutrosophic group and  $H, K$  be two AH-normal subgroups with  $K \leq H$ , then  $(M(G)/K)/(H/K) \cong M(G)/H$ .

Proof :

Suppose that  $H = H_0 \cup H_1 I \cup \dots \cup H_{n-1} I^{n-1}$  and  $K = K_0 \cup K_1 I \cup \dots \cup K_{n-1} I^{n-1}$  with  $K \leq H$ , then

$$(M(G)/K)/(H/K) = ((G/K_0) \cup \dots \cup (G/K_{n-1}) I^{n-1}) / ((H_0/K_0) \cup \dots \cup (H_{n-1}/K_{n-1}) I^{n-1}) \cong G/K_0 / (H_0/K_0) \cup \dots \cup (G/K_{n-1}) / (H_{n-1}/K_{n-1}) I^{n-1} \cong G/H_0 \cup (G/H_1) I \cup \dots \cup (G/H_{n-1}) I^{n-1} = M(G)/H.$$

**Theorem 3.14 :**

Let  $M(G)$  be an  $n$ -cyclic refined neutrosophic group, and  $H$  is an AH-normal subgroup, then for each AH-subgroup  $T$  of  $M(G)/H$  there is an AH-subgroup of  $M(G)$  contains  $H$ .

Proof : It can be proved as the classical case.

**Definition 3.15 :**

Let  $M(G)$ ,  $M(H)$  be two  $n$ -cyclic refined neutrosophic groups,

we define  $M(G) \times M(H) = (G \times H) \cup (G \times H) I I' \cup \dots \cup (G \times H) I^n (I')^n$  with  $(I I')^k = I^k (I')^k$  for all  $k$ , it is clear that  $M(G) \times M(H)$  is an  $n$ -generalized neutrosophic group with neutrosophic element  $I I'$ .

**Theorem 3.16 :**

Let  $M(G)$ ,  $M(H)$  be two  $n$ -cyclic refined neutrosophic groups. Then

- (a) If  $M(G)$ ,  $M(H)$  are abelian then  $M(G) \times M(H)$  is abelian.
- (b) If  $T, S$  are two AH-subgroups of  $M(G)$ ,  $M(H)$  respectively, then  $T \times S$  is an AH-subgroup of  $M(G) \times M(H)$ .
- (c) If  $T, S$  are two AH-normal subgroups of  $M(G)$ ,  $M(H)$  respectively, then  $T \times S$  is an AH-normal subgroup of  $M(G) \times M(H)$ .
- (d) If  $T, S$  are two AHS-subgroups of  $M(G)$ ,  $M(H)$  respectively, then  $T \times S$  is an AHS-subgroup of  $M(G) \times M(H)$ .
- (e) If  $T, S$  are two AHS-normal subgroups of  $M(G)$ ,  $M(H)$  respectively then  $T \times S$  is an AHS-normal subgroup of  $M(G) \times M(H)$ .

Proof :

- (a) It is clear since  $G \times H$  is abelian.
  - (b) Assume that  $T = T_0 \cup \dots \cup T_{n-1} I^{n-1}$  and  $S = S_0 \cup \dots \cup S_{n-1} (I')^{n-1}$ , then
- $$T \times S = (T_0 \times S_0) \cup \dots \cup (T_{n-1} \times S_{n-1}) (I I')^{n-1},$$
- we can regard that  $T_i \times S_i$  is a subgroup of  $G \times H$ , so  $T \times S$  is an AH-subgroup.
- (c) It holds directly from (b).
  - (d) If  $S_j \cong T_i$  and  $S_j \cong S_i$  then  $T_i \times S_i \cong T_j \times S_j$  and then  $T \times S$  is an AHS-subgroup.
  - (e) It holds directly from (d) and (c).

**Example 3.17:**

Consider the additive group  $(R^*, +)$  and the integer  $n = 3$ . The corresponding 3-cyclic refined neutrosophic group is

$$.M(R) = \{a, bI, cI^2; a, b, c \in R^*\}$$

1) We know that  $(Q^*, .)$  is a subgroup of  $(R^*, .)$ , hence  $L=Q^* \cup Q^*I \cup Q^*I^2 = \{x, yI, zI^2; x, y, z \in Q^*\}$  is a 3-cyclic refined AHS-subgroup.

2) The corresponding AH-factor is  $M(R)/_L = R^*/_{Q^*} \cup R^*/_{Q^*}I \cup R^*/_{Q^*}I^2$ .

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