Recognition of the Pattern for Vertices to Make Dimension by Resolving in some Classes of Neutrosophic Graphs

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Abstract

New setting is introduced to study k-number-resolving number and neutrosophic k-number-resolving number arising from k-number-resolved vertices in neutrosophic graphs assigned to neutrosophic graphs. Minimum number of k-number-resolved vertices, is a number which is representative based on those vertices. Minimum neutrosophic number of k-number-resolved vertices corresponded to k-number-resolving set is called neutrosophic k-number-resolving number. Forming sets from k-number-resolved vertices to figure out different types of number of vertices in the sets from k-number-resolved sets in the terms of minimum number of vertices to get minimum number to assign to neutrosophic graphs is key type of approach to have these notions namely k-number-resolving number and neutrosophic k-number-resolving number arising from k-number-resolved vertices in neutrosophic graphs assigned to neutrosophic graphs. Two numbers and one set are assigned to a neutrosophic graph, are obtained but now both settings lead to approach is on demand which is to compute and to find representatives of sets having smallest number of k-number-resolved vertices from different types of sets in the terms of minimum number and minimum neutrosophic number forming it to get minimum number to assign to a neutrosophic graph. Let $NTG : (V, E, \sigma, \mu)$ be a neutrosophic graph. Then for given vertices n and n' if $d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n')$, then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum cardinality between all k-number-resolving sets is called k-number-resolving number and it's denoted by $\mathcal{N}^k(NTG)$; for given vertices n and n' if $d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n')$, then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called neutrosophic k-number-resolving set. The minimum neutrosophic cardinality between all k-number-resolving sets is called neutrosophic k-number-resolving number and it's denoted by $\mathcal{N}_n^k(NTG)$. As concluding results, there are some statements, remarks, examples and clarifications about some classes of neutrosophic graphs namely path-neutrosophic graphs, cycle-neutrosophic graphs, complete-neutrosophic graphs, star-neutrosophic graphs, complete-bipartite-neutrosophic graphs, complete-t-partite-neutrosophic graphs, and wheel-neutrosophic graphs. The clarifications are also presented in both sections "Setting of k-number-resolving number," and "Setting of neutrosophic k-number-resolving number," for introduced results and used classes. This approach facilitates identifying sets which form k-number-resolving number and neutrosophic k-number-resolving number arising from k-number-resolved vertices in neutrosophic graphs assigned to neutrosophic graphs. In both settings, some classes of well-known neutrosophic graphs are studied. Some clarifications for each result and each definition are provided. The cardinality of set of k-number-resolved vertices and neutrosophic cardinality of set of k-number-resolved vertices corresponded to k-number-resolving set have eligibility to define k-number-resolving number and neutrosophic k-number-resolving number but different types of set of k-number-resolved vertices to define k-number-resolving sets. Some results get more frameworks and more perspectives about these definitions. The way in that, different types of set of k-number-resolved vertices in the terms of minimum number to assign to neutrosophic graphs, opens the way to do some approaches. These notions are applied into neutrosophic graphs as individuals but not family of them as drawbacks for these notions. Finding special neutrosophic graphs which are well-known, is an open way to pursue this study. Neutrosophic k-number-resolving notion is applied to different settings and classes of neutrosophic graphs. Some problems are proposed to pursue this study. Basic familiarities with graph theory and neutrosophic graph theory are proposed for this article.

Keywords: k-number-resolving Number, Neutrosophic k-number-resolving Number, Classes of Neutrosophic Graphs

AMS Subject Classification: 05C17, 05C22, 05E45

1 Background

Fuzzy set in **Ref.** [22] by Zadeh (1965), intuitionistic fuzzy sets in **Ref.** [3] by Atanassov (1986), a first step to a theory of the intuitionistic fuzzy graphs in **Ref.** [18] by Shannon and Atanassov (1994), a unifying field in logics neutrosophy: neutrosophic probability, set and logic, rehoboth in **Ref.** [19] by Smarandache (1998), single-valued neutrosophic sets in **Ref.** [20] by Wang et al. (2010), single-valued neutrosophic graphs in **Ref.** [6] by Broumi et al. (2016), operations on single-valued neutrosophic graphs in **Ref.** [1] by Akram and Shahzadi (2017), neutrosophic soft graphs in **Ref.** [17] by Shah and Hussain (2016), bounds on the average and minimum attendance in preference-based activity scheduling in **Ref.** [2] by Aronshtam and Ilani (2022), investigating the recoverable robust single machine scheduling problem under interval uncertainty in **Ref.** [5] by Bold and Goerigk (2022), error-correcting codes from k-resolving sets in **Ref.** [4] by R.F. Bold, and I.G. Yero (2016), restrained 2-resolving dominating sets in the join, corona and lexicographic product of two graphs in **Ref.** [7] by .M. Cabaro, and H. Rara (2022), restrained 2-resolving sets in the join, corona and lexicographic product of two graphs in **Ref.** [8] by J.M. Cabaro, and H. Rara (2022), on 2-resolving dominating sets in the join, corona and lexicographic product of two graphs in **Ref.** [9] by J.M. Cabaro, and H. Rara (2022), on 2-resolving sets in the join and corona of graphs in **Ref.** [10] by J.M. Cabaro, and H. Rara (2021), 2-metric dimension of cartesian product of graphs in **Ref.** [11] by K.N. Geetha, and B. Sooryanarayana (2017), on 2-metric resolvability in rotationally-symmetric graphs in **Ref.** [16] by B. Humera et al. (2021), the distance 2-resolving domination number of graphs in **Ref.** [21] by D.A.R. Wardani et al. (2021), three types of neutrosophic alliances based on connectedness and (strong) edges in **Ref.** [15] by Henry Garrett (2022), properties of SuperHyperGraph and neutrosophic SuperHyperGraph in **Ref.** [14] by Henry Garrett (2022), are studied. Also, some studies and researches about neutrosophic graphs, are proposed as books in **Ref.** [12] by Henry Garrett (2022) which is indexed by Google Scholar and has more than 300 readers in Scribd; in **Ref.** [13] by Henry Garrett (2022) which is indexed by Google Scholar and has more than 1000 readers in Scribd.

In this section, I use two subsections to illustrate a perspective about the background of this study.

1.1 Motivation and Contributions

In this study, there's an idea which could be considered as a motivation.

Question 1.1. *Is it possible to use mixed versions of ideas concerning "k-number-resolving number", "neutrosophic k-number-resolving number" and "Neutrosophic Graph" to define some notions which are applied to neutrosophic graphs?*

It's motivation to find notions to use in any classes of neutrosophic graphs. Real-world applications about time table and scheduling are another thoughts which lead to be considered as motivation. Having connection amid two vertices have key roles to assign k-number-resolving number and neutrosophic k-number-resolving number arising from k-number-resolved vertices in neutrosophic graphs assigned to neutrosophic graphs. Thus they're used to define new ideas which conclude to the structure of k-number-resolving number and neutrosophic k-number-resolving number arising from k-number-resolved vertices in neutrosophic graphs assigned to neutrosophic graphs. The concept of having smallest number of k-number-resolved vertices in the terms of crisp setting and in the terms of neutrosophic setting inspires us to study the behavior of all k-number-resolved vertices in the way that, some types of numbers, k-number-resolving number and neutrosophic k-number-resolving number arising from k-number-resolved vertices in neutrosophic graphs assigned to neutrosophic graphs, are the cases of study in the setting of individuals. In both settings, corresponded numbers conclude the discussion. Also, there are some avenues to extend these notions.

The framework of this study is as follows. In the beginning, I introduce basic definitions to clarify about preliminaries. In subsection "Preliminaries", new notions of k-number-resolving number and neutrosophic k-number-resolving number arising from k-number-resolved vertices in neutrosophic graphs assigned to neutrosophic graphs, are highlighted, are introduced and are clarified as individuals. In section "Preliminaries", minimum number of k-number-resolved vertices, is a number which is representative based on those vertices, have the key role in this way. General results are obtained and also, the results about the basic notions of k-number-resolving number and neutrosophic k-number-resolving number arising from k-number-resolved vertices in neutrosophic graphs assigned to neutrosophic graphs, are elicited. Some classes of neutrosophic graphs are studied in the terms of k-number-resolving number and neutrosophic k-number-resolving number arising from k-number-resolved vertices in neutrosophic graphs assigned to neutrosophic graphs, in section "Setting of k-number-resolving number," as individuals. In section "Setting of k-number-resolving number," k-number-resolving number is applied into individuals. As concluding results, there are some statements, remarks, examples and clarifications about some classes of neutrosophic graphs namely path-neutrosophic graphs, cycle-neutrosophic graphs, complete-neutrosophic graphs, star-neutrosophic graphs, complete-bipartite-neutrosophic graphs, complete-t-partite-neutrosophic graphs, and wheel-neutrosophic graphs. The clarifications are also presented in both sections "Setting of k-number-resolving number," and "Setting of neutrosophic k-number-resolving number," for introduced results and used classes. In section

"Applications in Time Table and Scheduling", two applications are posed for quasi-complete and complete notions, namely complete-neutrosophic graphs and complete-t-partite-neutrosophic graphs concerning time table and scheduling when the suspicions are about choosing some subjects and the mentioned models are considered as individual. In section "Open Problems", some problems and questions for further studies are proposed. In section "Conclusion and Closing Remarks", gentle discussion about results and applications is featured. In section "Conclusion and Closing Remarks", a brief overview concerning advantages and limitations of this study alongside conclusions is formed.

1.2 Preliminaries

In this subsection, basic material which is used in this article, is presented. Also, new ideas and their clarifications are elicited.

Basic idea is about the model which is used. First definition introduces basic model.

Definition 1.2. (Graph).
$G = (V, E)$ is called a **graph** if V is a set of objects and E is a subset of $V \times V$ (E is a set of 2-subsets of V) where V is called **vertex set** and E is called **edge set**. Every two vertices have been corresponded to at most one edge.

Neutrosophic graph is the foundation of results in this paper which is defined as follows. Also, some related notions are demonstrated.

Definition 1.3. (Neutrosophic Graph And Its Special Case).
$NTG = (V, E, \sigma = (\sigma_1, \sigma_2, \sigma_3), \mu = (\mu_1, \mu_2, \mu_3))$ is called a **neutrosophic graph** if it's graph, $\sigma_i : V \to [0, 1]$, and $\mu_i : E \to [0, 1]$. We add one condition on it and we use **special case** of neutrosophic graph but with same name. The added condition is as follows, for every $v_iv_j \in E$,

$$\mu(v_iv_j) \leq \sigma(v_i) \wedge \sigma(v_j).$$

(i) : σ is called **neutrosophic vertex set**.

(ii) : μ is called **neutrosophic edge set**.

(iii) : $|V|$ is called **order** of NTG and it's denoted by $\mathcal{O}(NTG)$.

(iv) : $\sum_{v \in V} \sum_{i=1}^{3} \sigma_i(v)$ is called **neutrosophic order** of NTG and it's denoted by $\mathcal{O}_n(NTG)$.

(v) : $|E|$ is called **size** of NTG and it's denoted by $\mathcal{S}(NTG)$.

(vi) : $\sum_{e \in E} \sum_{i=1}^{3} \mu_i(e)$ is called **neutrosophic size** of NTG and it's denoted by $\mathcal{S}_n(NTG)$.

Some classes of well-known neutrosophic graphs are defined. These classes of neutrosophic graphs are used to form this study and the most results are about them.

Definition 1.4. Let $NTG : (V, E, \sigma, \mu)$ be a neutrosophic graph. Then

(i) : a sequence of consecutive vertices $P : x_0, x_1, \cdots, x_{\mathcal{O}(NTG)}$ is called **path** where $x_ix_{i+1} \in E,\ i = 0, 1, \cdots, \mathcal{O}(NTG) - 1$;

(ii) : **strength** of path $P : x_0, x_1, \cdots, x_{\mathcal{O}(NTG)}$ is $\bigwedge_{i=0,\cdots,\mathcal{O}(NTG)-1} \mu(x_ix_{i+1})$;

(iii) : **connectedness** amid vertices x_0 and x_t is

$$\mu^{\infty}(x_0, x_t) = \bigvee_{P:x_0,x_1,\cdots,x_t} \bigwedge_{i=0,\cdots,t-1} \mu(x_ix_{i+1});$$

$(iv):$ a sequence of consecutive vertices $P: x_0, x_1, \cdots, x_{\mathcal{O}(NTG)}, x_0$ is called **cycle** where $x_i x_{i+1} \in E,\ i = 0, 1, \cdots, \mathcal{O}(NTG) - 1,\ x_{\mathcal{O}(NTG)} x_0 \in E$ and there are two edges xy and uv such that $\mu(xy) = \mu(uv) = \bigwedge_{i=0,1,\cdots,n-1} \mu(v_i v_{i+1})$;

$(v):$ it's **t-partite** where V is partitioned to t parts, $V_1^{s_1}, V_2^{s_2}, \cdots, V_t^{s_t}$ and the edge xy implies $x \in V_i^{s_i}$ and $y \in V_j^{s_j}$ where $i \neq j$. If it's complete, then it's denoted by $K_{\sigma_1, \sigma_2, \cdots, \sigma_t}$ where σ_i is σ on $V_i^{s_i}$ instead V which mean $x \notin V_i$ induces $\sigma_i(x) = 0$. Also, $|V_j^{s_i}| = s_i$;

$(vi):$ t-partite is **complete bipartite** if $t = 2$, and it's denoted by K_{σ_1, σ_2};

$(vii):$ complete bipartite is **star** if $|V_1| = 1$, and it's denoted by S_{1, σ_2};

$(viii):$ a vertex in V is **center** if the vertex joins to all vertices of a cycle. Then it's **wheel** and it's denoted by W_{1, σ_2};

$(ix):$ it's **complete** where $\forall uv \in V,\ \mu(uv) = \sigma(u) \wedge \sigma(v)$;

$(x):$ it's **strong** where $\forall uv \in E,\ \mu(uv) = \sigma(u) \wedge \sigma(v)$.

To make them concrete, I bring preliminaries of this article in two upcoming definitions in other ways.

Definition 1.5. (Neutrosophic Graph And Its Special Case).

$NTG = (V, E, \sigma = (\sigma_1, \sigma_2, \sigma_3), \mu = (\mu_1, \mu_2, \mu_3))$ is called a **neutrosophic graph** if it's graph, $\sigma_i : V \to [0, 1]$, and $\mu_i : E \to [0, 1]$. We add one condition on it and we use **special case** of neutrosophic graph but with same name. The added condition is as follows, for every $v_i v_j \in E$,

$$\mu(v_i v_j) \leq \sigma(v_i) \wedge \sigma(v_j).$$

$|V|$ is called **order** of NTG and it's denoted by $\mathcal{O}(NTG)$. $\Sigma_{v \in V} \sigma(v)$ is called **neutrosophic order** of NTG and it's denoted by $\mathcal{O}_n(NTG)$.

Definition 1.6. Let $NTG : (V, E, \sigma, \mu)$ be a neutrosophic graph. Then it's **complete** and denoted by CMT_σ if $\forall x, y \in V, xy \in E$ and $\mu(xy) = \sigma(x) \wedge \sigma(y)$; a sequence of consecutive vertices $P : x_0, x_1, \cdots, x_{\mathcal{O}(NTG)}$ is called **path** and it's denoted by PTH where $x_i x_{i+1} \in E,\ i = 0, 1, \cdots, n-1$; a sequence of consecutive vertices $P : x_0, x_1, \cdots, x_{\mathcal{O}(NTG)}, x_0$ is called **cycle** and denoted by CYC where $x_i x_{i+1} \in E,\ i = 0, 1, \cdots, n-1,\ x_{\mathcal{O}(NTG)} x_0 \in E$ and there are two edges xy and uv such that $\mu(xy) = \mu(uv) = \bigwedge_{i=0,1,\cdots,n-1} \mu(v_i v_{i+1})$; it's **t-partite** where V is partitioned to t parts, $V_1^{s_1}, V_2^{s_2}, \cdots, V_t^{s_t}$ and the edge xy implies $x \in V_i^{s_i}$ and $y \in V_j^{s_j}$ where $i \neq j$. If it's **complete**, then it's denoted by $CMT_{\sigma_1, \sigma_2, \cdots, \sigma_t}$ where σ_i is σ on $V_i^{s_i}$ instead V which mean $x \notin V_i$ induces $\sigma_i(x) = 0$. Also, $|V_j^{s_i}| = s_i$; t-partite is **complete bipartite** if $t = 2$, and it's denoted by CMT_{σ_1, σ_2}; complete bipartite is **star** if $|V_1| = 1$, and it's denoted by STR_{1, σ_2}; a vertex in V is **center** if the vertex joins to all vertices of a cycle. Then it's **wheel** and it's denoted by WHL_{1, σ_2}.

Remark 1.7. Using notations which is mixed with literatures, are reviewed.

1. $NTG = (V, E, \sigma = (\sigma_1, \sigma_2, \sigma_3), \mu = (\mu_1, \mu_2, \mu_3)),\ \mathcal{O}(NTG)$, and $\mathcal{O}_n(NTG)$;

2. $CMT_\sigma, PTH, CYC, STR_{1, \sigma_2}, CMT_{\sigma_1, \sigma_2}, CMT_{\sigma_1, \sigma_2, \cdots, \sigma_t}$, and WHL_{1, σ_2}.

Definition 1.8. (k-number-resolving numbers).

Let $NTG : (V, E, \sigma, \mu)$ be a neutrosophic graph. Then (*i*) for given vertices n and n' if

$$d(s_1,n) \neq d(s_1,n'), d(s_2,n) \neq d(s_2,n'), \ldots, d(s_k,n) \neq d(s_k,n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called **k-number-resolving set**. The minimum cardinality between all k-number-resolving sets is called **k-number-resolving number** and it's denoted by $\mathcal{N}^k(NTG)$;

(*ii*) for given vertices n and n' if

$$d(s_1,n) \neq d(s_1,n'), d(s_2,n) \neq d(s_2,n'), \ldots, d(s_k,n) \neq d(s_k,n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called **neutrosophic k-number-resolving set**. The minimum neutrosophic cardinality between all k-number-resolving sets is called **neutrosophic k-number-resolving number** and it's denoted by $\mathcal{N}_n^k(NTG)$.

For convenient usages, the word neutrosophic which is used in previous definition, won't be used, usually.

Proposition 1.9. *Let $NTG : (V, E, \sigma, \mu)$ be a neutrosophic graph. Then k-number-resolving number is greater than k.*

Proof. Let $NTG : (V, E, \sigma, \mu)$ be a neutrosophic graph. Then for given vertices n and n' if

$$d(s_1,n) \neq d(s_1,n'), d(s_2,n) \neq d(s_2,n'), \ldots, d(s_k,n) \neq d(s_k,n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum cardinality between all k-number-resolving sets is called k-number-resolving number and it's denoted by $\mathcal{N}^k(NTG)$; thus $\mathcal{N}^k(NTG) \geq k$. □

Proposition 1.10. *Let $NTG : (V, E, \sigma, \mu)$ be a neutrosophic graph. If $|S| = k$, then k-number-resolving number is k.*

Proof. Let $NTG : (V, E, \sigma, \mu)$ be a neutrosophic graph. Then for given vertices n and n' if

$$d(s_1,n) \neq d(s_1,n'), d(s_2,n) \neq d(s_2,n'), \ldots, d(s_k,n) \neq d(s_k,n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum cardinality between all k-number-resolving sets is called k-number-resolving number and it's denoted by $\mathcal{N}^k(NTG)$; thus $\mathcal{N}^k(NTG) \geq k$ and by Proposition (1.9). By $|S| = k$ and $\mathcal{N}^k(NTG) \geq k$, $\mathcal{N}^k(NTG) = k$. □

In next part, clarifications about main definition are given. To avoid confusion and for convenient usages, examples are usually used after every part and names are used in the way that, abbreviation, simplicity, and summarization are the matters of mind.

Example 1.11. In Figure (1), a complete-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows.

(i) For given neutrosophic vertex, s, there's an edge with other vertices;

(ii) in the setting of complete, a vertex of resolving set corresponded to resolving number resolves as if it doesn't k-number-resolve so as resolving is different from k-number-resolving. Resolving number and k-number-resolving number are the same if $k = 1$;

(iii) all minimal k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_1, n_2, n_3\}^3, \{n_1, n_2, n_4\}^3, \{n_1, n_3, n_4\}^3.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum cardinality between all k-number-resolving sets is called k-number-resolving number and it's denoted by $\mathcal{N}^k(NTG) = k,\ k = \mathcal{O}(NTG) - 1$; and corresponded to k-number-resolving sets are

$$\{n_1, n_2, n_3\}^3, \{n_1, n_2, n_4\}^3, \{n_1, n_3, n_4\}^3;$$

(iv) there are four k-number-resolving sets

$$\{n_1, n_2, n_3\}^3, \{n_1, n_2, n_4\}^3, \{n_1, n_3, n_4\}^3,$$
$$\{n_1, n_2, n_3, n_4\}^4,$$

so as it's possible to have one of them as a set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is characteristic;

(v) there are three k-number-resolving sets

$$\{n_1, n_2, n_3\}^3, \{n_1, n_2, n_4\}^3, \{n_1, n_3, n_4\}^3,$$

corresponded to k-number-resolving number as if there's one k-number-resolving set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is the determiner;

(vi) all k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_1, n_2, n_3\}^3, \{n_1, n_2, n_4\}^3, \{n_1, n_3, n_4\}^3.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

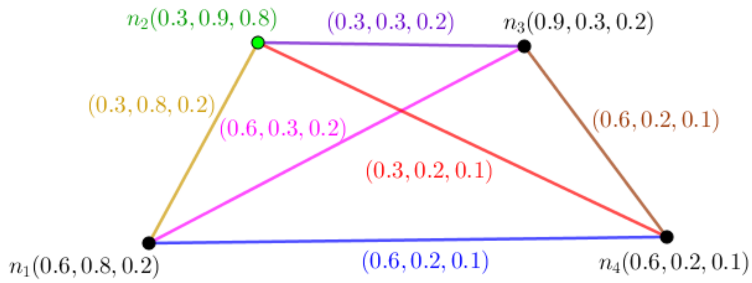

Figure 1. A Neutrosophic Graph in the Viewpoint of its k-number-resolving number and its neutrosophic k-number-resolving number.

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum neutrosophic cardinality between all k-number-resolving sets is called neutrosophic k-number-resolving number and it's denoted by
$\mathcal{N}_n^k(NTG) = 3.9,\ k = \mathcal{O}(NTG) - 1$; and corresponded to k-number-resolving sets are

$$\{n_1, n_3, n_4\}^3.$$

2 Setting of k-number-resolving number

In this section, I provide some results in the setting of k-number-resolving number. Some classes of neutrosophic graphs are chosen. Complete-neutrosophic graph, path-neutrosophic graph, cycle-neutrosophic graph, star-neutrosophic graph, bipartite-neutrosophic graph, t-partite-neutrosophic graph, and wheel-neutrosophic graph, are both of cases of study and classes which the results are about them.

Proposition 2.1. *Let $NTG : (V, E, \sigma, \mu)$ be a complete-neutrosophic graph. Then*

$$\mathcal{N}^k(CMT_\sigma) = k,\ k = \mathcal{O}(CMT_\sigma) - 1.$$

Thus,

$$\mathcal{N}^{\mathcal{O}(CMT_\sigma)-1}(CMT_\sigma) = \mathcal{O}(CMT_\sigma) - 1.$$

Proof. Suppose $CMT_\sigma : (V, E, \sigma, \mu)$ is a complete-neutrosophic graph. By $CMT_\sigma : (V, E, \sigma, \mu)$ is a complete-neutrosophic graph, all vertices are connected to each other. So there's one edge between two vertices. In the setting of complete, a vertex of resolving set corresponded to resolving number resolves as if it doesn't k-number-resolve so as resolving is different from k-number-resolving. Resolving number and k-number-resolving number are the same if $k = 1$. All minimal k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_2, n_3, n_4, \ldots, n_{\mathcal{O}(CMT_\sigma)-2}, n_{\mathcal{O}(CMT_\sigma)-1}, n_{\mathcal{O}(CMT_\sigma)}\},$$
$$\{n_1, n_3, n_4, \ldots, n_{\mathcal{O}(CMT_\sigma)-2}, n_{\mathcal{O}(CMT_\sigma)-1}, n_{\mathcal{O}(CMT_\sigma)}\},$$
$$\{n_1, n_2, n_4, \ldots, n_{\mathcal{O}(CMT_\sigma)-2}, n_{\mathcal{O}(CMT_\sigma)-1}, n_{\mathcal{O}(CMT_\sigma)}\},$$
$$\ldots$$
$$\{n_1, n_2, n_3, \ldots, n_{\mathcal{O}(CMT_\sigma)-3}, n_{\mathcal{O}(CMT_\sigma)-1}, n_{\mathcal{O}(CMT_\sigma)}\},$$
$$\{n_1, n_2, n_3, \ldots, n_{\mathcal{O}(CMT_\sigma)-3}, n_{\mathcal{O}(CMT_\sigma)-2}, n_{\mathcal{O}(CMT_\sigma)}\},$$
$$\{n_1, n_2, n_3, \ldots, n_{\mathcal{O}(CMT_\sigma)-3}, n_{\mathcal{O}(CMT_\sigma)-2}, n_{\mathcal{O}(CMT_\sigma)-1}\}.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum cardinality between all k-number-resolving sets is called k-number-resolving number and it's denoted by

$$\mathcal{N}^k(CMT_\sigma) = k, \; k = \mathcal{O}(CMT_\sigma) - 1.$$

Thus,

$$\mathcal{N}^{\mathcal{O}(CMT_\sigma)-1}(CMT_\sigma) = \mathcal{O}(CMT_\sigma) - 1;$$

and corresponded to k-number-resolving sets are

$$\{n_2, n_3, n_4, \ldots, n_{\mathcal{O}(CMT_\sigma)-2}, n_{\mathcal{O}(CMT_\sigma)-1}, n_{\mathcal{O}(CMT_\sigma)}\},$$
$$\{n_1, n_3, n_4, \ldots, n_{\mathcal{O}(CMT_\sigma)-2}, n_{\mathcal{O}(CMT_\sigma)-1}, n_{\mathcal{O}(CMT_\sigma)}\},$$
$$\{n_1, n_2, n_4, \ldots, n_{\mathcal{O}(CMT_\sigma)-2}, n_{\mathcal{O}(CMT_\sigma)-1}, n_{\mathcal{O}(CMT_\sigma)}\},$$
$$\ldots$$
$$\{n_1, n_2, n_3, \ldots, n_{\mathcal{O}(CMT_\sigma)-3}, n_{\mathcal{O}(CMT_\sigma)-1}, n_{\mathcal{O}(CMT_\sigma)}\},$$
$$\{n_1, n_2, n_3, \ldots, n_{\mathcal{O}(CMT_\sigma)-3}, n_{\mathcal{O}(CMT_\sigma)-2}, n_{\mathcal{O}(CMT_\sigma)}\},$$
$$\{n_1, n_2, n_3, \ldots, n_{\mathcal{O}(CMT_\sigma)-3}, n_{\mathcal{O}(CMT_\sigma)-2}, n_{\mathcal{O}(CMT_\sigma)-1}\}.$$

$$\mathcal{N}^k(CMT_\sigma) = k, \; k = \mathcal{O}(CMT_\sigma) - 1.$$

Thus,

$$\mathcal{N}^{\mathcal{O}(CMT_\sigma)-1}(CMT_\sigma) = \mathcal{O}(CMT_\sigma) - 1.$$

□

Proposition 2.2. *Let $NTG : (V, E, \sigma, \mu)$ be a complete-neutrosophic graph. Then k-number-resolving number isn't equal to resolving number where $k > 1$.*

Proposition 2.3. *Let $NTG : (V, E, \sigma, \mu)$ be a complete-neutrosophic graph. Then the number of k-number-resolving sets corresponded to k-number-resolving number is $\mathcal{O}(CMT_\sigma) - 1$.*

Proposition 2.4. *Let $NTG : (V, E, \sigma, \mu)$ be a complete-neutrosophic graph. Then the number of k-number-resolving sets is $\mathcal{O}(CMT_\sigma)$.*

The clarifications about results are in progress as follows. A complete-neutrosophic graph is related to previous result and it's studied to apply the definitions on it. To make it more clear, next part gives one special case to apply definitions and results on it. Some items are devised to make more sense about new notions. A complete-neutrosophic graph is related to previous result and it's studied to apply the definitions on it, too.

Example 2.5. In Figure (2), a complete-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows.

(i) For given neutrosophic vertex, s, there's an edge with other vertices;

(ii) in the setting of complete, a vertex of resolving set corresponded to resolving number resolves as if it doesn't k-number-resolve so as resolving is different from k-number-resolving. Resolving number and k-number-resolving number are the same if $k = 1$;

(iii) all minimal k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_1, n_2, n_3\}^3, \{n_1, n_2, n_4\}^3, \{n_1, n_3, n_4\}^3.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum cardinality between all k-number-resolving sets is called k-number-resolving number and it's denoted by $\mathcal{N}^k(CMT_\sigma) = k,\ k = \mathcal{O}(CMT_\sigma) - 1$; and corresponded to k-number-resolving sets are

$$\{n_1, n_2, n_3\}^3, \{n_1, n_2, n_4\}^3, \{n_1, n_3, n_4\}^3;$$

(iv) there are four k-number-resolving sets

$$\{n_1, n_2, n_3\}^3, \{n_1, n_2, n_4\}^3, \{n_1, n_3, n_4\}^3,$$
$$\{n_1, n_2, n_3, n_4\}^4,$$

so as it's possible to have one of them as a set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is characteristic;

(v) there are three k-number-resolving sets

$$\{n_1, n_2, n_3\}^3, \{n_1, n_2, n_4\}^3, \{n_1, n_3, n_4\}^3,$$

corresponded to k-number-resolving number as if there's one k-number-resolving set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is the determiner;

(vi) all k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_1, n_2, n_3\}^3, \{n_1, n_2, n_4\}^3, \{n_1, n_3, n_4\}^3.$$

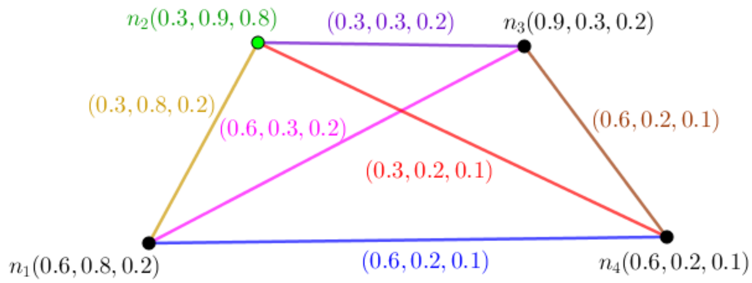

Figure 2. A Neutrosophic Graph in the Viewpoint of its k-number-resolving number and its neutrosophic k-number-resolving number.

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \dots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \dots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \dots, s_k$ in S such that $s_1, s_2, \dots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum neutrosophic cardinality between all k-number-resolving sets is called neutrosophic k-number-resolving number and it's denoted by $\mathcal{N}_n^k(CMT_\sigma) = 3.9,\ k = \mathcal{O}(CMT_\sigma) - 1$; and corresponded to k-number-resolving sets are

$$\{n_1, n_3, n_4\}^3.$$

Another class of neutrosophic graphs is addressed to path-neutrosophic graph.

Proposition 2.6. *Let $NTG : (V, E, \sigma, \mu)$ be a path-neutrosophic graph. Then*

$$\mathcal{N}^k(PTH) = k,\ k = 1, 2, 3, \dots, \mathcal{O}(PTH).$$

Proof. Suppose $PTH : (V, E, \sigma, \mu)$ is a path-neutrosophic graph. Let $n_1, n_2, \dots, n_{\mathcal{O}(PTH)}$ be a path-neutrosophic graph. For given two vertices, x and y, there's one path from x to y. In the setting of path, a vertex of resolving set corresponded to resolving number resolves as if it doesn't k-number-resolve in the setting of resolving. All minimal k-number-resolving sets corresponded to k-number-resolving number are

$$\begin{aligned}&\{n_1\}^1, \{n_{\mathcal{O}(PTH)}\}^1, \{n_i, n_j\}^2,\\&\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5,\\&\dots,\\&\{n_i, n_j, n_k, n_r, n_s, \dots, n_t\}^{\mathcal{O}(PTH)}.\end{aligned}$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \dots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \dots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices

$s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum cardinality between all k-number-resolving sets is called k-number-resolving number and it's denoted by

$$\mathcal{N}^k(PTH) = k,\ k = 1, 2, 3, \ldots, \mathcal{O}(PTH);$$

and corresponded to k-number-resolving sets are

$$\begin{aligned}&\{n_1\}^1, \{n_{\mathcal{O}(PTH)}\}^1, \{n_i, n_j\}^2,\\&\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5,\\&\ldots,\\&\{n_i, n_j, n_k, n_r, n_s, \ldots, n_t\}^{\mathcal{O}(PTH)}.\end{aligned}$$

Thus

$$\mathcal{N}^k(PTH) = k,\ k = 1, 2, 3, \ldots, \mathcal{O}(PTH).$$

□

Proposition 2.7. *Let $NTG : (V, E, \sigma, \mu)$ be a path-neutrosophic graph. If k isn't equal to one, then all leaves belong k-number-resolving sets corresponded to k-number-resolving number.*

Proposition 2.8. *Let $NTG : (V, E, \sigma, \mu)$ be a path-neutrosophic graph. If at least one leaf doesn't belong k-number-resolving sets corresponded to k-number-resolving number, then k is equal to two where $k = 1$.*

Proposition 2.9. *Let $NTG : (V, E, \sigma, \mu)$ be a path-neutrosophic graph. If at least one leaf doesn't belong k-number-resolving sets corresponded to k-number-resolving number, then k is equal to $\mathcal{O}(PTH)$ choose k where $k \neq 1$.*

Example 2.10. There are two sections for clarifications.

(a) In Figure (3), an odd-path-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows.

- (i) For given neutrosophic vertex, s, there's only one path with other vertices;
- (ii) in the setting of path, a vertex of resolving set corresponded to resolving number resolves as if it doesn't k-number-resolve in the setting of resolving;
- (iii) all minimal k-number-resolving sets corresponded to k-number-resolving number are

$$\begin{aligned}&\{n_1\}^1, \{n_5\}^1, \{n_i, n_j\}^2,\\&\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5.\end{aligned}$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum cardinality between all k-number-resolving sets is called k-number-resolving number and it's denoted by $\mathcal{N}^k(PTH) = k,\ k = 1, 2, 3, \ldots, \mathcal{O}(PTH)$; and corresponded to k-number-resolving sets are

$$\{n_1\}^1, \{n_5\}^1, \{n_i, n_j\}^2,$$
$$\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5;$$

(iv) there are some k-number-resolving sets

$$\{n_1\}^1, \{n_5\}^1, \{n_i, n_j\}^2,$$
$$\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5,$$

so as it's possible to have one of them as a set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is characteristic;

(v) there are some k-number-resolving sets

$$\{n_1\}^1, \{n_5\}^1, \{n_i, n_j\}^2,$$
$$\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5,$$

corresponded to k-number-resolving number as if there's one k-number-resolving set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is the determiner;

(vi) all k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_1\}^1, \{n_5\}^1, \{n_i, n_j\}^2,$$
$$\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum neutrosophic cardinality between all k-number-resolving sets is called neutrosophic k-number-resolving number and it's denoted by $\mathcal{N}_n^1(PTH) = 1.2, \mathcal{N}_n^2(PTH) = 1.9, \mathcal{N}_n^3(PTH) = 3.1, \mathcal{N}_n^4(PTH) = 4.5, \mathcal{N}_n^5(PTH) = 6.3$; and corresponded to k-number-resolving sets are

$$\{n_5\}^1, \{n_3, n_4\}^2, \{n_3, n_5\}^2,$$
$$\{n_3, n_4, n_5\}^3, \{n_3, n_4, n_5, n_1\}^4, \{n_1, n_2, n_3, n_4, n_5\}^5.$$

(b) In Figure (4), an even-path-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows.

(i) For given neutrosophic vertex, s, there's only one path with other vertices;

(ii) in the setting of path, a vertex of resolving set corresponded to resolving number resolves as if it doesn't k-number-resolve in the setting of resolving;

(iii) all minimal k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_1\}^1, \{n_6\}^1, \{n_i, n_j\}^2,$$
$$\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5,$$
$$\{n_i, n_j, n_k, n_r, n_s, n_t\}^6.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum cardinality between all k-number-resolving sets is called k-number-resolving number and it's denoted by $\mathcal{N}^k(PTH) = k,\ k = 1, 2, 3, \ldots, \mathcal{O}(PTH)$; and corresponded to k-number-resolving sets are

$$\{n_1\}^1, \{n_6\}^1, \{n_i, n_j\}^2,$$
$$\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5,$$
$$\{n_i, n_j, n_k, n_r, n_s, n_t\}^6;$$

(iv) there are some k-number-resolving sets

$$\{n_1\}^1, \{n_6\}^1, \{n_i, n_j\}^2,$$
$$\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5,$$
$$\{n_i, n_j, n_k, n_r, n_s, n_t\}^6,$$

so as it's possible to have one of them as a set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is characteristic;

(v) there are some k-number-resolving sets

$$\{n_1\}^1, \{n_6\}^1, \{n_i, n_j\}^2,$$
$$\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5,$$
$$\{n_i, n_j, n_k, n_r, n_s, n_t\}^6,$$

corresponded to k-number-resolving number as if there's one k-number-resolving set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is the determiner;

(vi) all k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_1\}^1, \{n_6\}^1, \{n_i, n_j\}^2,$$
$$\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5,$$
$$\{n_i, n_j, n_k, n_r, n_s, n_t\}^6.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum neutrosophic cardinality between all k-number-resolving sets is called neutrosophic k-number-resolving number and it's denoted by $\mathcal{N}_n^1(PTH) = 1.9, \mathcal{N}_n^2(PTH) = 1.8, \mathcal{N}_n^3(PTH) =$

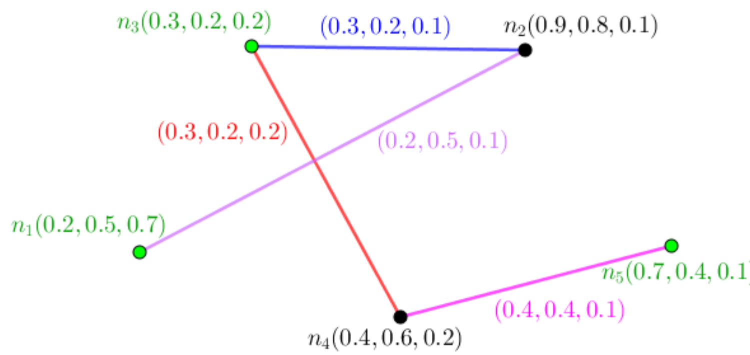

Figure 3. A Neutrosophic Graph in the Viewpoint of its k-number-resolving number and its neutrosophic k-number-resolving number.

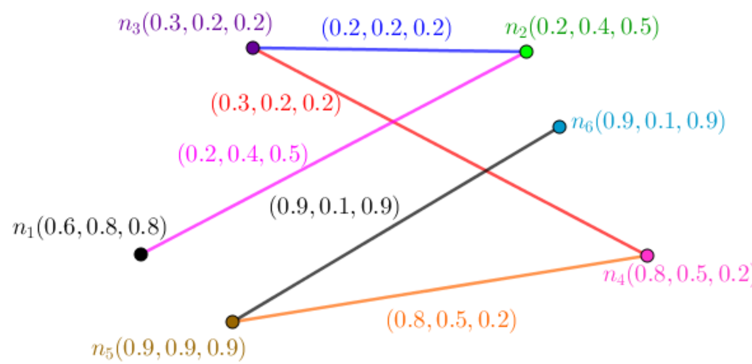

Figure 4. A Neutrosophic Graph in the Viewpoint of its k-number-resolving number and its neutrosophic k-number-resolving number.

3.3, $\mathcal{N}_n^4(PTH) = 3.9, \mathcal{N}_n^5(PTH) = 5.1, \mathcal{N}_n^6(PTH) = 7.8$; and corresponded to k-number-resolving sets are

$$\{n_6\}^1, \{n_3, n_2\}^2, \{n_3, n_2, n_4\}^3,$$
$$\{n_3, n_2, n_4, n_6\}^4, \{n_3, n_2, n_4, n_6, n_1\}^5, \{n_3, n_2, n_4, n_6, n_1, n_5\}^6.$$

Proposition 2.11. *Let $NTG : (V, E, \sigma, \mu)$ be a cycle-neutrosophic graph where $\mathcal{O}(CYC) \geq 3$. Then*

$$\mathcal{N}^k(CYC) = k, \ k = 2, 3, \ldots, \mathcal{O}(CYC).$$

Proof. Suppose $CYC : (V, E, \sigma, \mu)$ is a cycle-neutrosophic graph. For given two vertices, x and y, there are only two paths with distinct edges from x to y. Let

$$n_1, n_2, \cdots, n_{\mathcal{O}(CYC)-1}, n_{\mathcal{O}(CYC)}, n_1$$

be a cycle-neutrosophic graph $CYC : (V, E, \sigma, \mu)$. In the setting of cycle, a vertex of resolving set corresponded to resolving number resolves as if it doesn't k-number-resolve in the setting of resolving. In the setting of cycle, always $k > 1$. Antipodal vertices play roles when $k = 2$ such that they're excluded from k-number-resolving sets but they play no role when $k \neq 2$. All minimal k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_i, n_j\}^2_{\text{excluding antipodal vertices}},$$
$$\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5,$$
$$\{n_i, n_j, n_k, n_r, n_s, n_t\}^6.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum cardinality between all k-number-resolving sets is called k-number-resolving number and it's denoted by

$$\mathcal{N}^k(CYC) = k, \ k = 2, 3, \ldots, \mathcal{O}(CYC);$$

and corresponded to k-number-resolving sets are

$$\{n_i, n_j\}^2_{\text{excluding antipodal vertices}},$$
$$\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5,$$
$$\{n_i, n_j, n_k, n_r, n_s, n_t\}^6;$$

Thus

$$\mathcal{N}^k(CYC) = k, \ k = 2, 3, \ldots, \mathcal{O}(CYC).$$

□

The clarifications about results are in progress as follows. An odd-cycle-neutrosophic graph is related to previous result and it's studied to apply the definitions on it. To make it more clear, next part gives one special case to apply definitions and results on it. Some items are devised to make more sense about new notions. An even-cycle-neutrosophic graph is related to previous result and it's studied to apply the definitions on it, too.

Example 2.12. There are two sections for clarifications.

(a) In Figure (5), an even-cycle-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows.

- (i) For given neutrosophic vertex, s, there's only one path with other vertices;
- (ii) in the setting of cycle, a vertex of resolving set corresponded to resolving number resolves as if it doesn't k-number-resolve in the setting of resolving. In the setting of cycle, always $k > 1$. Antipodal vertices play roles when $k = 2$ such that they're excluded from k-number-resolving sets but they play no role when $k \neq 2$;
- (iii) all minimal k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_i, n_j\}^2_{\text{excluding antipodal vertices}},$$
$$\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5,$$
$$\{n_i, n_j, n_k, n_r, n_s, n_t\}^6.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum cardinality between all k-number-resolving sets is called k-number-resolving number and it's denoted by $\mathcal{N}^k(CYC) = k,\ k = 2, 3, \ldots, \mathcal{O}(CYC)$; and corresponded to k-number-resolving sets are

$$\{n_i, n_j\}^2_{\text{excluding antipodal vertices}},$$
$$\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5,$$
$$\{n_i, n_j, n_k, n_r, n_s, n_t\}^6;$$

(iv) there are some k-number-resolving sets

$$\{n_i, n_j\}^2_{\text{excluding antipodal vertices}},$$
$$\{n_i, n_j, n_k\}^{2,3}, \{n_i, n_j, n_k, n_r\}^{2,3,4}, \{n_i, n_j, n_k, n_r, n_s\}^{2,3,4,5},$$
$$\{n_i, n_j, n_k, n_r, n_s, n_t\}^{2,3,4,5,6},$$

so as it's possible to have one of them as a set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is characteristic;

(v) there are some k-number-resolving sets

$$\{n_i, n_j\}^2_{\text{excluding antipodal vertices}},$$
$$\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5,$$
$$\{n_i, n_j, n_k, n_r, n_s, n_t\}^6,$$

corresponded to k-number-resolving number as if there's one k-number-resolving set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is the determiner;

(vi) all k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_i, n_j\}^2_{\text{excluding antipodal vertices}},$$
$$\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5,$$
$$\{n_i, n_j, n_k, n_r, n_s, n_t\}^6.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum neutrosophic cardinality between all k-number-resolving sets is called neutrosophic k-number-resolving number and it's denoted by $\mathcal{N}_n^2(CYC) = 1.3, \mathcal{N}_n^3(CYC) = 2.6, \mathcal{N}_n^4(CYC) = 4.1, \mathcal{N}_n^5(CYC) = 6.0, \mathcal{N}_n^6(CYC) = 7.5$; and corresponded to k-number-resolving sets are

$$\{n_1, n_5\}^2,$$
$$\{n_1, n_5, n_4\}^3, \{n_1, n_5, n_4, n_6\}^4, \{n_1, n_5, n_4, n_6, n_3\}^5,$$
$$\{n_1, n_5, n_4, n_6, n_3, n_2\}^6.$$

(b) In Figure (6), an odd-cycle-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows.

(i) For given neutrosophic vertex, s, there's only one path with other vertices;

(ii) in the setting of cycle, a vertex of resolving set corresponded to resolving number resolves as if it doesn't k-number-resolve in the setting of resolving. In the setting of cycle, always $k > 1$;

(iii) all minimal k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_i, n_j\}^2, \{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4,$$
$$\{n_i, n_j, n_k, n_r, n_s\}^5.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum cardinality between all k-number-resolving sets is called k-number-resolving number and it's denoted by $\mathcal{N}^k(CYC) = k,\ k = 2, 3, \ldots, \mathcal{O}(CYC)$; and corresponded to k-number-resolving sets are

$$\{n_i, n_j\}^2, \{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4,$$
$$\{n_i, n_j, n_k, n_r, n_s\}^5;$$

(iv) there are some k-number-resolving sets

$$\{n_i, n_j\}^2, \{n_i, n_j, n_k\}^{2,3}, \{n_i, n_j, n_k, n_r\}^{2,3,4},$$
$$\{n_i, n_j, n_k, n_r, n_s\}^{2,3,4,5},$$

so as it's possible to have one of them as a set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is characteristic;

(v) there are some k-number-resolving sets

$$\{n_i, n_j\}^2, \{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4,$$
$$\{n_i, n_j, n_k, n_r, n_s\}^5,$$

corresponded to k-number-resolving number as if there's one k-number-resolving set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is the determiner;

(vi) all k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_i, n_j\}^2, \{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4,$$
$$\{n_i, n_j, n_k, n_r, n_s\}^5.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

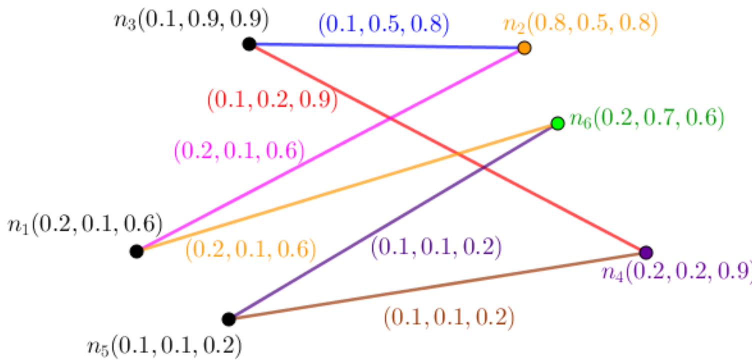

Figure 5. A Neutrosophic Graph in the Viewpoint of its k-number-resolving number and its neutrosophic k-number-resolving number.

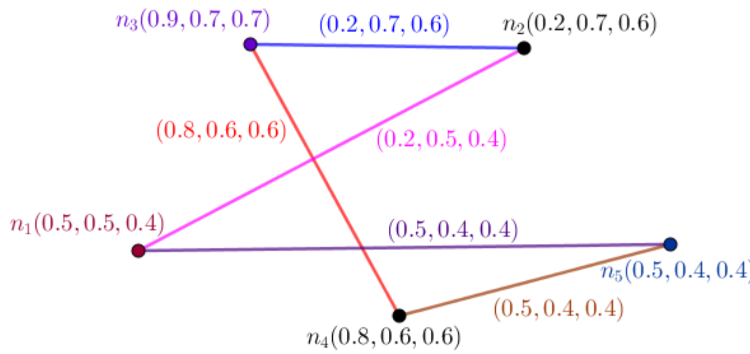

Figure 6. A Neutrosophic Graph in the Viewpoint of its k-number-resolving number and its neutrosophic k-number-resolving number.

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum neutrosophic cardinality between all k-number-resolving sets is called neutrosophic k-number-resolving number and it's denoted by
$\mathcal{N}_n^2(CYC) = 2.7, \mathcal{N}_n^3(CYC) = 4.2, \mathcal{N}_n^4(CYC) = 6.2, \mathcal{N}_n^5(CYC) = 8.5$; and corresponded to k-number-resolving sets are

$$\{n_1, n_5\}^2, \{n_1, n_5, n_2\}^3, \{n_1, n_5, n_2, n_4\}^4,$$
$$\{n_1, n_5, n_2, n_4, n_3\}^5.$$

Proposition 2.13. *Let $NTG : (V, E, \sigma, \mu)$ be a star-neutrosophic graph with center c. Then*

$$\mathcal{N}^{\mathcal{O}(STR_{1,\sigma_2})-2}(STR_{1,\sigma_2}) = \mathcal{O}(STR_{1,\sigma_2}) - 2.$$
$$\mathcal{N}^{\mathcal{O}(STR_{1,\sigma_2})-1}(STR_{1,\sigma_2}) = \mathcal{O}(STR_{1,\sigma_2}) - 1.$$
$$\mathcal{N}^{\mathcal{O}(STR_{1,\sigma_2})}(STR_{1,\sigma_2}) = \mathcal{O}(STR_{1,\sigma_2}).$$
$$k = \mathcal{O}(STR_{1,\sigma_2}) - 2, \mathcal{O}(STR_{1,\sigma_2}) - 1, \mathcal{O}(STR_{1,\sigma_2}).$$

Proof. Suppose $STR_{1,\sigma_2} : (V, E, \sigma, \mu)$ is a star-neutrosophic graph. An edge always has center, c, as one of its endpoints where $n_{\mathcal{O}(STR_{1,\sigma_2})} = c$. All paths have one as their lengths, forever. In the setting of star, a vertex of resolving set corresponded to resolving number resolves as if it doesn't k-number-resolve in the setting of resolving. All minimal k-number-resolving sets corresponded to k-number-resolving number are

$$V \setminus \{n_{\mathcal{O}(STR_{1,\sigma_2})}, n_i\}_{n_i \neq n_{\mathcal{O}(STR_{1,\sigma_2})}}^{\mathcal{O}(STR_{1,\sigma_2})-2}, V \setminus \{n_i\}^{\mathcal{O}(STR_{1,\sigma_2})-1}, V^{\mathcal{O}(STR_{1,\sigma_2})}.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum cardinality between all k-number-resolving sets is called k-number-resolving number and it's denoted by

$$\mathcal{N}^{\mathcal{O}(STR_{1,\sigma_2})-2}(STR_{1,\sigma_2}) = \mathcal{O}(STR_{1,\sigma_2}) - 2.$$
$$\mathcal{N}^{\mathcal{O}(STR_{1,\sigma_2})-1}(STR_{1,\sigma_2}) = \mathcal{O}(STR_{1,\sigma_2}) - 1.$$
$$\mathcal{N}^{\mathcal{O}(STR_{1,\sigma_2})}(STR_{1,\sigma_2}) = \mathcal{O}(STR_{1,\sigma_2}).$$
$$k = \mathcal{O}(STR_{1,\sigma_2}) - 2, \mathcal{O}(STR_{1,\sigma_2}) - 1, \mathcal{O}(STR_{1,\sigma_2});$$

and corresponded to k-number-resolving sets are

$$V \setminus \{n_{\mathcal{O}(STR_{1,\sigma_2})}, n_i\}_{n_i \neq n_{\mathcal{O}(STR_{1,\sigma_2})}}^{\mathcal{O}(STR_{1,\sigma_2})-2}, V \setminus \{n_i\}^{\mathcal{O}(STR_{1,\sigma_2})-1}, V^{\mathcal{O}(STR_{1,\sigma_2})}.$$

Thus

$$\mathcal{N}^{\mathcal{O}(STR_{1,\sigma_2})-2}(STR_{1,\sigma_2}) = \mathcal{O}(STR_{1,\sigma_2}) - 2.$$
$$\mathcal{N}^{\mathcal{O}(STR_{1,\sigma_2})-1}(STR_{1,\sigma_2}) = \mathcal{O}(STR_{1,\sigma_2}) - 1.$$
$$\mathcal{N}^{\mathcal{O}(STR_{1,\sigma_2})}(STR_{1,\sigma_2}) = \mathcal{O}(STR_{1,\sigma_2}).$$
$$k = \mathcal{O}(STR_{1,\sigma_2}) - 2, \mathcal{O}(STR_{1,\sigma_2}) - 1, \mathcal{O}(STR_{1,\sigma_2}).$$

□

Proposition 2.14. *Let $NTG : (V, E, \sigma, \mu)$ be a star-neutrosophic graph. Then k-number-resolving number isn't equal to resolving number where $k \neq 1$.*

Proposition 2.15. *Let $NTG : (V, E, \sigma, \mu)$ be a star-neutrosophic graph with center c. Then*

(i) the number of k-number-resolving sets is $\mathcal{O}(STR_{1,\sigma_2})$ choose $\mathcal{O}(STR_{1,\sigma_2}) - 2$ plus $\mathcal{O}(STR_{1,\sigma_2})$ plus one where $k = \mathcal{O}(STR_{1,\sigma_2}) - 2$;

(ii) the number of k-number-resolving sets is $\mathcal{O}(STR_{1,\sigma_2})$ plus one where $k = \mathcal{O}(STR_{1,\sigma_2}) - 1$;

(iii) the number of k-number-resolving sets is one where $k = \mathcal{O}(STR_{1,\sigma_2})$.

Proposition 2.16. *Let $NTG : (V, E, \sigma, \mu)$ be a star-neutrosophic graph with center c. Then*

(i) *the number of k-number-resolving sets corresponded to k-number-resolving number is* $\mathcal{O}(STR_{1,\sigma_2})$ *choose* $\mathcal{O}(STR_{1,\sigma_2}) - 2$ *where* $k = \mathcal{O}(STR_{1,\sigma_2}) - 2$;

(ii) *the number of k-number-resolving sets corresponded to k-number-resolving number is* $\mathcal{O}(STR_{1,\sigma_2})$ *where* $k = \mathcal{O}(STR_{1,\sigma_2}) - 1$;

(iii) *the number of k-number-resolving sets corresponded to k-number-resolving number is one where* $k = \mathcal{O}(STR_{1,\sigma_2})$.

The clarifications about results are in progress as follows. A star-neutrosophic graph is related to previous result and it's studied to apply the definitions on it. To make it more clear, next part gives one special case to apply definitions and results on it. Some items are devised to make more sense about new notions. A star-neutrosophic graph is related to previous result and it's studied to apply the definitions on it, too.

Example 2.17. There is one section for clarifications. In Figure (7), a star-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows.

(i) For given two neutrosophic vertices, s and n_1, there's only one path, precisely one edge between them and there's no path despite them;

(ii) in the setting of star, a vertex of resolving set corresponded to resolving number resolves as if it doesn't k-number-resolve in the setting of resolving;

(iii) all minimal k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_2,n_3,n_4\}^3, \{n_2,n_3,n_5\}^3, \{n_2,n_4,n_5\}^3,$$
$$\{n_3,n_4,n_5\}^3, \{n_1,n_2,n_3,n_4\}^4, \{n_1,n_2,n_3,n_5\}^4,$$
$$\{n_1,n_2,n_4,n_5\}^4, \{n_1,n_3,n_4,n_5\}^4, \{n_2,n_3,n_4,n_5\}^4,$$
$$\{n_1,n_2,n_3,n_4,n_5\}^5.$$

For given vertices n and n' if

$$d(s_1,n) \neq d(s_1,n'), d(s_2,n) \neq d(s_2,n'), \ldots, d(s_k,n) \neq d(s_k,n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum cardinality between all k-number-resolving sets is called k-number-resolving number and it's denoted by $\mathcal{N}^k(STR_{1,\sigma_2}) = k,\ k = \mathcal{O}(STR_{1,\sigma_2}) - 2, \mathcal{O}(STR_{1,\sigma_2}) - 1, \mathcal{O}(STR_{1,\sigma_2})$; and corresponded to k-number-resolving sets are

$$\{n_2,n_3,n_4\}^3, \{n_2,n_3,n_5\}^3, \{n_2,n_4,n_5\}^3,$$
$$\{n_3,n_4,n_5\}^3, \{n_1,n_2,n_3,n_4\}^4, \{n_1,n_2,n_3,n_5\}^4,$$
$$\{n_1,n_2,n_4,n_5\}^4, \{n_1,n_3,n_4,n_5\}^4, \{n_2,n_3,n_4,n_5\}^4,$$
$$\{n_1,n_2,n_3,n_4,n_5\}^5;$$

(iv) there are ten k-number-resolving sets

$$\{n_2,n_3,n_4\}^3, \{n_2,n_3,n_5\}^3, \{n_2,n_4,n_5\}^3,$$
$$\{n_3,n_4,n_5\}^3, \{n_1,n_2,n_3,n_4\}^4, \{n_1,n_2,n_3,n_5\}^4,$$
$$\{n_1,n_2,n_4,n_5\}^4, \{n_1,n_3,n_4,n_5\}^4, \{n_2,n_3,n_4,n_5\}^4,$$
$$\{n_1,n_2,n_3,n_4,n_5\}^5,$$

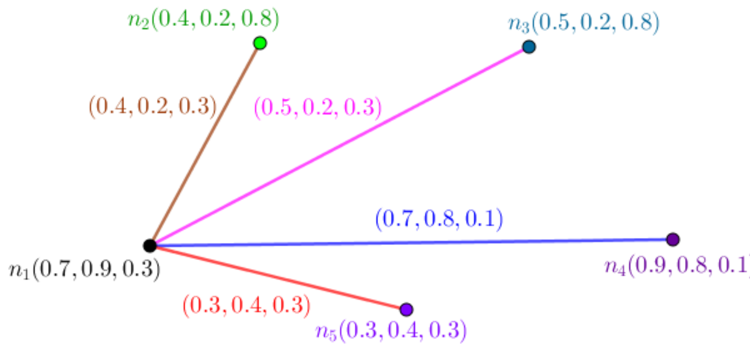

Figure 7. A Neutrosophic Graph in the Viewpoint of its k-number-resolving number and its neutrosophic k-number-resolving number.

so as it's possible to have one of them as a set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is characteristic;

(v) there are ten k-number-resolving sets

$$\{n_2, n_3, n_4\}^3, \{n_2, n_3, n_5\}^3, \{n_2, n_4, n_5\}^3,$$
$$\{n_3, n_4, n_5\}^3, \{n_1, n_2, n_3, n_4\}^4, \{n_1, n_2, n_3, n_5\}^4,$$
$$\{n_1, n_2, n_4, n_5\}^4, \{n_1, n_3, n_4, n_5\}^4, \{n_2, n_3, n_4, n_5\}^4,$$
$$\{n_1, n_2, n_3, n_4, n_5\}^5,$$

corresponded to k-number-resolving number as if there's one k-number-resolving set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is the determiner;

(vi) all k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_i, n_j\}^2, \{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4,$$
$$\{n_i, n_j, n_k, n_r, n_s\}^5.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum neutrosophic cardinality between all k-number-resolving sets is called neutrosophic k-number-resolving number and it's denoted by $\mathcal{N}_n^3(STR_{1,\sigma_2}) = 3.9, \mathcal{N}_n^4(STR_{1,\sigma_2}) = 5.8, \mathcal{N}_n^5(STR_{1,\sigma_2}) = 7.6$; and corresponded to k-number-resolving sets are

$$\{n_2, n_3, n_5\}^3, \{n_1, n_2, n_3, n_5\}^4, \{n_1, n_2, n_3, n_4, n_5\}^5.$$

Proposition 2.18. *Let $NTG : (V, E, \sigma, \mu)$ be a complete-bipartite-neutrosophic graph which isn't star-neutrosophic graph which means $|V_1|, |V_2| \geq 2$. Then*

$$\mathcal{N}^{\mathcal{O}(CMC_{\sigma_1,\sigma_2})-2}(CMC_{\sigma_1,\sigma_2}) = \mathcal{O}(CMC_{\sigma_1,\sigma_2}) - 2.$$

$$\mathcal{N}^{\mathcal{O}(CMC_{\sigma_1,\sigma_2})-1}(CMC_{\sigma_1,\sigma_2}) = \mathcal{O}(CMC_{\sigma_1,\sigma_2}) - 1.$$
$$\mathcal{N}^{\mathcal{O}(CMC_{\sigma_1,\sigma_2})}(CMC_{\sigma_1,\sigma_2}) = \mathcal{O}(CMC_{\sigma_1,\sigma_2}).$$
$$k = \mathcal{O}(CMC_{\sigma_1,\sigma_2}) - 2, \mathcal{O}(CMC_{\sigma_1,\sigma_2}) - 1, \mathcal{O}(CMC_{\sigma_1,\sigma_2}).$$

Proof. Suppose $CMC_{\sigma_1,\sigma_2} : (V, E, \sigma, \mu)$ is a complete-bipartite-neutrosophic graph. Every vertex in a part and another vertex in opposite part k-number-resolves any given vertex. Assume same parity for same partition of vertex set which means V_1 has odd indexes and V_2 has even indexes. In the setting of complete-bipartite, a vertex of resolving set corresponded to resolving number resolves as if it doesn't k-number-resolve so as resolving is different from k-number-resolving. All minimal k-number-resolving sets corresponded to k-number-resolving number are

$$V \setminus \{n_i^1, n_j^2\}_{n_i^1 \neq n_j^2}^{\mathcal{O}(CMC_{\sigma_1,\sigma_2})-2}, V \setminus \{n_i\}^{\mathcal{O}(CMC_{\sigma_1,\sigma_2})-1}, V^{\mathcal{O}(CMC_{\sigma_1,\sigma_2})}.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum cardinality between all k-number-resolving sets is called k-number-resolving number and it's denoted by

$$\mathcal{N}^{\mathcal{O}(CMC_{\sigma_1,\sigma_2})-2}(CMC_{\sigma_1,\sigma_2}) = \mathcal{O}(CMC_{\sigma_1,\sigma_2}) - 2.$$
$$\mathcal{N}^{\mathcal{O}(CMC_{\sigma_1,\sigma_2})-1}(CMC_{\sigma_1,\sigma_2}) = \mathcal{O}(CMC_{\sigma_1,\sigma_2}) - 1.$$
$$\mathcal{N}^{\mathcal{O}(CMC_{\sigma_1,\sigma_2})}(CMC_{\sigma_1,\sigma_2}) = \mathcal{O}(CMC_{\sigma_1,\sigma_2}).$$
$$k = \mathcal{O}(CMC_{\sigma_1,\sigma_2}) - 2, \mathcal{O}(CMC_{\sigma_1,\sigma_2}) - 1, \mathcal{O}(CMC_{\sigma_1,\sigma_2});$$

and corresponded to k-number-resolving sets are

$$V \setminus \{n_i^1, n_j^2\}_{n_i^1 \neq n_j^2}^{\mathcal{O}(CMC_{\sigma_1,\sigma_2})-2}, V \setminus \{n_i\}^{\mathcal{O}(CMC_{\sigma_1,\sigma_2})-1}, V^{\mathcal{O}(CMC_{\sigma_1,\sigma_2})}.$$

Thus

$$\mathcal{N}^{\mathcal{O}(CMC_{\sigma_1,\sigma_2})-2}(CMC_{\sigma_1,\sigma_2}) = \mathcal{O}(CMC_{\sigma_1,\sigma_2}) - 2.$$
$$\mathcal{N}^{\mathcal{O}(CMC_{\sigma_1,\sigma_2})-1}(CMC_{\sigma_1,\sigma_2}) = \mathcal{O}(CMC_{\sigma_1,\sigma_2}) - 1.$$
$$\mathcal{N}^{\mathcal{O}(CMC_{\sigma_1,\sigma_2})}(CMC_{\sigma_1,\sigma_2}) = \mathcal{O}(CMC_{\sigma_1,\sigma_2}).$$
$$k = \mathcal{O}(CMC_{\sigma_1,\sigma_2}) - 2, \mathcal{O}(CMC_{\sigma_1,\sigma_2}) - 1, \mathcal{O}(CMC_{\sigma_1,\sigma_2}).$$

□

Proposition 2.19. *Let $NTG : (V, E, \sigma, \mu)$ be a complete-bipartite-neutrosophic graph. Then k-number-resolving number isn't equal to resolving number where $k \neq 1$.*

Proposition 2.20. *Let $NTG : (V, E, \sigma, \mu)$ be a complete-bipartite-neutrosophic graph with center c. Then*

(i) *the number of k-number-resolving sets is $|V_1|$ multiplying $|V_2|$ plus $\mathcal{O}(CMC_{\sigma_1,\sigma_2})$ plus one where $k = \mathcal{O}(CMC_{\sigma_1,\sigma_2}) - 2$;*

(*ii*) *the number of k-number-resolving sets is* $\mathcal{O}(CMC_{\sigma_1,\sigma_2})$ *plus one where* $k = \mathcal{O}(CMC_{\sigma_1,\sigma_2}) - 1$;

(*iii*) *the number of k-number-resolving sets is one where* $k = \mathcal{O}(CMC_{\sigma_1,\sigma_2})$.

Proposition 2.21. *Let* $NTG : (V, E, \sigma, \mu)$ *be a complete-bipartite-neutrosophic graph with center c. Then*

(*i*) *the number of k-number-resolving sets corresponded to k-number-resolving number is* $|V_1|$ *multiplying* $|V_2|$ *where* $k = \mathcal{O}(CMC_{\sigma_1,\sigma_2}) - 2$;

(*ii*) *the number of k-number-resolving sets corresponded to k-number-resolving number is* $\mathcal{O}(CMC_{\sigma_1,\sigma_2})$ *where* $k = \mathcal{O}(CMC_{\sigma_1,\sigma_2}) - 1$;

(*iii*) *the number of k-number-resolving sets corresponded to k-number-resolving number is one where* $k = \mathcal{O}(CMC_{\sigma_1,\sigma_2})$.

The clarifications about results are in progress as follows. A complete-bipartite-neutrosophic graph is related to previous result and it's studied to apply the definitions on it. To make it more clear, next part gives one special case to apply definitions and results on it. Some items are devised to make more senses about new notions. A complete-bipartite-neutrosophic graph is related to previous result and it's studied to apply the definitions on it, too.

Example 2.22. There is one section for clarifications. In Figure (8), a complete-bipartite-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows.

(*i*) For given two neutrosophic vertices, n and n', there is either one path with length one or one path with length two between them;

(*ii*) in the setting of complete-bipartite, a vertex of resolving set corresponded to resolving number resolves as if it doesn't k-number-resolve so as resolving is different from k-number-resolving;

(*iii*) all minimal k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_1, n_2\}^2, \{n_1, n_3\}^2, \{n_4, n_2\}^2,$$
$$\{n_4, n_3\}^2, \{n_1, n_2, n_3\}^3, \{n_1, n_2, n_4\}^3,$$
$$\{n_1, n_3, n_4\}^3, \{n_2, n_3, n_4\}^3, \{n_1, n_2, n_3, n_4\}^4.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum cardinality between all k-number-resolving sets is called k-number-resolving number and it's denoted by
$\mathcal{N}^k(CMC_{\sigma_1,\sigma_2}) = k, \ k = \mathcal{O}(CMC_{\sigma_1,\sigma_2}) - 2, \mathcal{O}(CMC_{\sigma_1,\sigma_2}) - 1, \mathcal{O}(CMC_{\sigma_1,\sigma_2})$;
and corresponded to k-number-resolving sets are

$$\{n_1, n_2\}^2, \{n_1, n_3\}^2, \{n_4, n_2\}^2,$$
$$\{n_4, n_3\}^2, \{n_1, n_2, n_3\}^3, \{n_1, n_2, n_4\}^3,$$
$$\{n_1, n_3, n_4\}^3, \{n_2, n_3, n_4\}^3, \{n_1, n_2, n_3, n_4\}^4;$$

(iv) there are nine k-number-resolving sets

$$\{n_1,n_2\}^2,\{n_1,n_3\}^2,\{n_4,n_2\}^2,$$
$$\{n_4,n_3\}^2,\{n_1,n_2,n_3\}^{2,3},\{n_1,n_2,n_4\}^{2,3},$$
$$\{n_1,n_3,n_4\}^{2,3},\{n_2,n_3,n_4\}^{2,3},\{n_1,n_2,n_3,n_4\}^{2,3,4},$$

so as it's possible to have one of them as a set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is characteristic;

(v) there are nine k-number-resolving sets

$$\{n_1,n_2\}^2,\{n_1,n_3\}^2,\{n_4,n_2\}^2,$$
$$\{n_4,n_3\}^2,\{n_1,n_2,n_3\}^3,\{n_1,n_2,n_4\}^3,$$
$$\{n_1,n_3,n_4\}^3,\{n_2,n_3,n_4\}^3,\{n_1,n_2,n_3,n_4\}^4,$$

corresponded to k-number-resolving number as if there's one k-number-resolving set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is the determiner;

(vi) all k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_1,n_2\}^2,\{n_1,n_3\}^2,\{n_4,n_2\}^2,$$
$$\{n_4,n_3\}^2,\{n_1,n_2,n_3\}^3,\{n_1,n_2,n_4\}^3,$$
$$\{n_1,n_3,n_4\}^3,\{n_2,n_3,n_4\}^3,\{n_1,n_2,n_3,n_4\}^4.$$

For given vertices n and n' if

$$d(s_1,n)\neq d(s_1,n'),d(s_2,n)\neq d(s_2,n'),\dots,d(s_k,n)\neq d(s_k,n'),$$

then $s_1,s_2,\dots,s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V\setminus S$, there are at least neutrosophic vertices $s_1,s_2,\dots,s_k$ in S such that $s_1,s_2,\dots,s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum neutrosophic cardinality between all k-number-resolving sets is called neutrosophic k-number-resolving number and it's denoted by $\mathcal{N}_n^2(CMC_{\sigma_1,\sigma_2})=2.4,\mathcal{N}_n^3(CMC_{\sigma_1,\sigma_2})=3.9,\mathcal{N}_n^4(CMC_{\sigma_1,\sigma_2})=5.8$; and corresponded to k-number-resolving sets are

$$\{n_4,n_2\}^2,\{n_2,n_3,n_4\}^3,\{n_1,n_2,n_3,n_4\}^4.$$

Proposition 2.23. *Let $NTG:(V,E,\sigma,\mu)$ be a complete-t-partite-neutrosophic graph where $t\geq 3$ and $|V_i\geq 2$. Then*

$$\mathcal{N}^{\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})-2}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})=\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})-2.$$

$$\mathcal{N}^{\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})-1}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})=\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})-1.$$

$$\mathcal{N}^{\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})=\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}).$$

$$k=\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})-2,\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})-1,\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}).$$

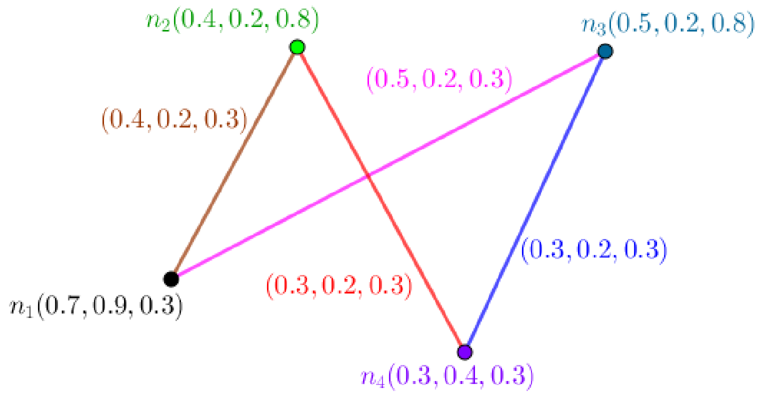

Figure 8. A Neutrosophic Graph in the Viewpoint of its k-number-resolving number and its neutrosophic k-number-resolving number.

Proof. Suppose $CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t} : (V, E, \sigma, \mu)$ is a complete-t-partite-neutrosophic graph. Every vertex in a part is k-number-resolved by another vertex in another part. Assume same parity for same partition of vertex set which means V_i has odd indexes and V_j has even indexes. In the setting of complete-t-partite, a vertex of resolving set corresponded to resolving number resolves as if it doesn't k-number-resolve so as resolving is different from k-number-resolving. All minimal k-number-resolving sets corresponded to k-number-resolving number are

$$V \setminus \{n_i^r, n_j^s\}_{n_i^r \neq n_j^s}^{\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})-2}, V \setminus \{n_i\}^{\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})-1}, V^{\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})}.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum cardinality between all k-number-resolving sets is called k-number-resolving number and it's denoted by

$$\mathcal{N}^{\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})-2}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) = \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) - 2.$$
$$\mathcal{N}^{\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})-1}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) = \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) - 1.$$
$$\mathcal{N}^{\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) = \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}).$$
$$k = \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) - 2, \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) - 1, \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t});$$

and corresponded to k-number-resolving sets are

$$V \setminus \{n_i^r, n_j^s\}_{n_i^r \neq n_j^s}^{\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})-2}, V \setminus \{n_i\}^{\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})-1}, V^{\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})}.$$

Thus

$$\mathcal{N}^{\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})-2}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) = \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) - 2.$$
$$\mathcal{N}^{\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})-1}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) = \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) - 1.$$
$$\mathcal{N}^{\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) = \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}).$$
$$k = \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) - 2, \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) - 1, \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}).$$

□

Proposition 2.24. *Let $NTG : (V, E, \sigma, \mu)$ be a complete-t-partite-neutrosophic graph. Then k-number-resolving number isn't equal to resolving number where $k \neq 1$.*

Proposition 2.25. *Let $NTG : (V, E, \sigma, \mu)$ be a complete-t-partite-neutrosophic graph with center c. Then*

(i) *the number of k-number-resolving sets is $|V_1|$ multiplying $|V_2|$ plus $\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})$ plus one where $k = \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) - 2$;*

(ii) *the number of k-number-resolving sets is $\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})$ plus one where $k = \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) - 1$;*

(iii) *the number of k-number-resolving sets is one where $k = \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})$.*

Proposition 2.26. *Let $NTG : (V, E, \sigma, \mu)$ be a complete-t-partite-neutrosophic graph with center c. Then*

(i) *the number of k-number-resolving sets corresponded to k-number-resolving number is $|V_1|$ multiplying $|V_2|$ where $k = \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) - 2$;*

(ii) *the number of k-number-resolving sets corresponded to k-number-resolving number is $\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})$ where $k = \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) - 1$;*

(iii) *the number of k-number-resolving sets corresponded to k-number-resolving number is one where $k = \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})$.*

Example 2.27. There is one section for clarifications. In Figure (9), a complete-t-partite-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows.

(i) For given two neutrosophic vertices, n and n', there is either one path with length one or one path with length two between them;

(ii) in the setting of complete-t-partite, a vertex of resolving set corresponded to resolving number resolves as if it doesn't k-number-resolve so as resolving is different from k-number-resolving;

(iii) all minimal k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_1, n_2, n_3\}^3, \{n_1, n_2, n_5\}^3, \{n_1, n_3, n_5\}^3,$$
$$\{n_4, n_2, n_3\}^3, \{n_4, n_2, n_5\}^3, \{n_4, n_3, n_5\}^3,$$
$$\{n_1, n_2, n_3, n_4\}^4, \{n_1, n_2, n_3, n_5\}^4, \{n_1, n_2, n_4, n_5\}^4,$$
$$\{n_1, n_3, n_4, n_5\}^4, \{n_2, n_3, n_4, n_5\}^4, \{n_1, n_2, n_3, n_4, n_5\}^5.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum cardinality between all k-number-resolving sets is called k-number-resolving number and it's denoted by $\mathcal{N}^k(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) = k,\ k =$

$\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})-2, \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})-1, \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})$; and corresponded to k-number-resolving sets are

$$\{n_1,n_2,n_3\}^3,\{n_1,n_2,n_5\}^3,\{n_1,n_3,n_5\}^3,$$
$$\{n_4,n_2,n_3\}^3,\{n_4,n_2,n_5\}^3,\{n_4,n_3,n_5\}^3,$$
$$\{n_1,n_2,n_3,n_4\}^4,\{n_1,n_2,n_3,n_5\}^4,\{n_1,n_2,n_4,n_5\}^4,$$
$$\{n_1,n_3,n_4,n_5\}^4,\{n_2,n_3,n_4,n_5\}^4,\{n_1,n_2,n_3,n_4,n_5\}^5;$$

(iv) there are sixteen k-number-resolving sets

$$\{n_1,n_2,n_3\}^3,\{n_1,n_2,n_5\}^3,\{n_1,n_3,n_5\}^3,$$
$$\{n_4,n_2,n_3\}^3,\{n_4,n_2,n_5\}^3,\{n_4,n_3,n_5\}^3,$$
$$\{n_1,n_2,n_3,n_4\}^{3,4},\{n_1,n_2,n_3,n_5\}^{3,4},\{n_1,n_2,n_4,n_5\}^{3,4},$$
$$\{n_1,n_3,n_4,n_5\}^{3,4},\{n_2,n_3,n_4,n_5\}^{3,4},\{n_1,n_2,n_3,n_4,n_5\}^{3,4,5},$$

so as it's possible to have one of them as a set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is characteristic;

(v) there are sixteen k-number-resolving sets

$$\{n_1,n_2,n_3\}^3,\{n_1,n_2,n_5\}^3,\{n_1,n_3,n_5\}^3,$$
$$\{n_4,n_2,n_3\}^3,\{n_4,n_2,n_5\}^3,\{n_4,n_3,n_5\}^3,$$
$$\{n_1,n_2,n_3,n_4\}^4,\{n_1,n_2,n_3,n_5\}^4,\{n_1,n_2,n_4,n_5\}^4,$$
$$\{n_1,n_3,n_4,n_5\}^4,\{n_2,n_3,n_4,n_5\}^4,\{n_1,n_2,n_3,n_4,n_5\}^5,$$

corresponded to k-number-resolving number as if there's one k-number-resolving set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is the determiner;

(vi) all k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_1,n_2,n_3\}^3,\{n_1,n_2,n_5\}^3,\{n_1,n_3,n_5\}^3,$$
$$\{n_4,n_2,n_3\}^3,\{n_4,n_2,n_5\}^3,\{n_4,n_3,n_5\}^3,$$
$$\{n_1,n_2,n_3,n_4\}^4,\{n_1,n_2,n_3,n_5\}^4,\{n_1,n_2,n_4,n_5\}^4,$$
$$\{n_1,n_3,n_4,n_5\}^4,\{n_2,n_3,n_4,n_5\}^4,\{n_1,n_2,n_3,n_4,n_5\}^5.$$

For given vertices n and n' if

$$d(s_1,n)\neq d(s_1,n'), d(s_2,n)\neq d(s_2,n'),\ldots,d(s_k,n)\neq d(s_k,n'),$$

then $s_1,s_2,\ldots,s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V\setminus S$, there are at least neutrosophic vertices $s_1,s_2,\ldots,s_k$ in S such that $s_1,s_2,\ldots,s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum neutrosophic cardinality between all k-number-resolving sets is called neutrosophic k-number-resolving number and it's denoted by $\mathcal{N}_n^3(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})=3.8, \mathcal{N}_n^4(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})=5.3, \mathcal{N}_n^5(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})=7.2$; and corresponded to k-number-resolving sets are

$$\{n_4,n_2,n_5\}^3,\{n_2,n_3,n_4,n_5\}^4,\{n_1,n_2,n_3,n_4,n_5\}^5.$$

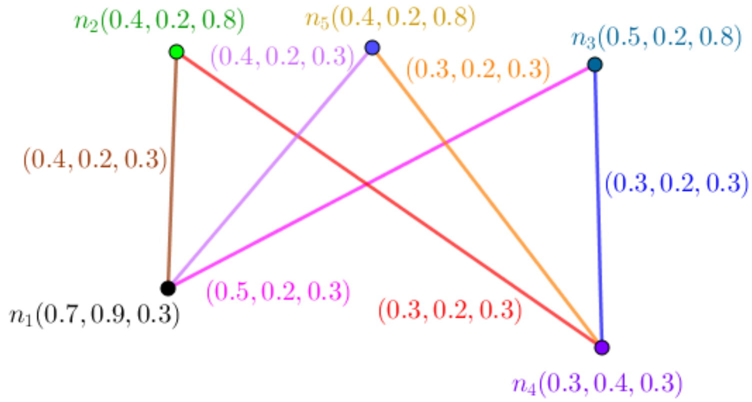

Figure 9. A Neutrosophic Graph in the Viewpoint of its k-number-resolving number and its neutrosophic k-number-resolving number.

Proposition 2.28. *Let $NTG : (V, E, \sigma, \mu)$ be a wheel-neutrosophic graph. Then*

$$\mathcal{N}^1 = \mathcal{O}(WHL_{1,\sigma_2}) - 3.$$

$$\mathcal{N}^{\mathcal{O}(WHL_{1,\sigma_2})-1}(WHL_{1,\sigma_2}) = \mathcal{O}(WHL_{1,\sigma_2}) - 1.$$

$$\mathcal{N}^{\mathcal{O}(WHL_{1,\sigma_2})}(WHL_{1,\sigma_2}) = \mathcal{O}(WHL_{1,\sigma_2}).$$

$$k = 1, \mathcal{O}(WHL_{1,\sigma_2}) - 1, \mathcal{O}(WHL_{1,\sigma_2}).$$

Proof. Suppose $WHL_{1,\sigma_2} : (V, E, \sigma, \mu)$ is a wheel-neutrosophic graph. The argument is elementary. All vertices of a cycle

$$n_1, n_2, n_3, \cdots, n_{\mathcal{O}(WHL_{1,\sigma_2})-3}, n_{\mathcal{O}(WHL_{1,\sigma_2})-2}, n_{\mathcal{O}(WHL_{1,\sigma_2})-1}, n_1$$

join to one vertex, $c = n_{\mathcal{O}(WHL_{1,\sigma_2})}$. For every vertices, the minimum number of edges amid them is either one or two because of center and the notion of neighbors. In the setting of wheel, a vertex of resolving set corresponded to resolving number resolves as if it doesn't k-number-resolve so as resolving is different from k-number-resolving. All minimal k-number-resolving sets corresponded to k-number-resolving number are

$$V \setminus \{n_i^r, n_j^s, n_{\mathcal{O}(WHL_{1,\sigma_2})}\}^{\mathcal{O}(WHL_{1,\sigma_2})-3}_{n_i^r n_j^s \in E, n_i^r, n_j^s, n_{\mathcal{O}(WHL_{1,\sigma_2})} \text{are pairwise disjoint.}},$$
$$V \setminus \{n_i\}^{\mathcal{O}(WHL_{1,\sigma_2})-1}, V^{\mathcal{O}(WHL_{1,\sigma_2})}.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum cardinality between all k-number-resolving sets is called k-number-resolving number and it's denoted by

$$\mathcal{N}^1 = \mathcal{O}(WHL_{1,\sigma_2}) - 3.$$

$$\mathcal{N}^{\mathcal{O}(WHL_{1,\sigma_2})-1}(WHL_{1,\sigma_2}) = \mathcal{O}(WHL_{1,\sigma_2}) - 1.$$

$$\mathcal{N}^{\mathcal{O}(WHL_{1,\sigma_2})}(WHL_{1,\sigma_2}) = \mathcal{O}(WHL_{1,\sigma_2}).$$
$$k = 1, \mathcal{O}(WHL_{1,\sigma_2}) - 1, \mathcal{O}(WHL_{1,\sigma_2});$$

and corresponded to k-number-resolving sets are

$$V \setminus \{n_i^r, n_j^s, n_{\mathcal{O}(WHL_{1,\sigma_2})}\}^{\mathcal{O}(WHL_{1,\sigma_2})-3}_{n_i^r n_j^s \in E, n_i^r, n_j^s, n_{\mathcal{O}(WHL_{1,\sigma_2})} \text{are pairwise disjoint.}},$$
$$V \setminus \{n_i\}^{\mathcal{O}(WHL_{1,\sigma_2})-1}, V^{\mathcal{O}(WHL_{1,\sigma_2})}.$$

Thus

$$\mathcal{N}^1 = \mathcal{O}(WHL_{1,\sigma_2}) - 3.$$
$$\mathcal{N}^{\mathcal{O}(WHL_{1,\sigma_2})-1}(WHL_{1,\sigma_2}) = \mathcal{O}(WHL_{1,\sigma_2}) - 1.$$
$$\mathcal{N}^{\mathcal{O}(WHL_{1,\sigma_2})}(WHL_{1,\sigma_2}) = \mathcal{O}(WHL_{1,\sigma_2}).$$
$$k = 1, \mathcal{O}(WHL_{1,\sigma_2}) - 1, \mathcal{O}(WHL_{1,\sigma_2}).$$

□

Proposition 2.29. *Let $NTG : (V, E, \sigma, \mu)$ be a wheel-neutrosophic graph. Then k-number-resolving number isn't equal to resolving number where $k \neq 1$.*

Proposition 2.30. *Let $NTG : (V, E, \sigma, \mu)$ be a wheel-neutrosophic graph with center c. Then*

(i) *the number of k-number-resolving sets is $\mathcal{O}(WHL_{1,\sigma_2}) - 1$ plus $\mathcal{O}(WHL_{1,\sigma_2})$ plus one where $k = \mathcal{O}(WHL_{1,\sigma_2}) - 3$;*

(ii) *the number of k-number-resolving sets is $\mathcal{O}(WHL_{1,\sigma_2})$ plus one where $k = \mathcal{O}(WHL_{1,\sigma_2}) - 1$;*

(iii) *the number of k-number-resolving sets is one where $k = \mathcal{O}(WHL_{1,\sigma_2})$.*

Proposition 2.31. *Let $NTG : (V, E, \sigma, \mu)$ be a wheel-neutrosophic graph with center c. Then*

(i) *the number of k-number-resolving sets corresponded to k-number-resolving number is $\mathcal{O}(WHL_{1,\sigma_2}) - 1$ where $k = \mathcal{O}(WHL_{1,\sigma_2}) - 3$;*

(ii) *the number of k-number-resolving sets corresponded to k-number-resolving number is $\mathcal{O}(WHL_{1,\sigma_2})$ where $k = \mathcal{O}(WHL_{1,\sigma_2}) - 1$;*

(iii) *the number of k-number-resolving sets corresponded to k-number-resolving number is one where $k = \mathcal{O}(WHL_{1,\sigma_2})$.*

Example 2.32. There is one section for clarifications. In Figure (10), a wheel-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows.

(i) For given two neutrosophic vertices, n and n', there is either one path with length one or one path with length two between them;

(ii) in the setting of wheel, a vertex of resolving set corresponded to resolving number resolves as if it doesn't k-number-resolve so as resolving is different from k-number-resolving;

(iii) all minimal k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_4, n_5\}^1, \{n_5, n_2\}^1, \{n_2, n_3\}^1,$$
$$\{n_3, n_4\}^1, \{n_1, n_4, n_5\}^1, \{n_1, n_5, n_2\}^1,$$
$$\{n_1, n_2, n_3\}^1, \{n_1, n_3, n_4\}^1, \{n_1, n_2, n_3, n_4\}^4,$$
$$\{n_1, n_2, n_3, n_5\}^4, \{n_1, n_2, n_4, n_5\}^4, \{n_1, n_3, n_4, n_5\}^4,$$
$$\{n_2, n_3, n_4, n_5\}^4, \{n_1, n_2, n_3, n_4, n_5\}^5.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum cardinality between all k-number-resolving sets is called k-number-resolving number and it's denoted by

$$\mathcal{N}^1 = \mathcal{O}(WHL_{1,\sigma_2}) - 3.$$
$$\mathcal{N}^{\mathcal{O}(WHL_{1,\sigma_2})-1}(WHL_{1,\sigma_2}) = \mathcal{O}(WHL_{1,\sigma_2}) - 1.$$
$$\mathcal{N}^{\mathcal{O}(WHL_{1,\sigma_2})}(WHL_{1,\sigma_2}) = \mathcal{O}(WHL_{1,\sigma_2}).$$
$$k = 1, \mathcal{O}(WHL_{1,\sigma_2}) - 1, \mathcal{O}(WHL_{1,\sigma_2});$$

and corresponded to k-number-resolving sets are

$$\{n_4, n_5\}^1, \{n_5, n_2\}^1, \{n_2, n_3\}^1,$$
$$\{n_3, n_4\}^1, \{n_1, n_4, n_5\}^1, \{n_1, n_5, n_2\}^1,$$
$$\{n_1, n_2, n_3\}^1, \{n_1, n_3, n_4\}^1, \{n_1, n_2, n_3, n_4\}^4,$$
$$\{n_1, n_2, n_3, n_5\}^4, \{n_1, n_2, n_4, n_5\}^4, \{n_1, n_3, n_4, n_5\}^4,$$
$$\{n_2, n_3, n_4, n_5\}^4, \{n_1, n_2, n_3, n_4, n_5\}^5;$$

(iv) there are fourteen k-number-resolving sets

$$\{n_4, n_5\}^1, \{n_5, n_2\}^1, \{n_2, n_3\}^1,$$
$$\{n_3, n_4\}^1, \{n_1, n_4, n_5\}^1, \{n_1, n_5, n_2\}^1,$$
$$\{n_1, n_2, n_3\}^1, \{n_1, n_3, n_4\}^1, \{n_1, n_2, n_3, n_4\}^{1,2,3,4},$$
$$\{n_1, n_2, n_3, n_5\}^{1,2,3,4}, \{n_1, n_2, n_4, n_5\}^{1,2,3,4}, \{n_1, n_3, n_4, n_5\}^{1,2,3,4},$$
$$\{n_2, n_3, n_4, n_5\}^{1,2,3,4}, \{n_1, n_2, n_3, n_4, n_5\}^{1,2,3,4,5},$$

so as it's possible to have one of them as a set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is characteristic;

(v) there are fourteen k-number-resolving sets

$$\{n_4, n_5\}^1, \{n_5, n_2\}^1, \{n_2, n_3\}^1,$$
$$\{n_3, n_4\}^1, \{n_1, n_4, n_5\}^1, \{n_1, n_5, n_2\}^1,$$
$$\{n_1, n_2, n_3\}^1, \{n_1, n_3, n_4\}^1, \{n_1, n_2, n_3, n_4\}^4,$$
$$\{n_1, n_2, n_3, n_5\}^4, \{n_1, n_2, n_4, n_5\}^4, \{n_1, n_3, n_4, n_5\}^4,$$
$$\{n_2, n_3, n_4, n_5\}^4, \{n_1, n_2, n_3, n_4, n_5\}^5,$$

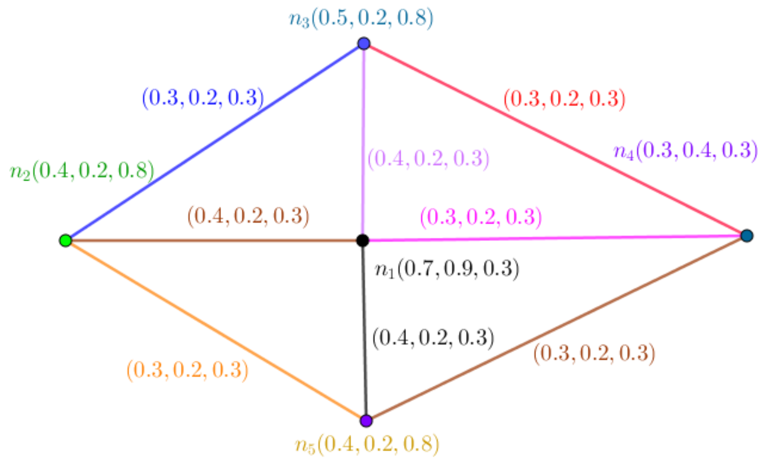

Figure 10. A Neutrosophic Graph in the Viewpoint of its k-number-resolving number and its neutrosophic k-number-resolving number.

corresponded to k-number-resolving number as if there's one k-number-resolving set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is the determiner;

(vi) all k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_4, n_5\}^1, \{n_5, n_2\}^1, \{n_2, n_3\}^1,$$
$$\{n_3, n_4\}^1, \{n_1, n_4, n_5\}^1, \{n_1, n_5, n_2\}^1,$$
$$\{n_1, n_2, n_3\}^1, \{n_1, n_3, n_4\}^1, \{n_1, n_2, n_3, n_4\}^4,$$
$$\{n_1, n_2, n_3, n_5\}^4, \{n_1, n_2, n_4, n_5\}^4, \{n_1, n_3, n_4, n_5\}^4,$$
$$\{n_2, n_3, n_4, n_5\}^4, \{n_1, n_2, n_3, n_4, n_5\}^5.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum neutrosophic cardinality between all k-number-resolving sets is called neutrosophic k-number-resolving number and it's denoted by

$$\mathcal{N}_n^1 = 2.4.$$

$$\mathcal{N}_n^{\mathcal{O}(WHL_{1,\sigma_2})-1}(WHL_{1,\sigma_2}) = 5.3.$$

$$\mathcal{N}_n^{\mathcal{O}(WHL_{1,\sigma_2})}(WHL_{1,\sigma_2}) = 7.2.$$

$$k = 1, \mathcal{O}(WHL_{1,\sigma_2}) - 1, \mathcal{O}(WHL_{1,\sigma_2});$$

and corresponded to k-number-resolving sets are

$$\{n_4, n_5\}^1, \{n_2, n_3, n_4, n_5\}^4, \{n_1, n_2, n_3, n_4, n_5\}^5.$$

3 Setting of neutrosophic k-number-resolving number

In this section, I provide some results in the setting of neutrosophic k-number-resolving number. Some classes of neutrosophic graphs are chosen. Complete-neutrosophic graph, path-neutrosophic graph, cycle-neutrosophic graph, star-neutrosophic graph, bipartite-neutrosophic graph, t-partite-neutrosophic graph, and wheel-neutrosophic graph, are both of cases of study and classes which the results are about them.

Proposition 3.1. *Let $NTG : (V, E, \sigma, \mu)$ be a complete-neutrosophic graph. Then*

$$\mathcal{N}_n^k(CMT_\sigma) = \min_{|S|=\mathcal{O}(CMT_\sigma)-1} \sum_{i=1}^{3} \sigma_i(x)_{x\in S},\ k = \mathcal{O}(CMT_\sigma) - 1.$$

Thus,

$$\mathcal{N}_n^{\mathcal{O}(CMT_\sigma)-1}(CMT_\sigma) = \min_{|S|=\mathcal{O}(CMT_\sigma)-1} \sum_{i=1}^{3} \sigma_i(x)_{x\in S},\ k = \mathcal{O}(CMT_\sigma) - 1.$$

Proof. Suppose $CMT_\sigma : (V, E, \sigma, \mu)$ is a complete-neutrosophic graph. By $CMT_\sigma : (V, E, \sigma, \mu)$ is a complete-neutrosophic graph, all vertices are connected to each other. So there's one edge between two vertices. In the setting of complete, a vertex of resolving set corresponded to resolving number resolves as if it doesn't k-number-resolve so as resolving is different from k-number-resolving. Resolving number and k-number-resolving number are the same if $k = 1$. All minimal k-number-resolving sets corresponded to k-number-resolving number are

$$\begin{aligned}
&\{n_2, n_3, n_4, \ldots, n_{\mathcal{O}(CMT_\sigma)-2}, n_{\mathcal{O}(CMT_\sigma)-1}, n_{\mathcal{O}(CMT_\sigma)}\},\\
&\{n_1, n_3, n_4, \ldots, n_{\mathcal{O}(CMT_\sigma)-2}, n_{\mathcal{O}(CMT_\sigma)-1}, n_{\mathcal{O}(CMT_\sigma)}\},\\
&\{n_1, n_2, n_4, \ldots, n_{\mathcal{O}(CMT_\sigma)-2}, n_{\mathcal{O}(CMT_\sigma)-1}, n_{\mathcal{O}(CMT_\sigma)}\},\\
&\ldots\\
&\{n_1, n_2, n_3, \ldots, n_{\mathcal{O}(CMT_\sigma)-3}, n_{\mathcal{O}(CMT_\sigma)-1}, n_{\mathcal{O}(CMT_\sigma)}\},\\
&\{n_1, n_2, n_3, \ldots, n_{\mathcal{O}(CMT_\sigma)-3}, n_{\mathcal{O}(CMT_\sigma)-2}, n_{\mathcal{O}(CMT_\sigma)}\},\\
&\{n_1, n_2, n_3, \ldots, n_{\mathcal{O}(CMT_\sigma)-3}, n_{\mathcal{O}(CMT_\sigma)-2}, n_{\mathcal{O}(CMT_\sigma)-1}\}.
\end{aligned}$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum neutrosophic cardinality between all k-number-resolving sets is called neutrosophic k-number-resolving number and it's denoted by

$$\mathcal{N}_n^k(CMT_\sigma) = \min_{|S|=\mathcal{O}(CMT_\sigma)-1} \sum_{i=1}^{3} \sigma_i(x)_{x\in S},\ k = \mathcal{O}(CMT_\sigma) - 1.$$

Thus,

$$\mathcal{N}_n^{\mathcal{O}(CMT_\sigma)-1}(CMT_\sigma) = \min_{|S|=\mathcal{O}(CMT_\sigma)-1} \sum_{i=1}^{3} \sigma_i(x)_{x\in S},\ k = \mathcal{O}(CMT_\sigma) - 1;$$

and corresponded to k-number-resolving sets are

$$\begin{aligned}&\{n_2, n_3, n_4, \ldots, n_{\mathcal{O}(CMT_\sigma)-2}, n_{\mathcal{O}(CMT_\sigma)-1}, n_{\mathcal{O}(CMT_\sigma)}\},\\&\{n_1, n_3, n_4, \ldots, n_{\mathcal{O}(CMT_\sigma)-2}, n_{\mathcal{O}(CMT_\sigma)-1}, n_{\mathcal{O}(CMT_\sigma)}\},\\&\{n_1, n_2, n_4, \ldots, n_{\mathcal{O}(CMT_\sigma)-2}, n_{\mathcal{O}(CMT_\sigma)-1}, n_{\mathcal{O}(CMT_\sigma)}\},\\&\ldots\\&\{n_1, n_2, n_3, \ldots, n_{\mathcal{O}(CMT_\sigma)-3}, n_{\mathcal{O}(CMT_\sigma)-1}, n_{\mathcal{O}(CMT_\sigma)}\},\\&\{n_1, n_2, n_3, \ldots, n_{\mathcal{O}(CMT_\sigma)-3}, n_{\mathcal{O}(CMT_\sigma)-2}, n_{\mathcal{O}(CMT_\sigma)}\},\\&\{n_1, n_2, n_3, \ldots, n_{\mathcal{O}(CMT_\sigma)-3}, n_{\mathcal{O}(CMT_\sigma)-2}, n_{\mathcal{O}(CMT_\sigma)-1}\}.\end{aligned}$$

$$\mathcal{N}^k(CMT_\sigma) = k,\ k = \mathcal{O}(CMT_\sigma) - 1.$$

Thus,

$$\mathcal{N}_n^k(CMT_\sigma) = \min_{|S|=\mathcal{O}(CMT_\sigma)-1} \sum_{i=1}^{3} \sigma_i(x)_{x\in S},\ k = \mathcal{O}(CMT_\sigma) - 1.$$

Thus,

$$\mathcal{N}_n^{\mathcal{O}(CMT_\sigma)-1}(CMT_\sigma) = \min_{|S|=\mathcal{O}(CMT_\sigma)-1} \sum_{i=1}^{3} \sigma_i(x)_{x\in S},\ k = \mathcal{O}(CMT_\sigma) - 1.$$

□

Proposition 3.2. *Let $NTG : (V, E, \sigma, \mu)$ be a complete-neutrosophic graph. Then k-number-resolving number isn't equal to resolving number where $k > 1$.*

Proposition 3.3. *Let $NTG : (V, E, \sigma, \mu)$ be a complete-neutrosophic graph. Then the number of k-number-resolving sets corresponded to k-number-resolving number is $\mathcal{O}(CMT_\sigma) - 1$.*

Proposition 3.4. *Let $NTG : (V, E, \sigma, \mu)$ be a complete-neutrosophic graph. Then the number of k-number-resolving sets is $\mathcal{O}(CMT_\sigma)$.*

The clarifications about results are in progress as follows. A complete-neutrosophic graph is related to previous result and it's studied to apply the definitions on it. To make it more clear, next part gives one special case to apply definitions and results on it. Some items are devised to make more sense about new notions. A complete-neutrosophic graph is related to previous result and it's studied to apply the definitions on it, too.

Example 3.5. In Figure (11), a complete-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows.

(*i*) For given neutrosophic vertex, s, there's an edge with other vertices;

(*ii*) in the setting of complete, a vertex of resolving set corresponded to resolving number resolves as if it doesn't k-number-resolve so as resolving is different from k-number-resolving. Resolving number and k-number-resolving number are the same if $k = 1$;

(*iii*) all minimal k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_1, n_2, n_3\}^3, \{n_1, n_2, n_4\}^3, \{n_1, n_3, n_4\}^3.$$

For given vertices n and n' if

$$d(s_1,n) \neq d(s_1,n'), d(s_2,n) \neq d(s_2,n'), \ldots, d(s_k,n) \neq d(s_k,n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum cardinality between all k-number-resolving sets is called k-number-resolving number and it's denoted by $\mathcal{N}^k(CMT_\sigma) = k,\ k = \mathcal{O}(CMT_\sigma) - 1$; and corresponded to k-number-resolving sets are

$$\{n_1,n_2,n_3\}^3, \{n_1,n_2,n_4\}^3, \{n_1,n_3,n_4\}^3;$$

(iv) there are four k-number-resolving sets

$$\{n_1,n_2,n_3\}^3, \{n_1,n_2,n_4\}^3, \{n_1,n_3,n_4\}^3,$$
$$\{n_1,n_2,n_3,n_4\}^4,$$

so as it's possible to have one of them as a set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is characteristic;

(v) there are three k-number-resolving sets

$$\{n_1,n_2,n_3\}^3, \{n_1,n_2,n_4\}^3, \{n_1,n_3,n_4\}^3,$$

corresponded to k-number-resolving number as if there's one k-number-resolving set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is the determiner;

(vi) all k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_1,n_2,n_3\}^3, \{n_1,n_2,n_4\}^3, \{n_1,n_3,n_4\}^3.$$

For given vertices n and n' if

$$d(s_1,n) \neq d(s_1,n'), d(s_2,n) \neq d(s_2,n'), \ldots, d(s_k,n) \neq d(s_k,n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum neutrosophic cardinality between all k-number-resolving sets is called neutrosophic k-number-resolving number and it's denoted by $\mathcal{N}_n^k(CMT_\sigma) = 3.9,\ k = \mathcal{O}(CMT_\sigma) - 1$; and corresponded to k-number-resolving sets are

$$\{n_1,n_3,n_4\}^3.$$

Another class of neutrosophic graphs is addressed to path-neutrosophic graph.

Proposition 3.6. *Let $NTG : (V, E, \sigma, \mu)$ be a path-neutrosophic graph. Then*

$$\mathcal{N}_n^k(PTH) = \min_{|S|=k} \sum_{i=1}^{3} \sigma_i(x)_{x \in S},\ k = 1, 2, 3, \ldots, \mathcal{O}(PTH).$$

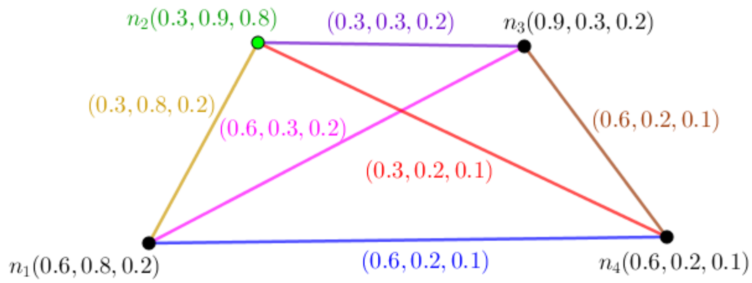

Figure 11. A Neutrosophic Graph in the Viewpoint of its k-number-resolving number and its neutrosophic k-number-resolving number.

Proof. Suppose $PTH : (V, E, \sigma, \mu)$ is a path-neutrosophic graph. Let $n_1, n_2, \ldots, n_{\mathcal{O}(PTH)}$ be a path-neutrosophic graph. For given two vertices, x and y, there's one path from x to y. In the setting of path, a vertex of resolving set corresponded to resolving number resolves as if it doesn't k-number-resolve in the setting of resolving. All minimal k-number-resolving sets corresponded to k-number-resolving number are

$$\begin{aligned}&\{n_1\}^1, \{n_{\mathcal{O}(PTH)}\}^1, \{n_i, n_j\}^2,\\&\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5,\\&\ldots,\\&\{n_i, n_j, n_k, n_r, n_s, \ldots, n_t\}^{\mathcal{O}(PTH)}.\end{aligned}$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum neutrosophic cardinality between all k-number-resolving sets is called neutrosophic k-number-resolving number and it's denoted by

$$\mathcal{N}_n^k(PTH) = \min_{|S|=k} \sum_{i=1}^{3} \sigma_i(x)_{x \in S},\ k = 1, 2, 3, \ldots, \mathcal{O}(PTH);$$

and corresponded to k-number-resolving sets are

$$\begin{aligned}&\{n_1\}^1, \{n_{\mathcal{O}(PTH)}\}^1, \{n_i, n_j\}^2,\\&\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5,\\&\ldots,\\&\{n_i, n_j, n_k, n_r, n_s, \ldots, n_t\}^{\mathcal{O}(PTH)}.\end{aligned}$$

Thus

$$\mathcal{N}_n^k(PTH) = \min_{|S|=k} \sum_{i=1}^{3} \sigma_i(x)_{x \in S},\ k = 1, 2, 3, \ldots, \mathcal{O}(PTH).$$

□

Proposition 3.7. *Let $NTG : (V, E, \sigma, \mu)$ be a path-neutrosophic graph. If k isn't equal to one, then all leaves belong k-number-resolving sets corresponded to k-number-resolving number.*

Proposition 3.8. *Let $NTG : (V, E, \sigma, \mu)$ be a path-neutrosophic graph. If at least one leaf doesn't belong k-number-resolving sets corresponded to k-number-resolving number, then k is equal to two where $k = 1$.*

Proposition 3.9. *Let $NTG : (V, E, \sigma, \mu)$ be a path-neutrosophic graph. If at least one leaf doesn't belong k-number-resolving sets corresponded to k-number-resolving number, then k is equal to $\mathcal{O}(PTH)$ choose k where $k \neq 1$.*

Example 3.10. There are two sections for clarifications.

(a) In Figure (12), an odd-path-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows.

(i) For given neutrosophic vertex, s, there's only one path with other vertices;

(ii) in the setting of path, a vertex of resolving set corresponded to resolving number resolves as if it doesn't k-number-resolve in the setting of resolving;

(iii) all minimal k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_1\}^1, \{n_5\}^1, \{n_i, n_j\}^2,$$
$$\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum cardinality between all k-number-resolving sets is called k-number-resolving number and it's denoted by $\mathcal{N}^k(PTH) = k,\ k = 1, 2, 3, \ldots, \mathcal{O}(PTH)$; and corresponded to k-number-resolving sets are

$$\{n_1\}^1, \{n_5\}^1, \{n_i, n_j\}^2,$$
$$\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5;$$

(iv) there are some k-number-resolving sets

$$\{n_1\}^1, \{n_5\}^1, \{n_i, n_j\}^2,$$
$$\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5,$$

so as it's possible to have one of them as a set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is characteristic;

(v) there are some k-number-resolving sets

$$\{n_1\}^1, \{n_5\}^1, \{n_i, n_j\}^2,$$
$$\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5,$$

corresponded to k-number-resolving number as if there's one k-number-resolving set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is the determiner;

(vi) all k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_1\}^1, \{n_5\}^1, \{n_i, n_j\}^2,$$
$$\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum neutrosophic cardinality between all k-number-resolving sets is called neutrosophic k-number-resolving number and it's denoted by $\mathcal{N}_n^1(PTH) = 1.2, \mathcal{N}_n^2(PTH) = 1.9, \mathcal{N}_n^3(PTH) = 3.1, \mathcal{N}_n^4(PTH) = 4.5, \mathcal{N}_n^5(PTH) = 6.3$; and corresponded to k-number-resolving sets are

$$\{n_5\}^1, \{n_3, n_4\}^2, \{n_3, n_5\}^2,$$
$$\{n_3, n_4, n_5\}^3, \{n_3, n_4, n_5, n_1\}^4, \{n_1, n_2, n_3, n_4, n_5\}^5.$$

(b) In Figure (13), an even-path-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows.

(i) For given neutrosophic vertex, s, there's only one path with other vertices;

(ii) in the setting of path, a vertex of resolving set corresponded to resolving number resolves as if it doesn't k-number-resolve in the setting of resolving;

(iii) all minimal k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_1\}^1, \{n_6\}^1, \{n_i, n_j\}^2,$$
$$\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5,$$
$$\{n_i, n_j, n_k, n_r, n_s, n_t\}^6.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum cardinality between all k-number-resolving sets is called k-number-resolving number and it's denoted by $\mathcal{N}^k(PTH) = k,\ k = 1, 2, 3, \ldots, \mathcal{O}(PTH)$; and corresponded to k-number-resolving sets are

$$\{n_1\}^1, \{n_6\}^1, \{n_i, n_j\}^2,$$
$$\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5,$$
$$\{n_i, n_j, n_k, n_r, n_s, n_t\}^6;$$

(*iv*) there are some k-number-resolving sets

$$\{n_1\}^1, \{n_6\}^1, \{n_i, n_j\}^2,$$
$$\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5,$$
$$\{n_i, n_j, n_k, n_r, n_s, n_t\}^6,$$

so as it's possible to have one of them as a set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is characteristic;

(*v*) there are some k-number-resolving sets

$$\{n_1\}^1, \{n_6\}^1, \{n_i, n_j\}^2,$$
$$\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5,$$
$$\{n_i, n_j, n_k, n_r, n_s, n_t\}^6,$$

corresponded to k-number-resolving number as if there's one k-number-resolving set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is the determiner;

(*vi*) all k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_1\}^1, \{n_6\}^1, \{n_i, n_j\}^2,$$
$$\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5,$$
$$\{n_i, n_j, n_k, n_r, n_s, n_t\}^6.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum neutrosophic cardinality between all k-number-resolving sets is called neutrosophic k-number-resolving number and it's denoted by $\mathcal{N}_n^1(PTH) = 1.9, \mathcal{N}_n^2(PTH) = 1.8, \mathcal{N}_n^3(PTH) = 3.3, \mathcal{N}_n^4(PTH) = 3.9, \mathcal{N}_n^5(PTH) = 5.1, \mathcal{N}_n^6(PTH) = 7.8$; and corresponded to k-number-resolving sets are

$$\{n_6\}^1, \{n_3, n_2\}^2, \{n_3, n_2, n_4\}^3,$$
$$\{n_3, n_2, n_4, n_6\}^4, \{n_3, n_2, n_4, n_6, n_1\}^5, \{n_3, n_2, n_4, n_6, n_1, n_5\}^6.$$

Proposition 3.11. *Let $NTG : (V, E, \sigma, \mu)$ be a cycle-neutrosophic graph where $\mathcal{O}(CYC) \geq 3$. Then*

$$\mathcal{N}_n^k(CYC) = \min_{|S|=k} \sum_{i=1}^{3} \sigma_i(x)_{x \in S}, \;\; k = 2, 3, \ldots, \mathcal{O}(CYC).$$

Proof. Suppose $CYC : (V, E, \sigma, \mu)$ is a cycle-neutrosophic graph. For given two vertices, x and y, there are only two paths with distinct edges from x to y. Let

$$n_1, n_2, \cdots, n_{\mathcal{O}(CYC)-1}, n_{\mathcal{O}(CYC)}, n_1$$

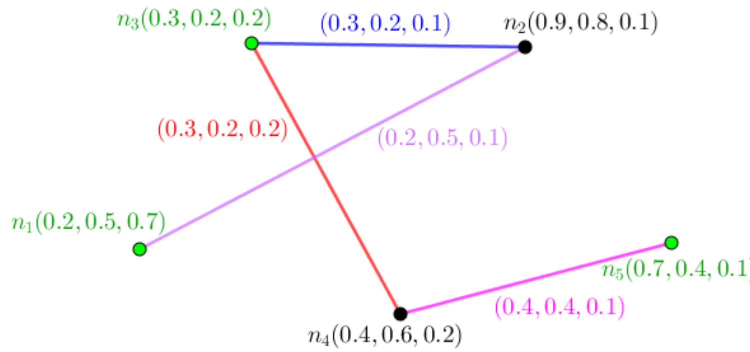

Figure 12. A Neutrosophic Graph in the Viewpoint of its k-number-resolving number and its neutrosophic k-number-resolving number.

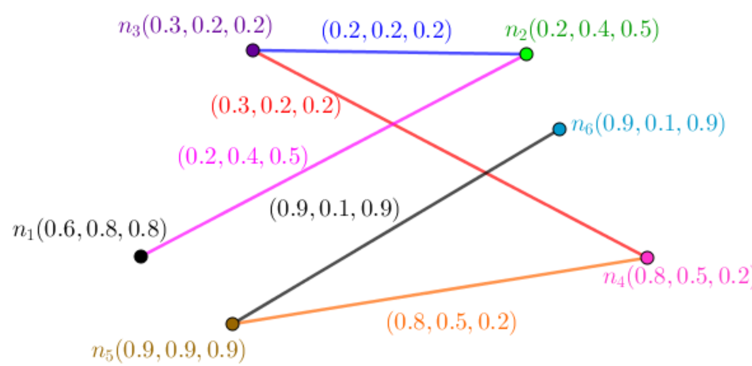

Figure 13. A Neutrosophic Graph in the Viewpoint of its k-number-resolving number and its neutrosophic k-number-resolving number.

be a cycle-neutrosophic graph $CYC : (V, E, \sigma, \mu)$. In the setting of cycle, a vertex of resolving set corresponded to resolving number resolves as if it doesn't k-number-resolve in the setting of resolving. In the setting of cycle, always $k > 1$. Antipodal vertices play roles when $k = 2$ such that they're excluded from k-number-resolving sets but they play no role when $k \neq 2$. All minimal k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_i, n_j\}^2_{\text{excluding antipodal vertices}},$$
$$\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5,$$
$$\{n_i, n_j, n_k, n_r, n_s, n_t\}^6.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum neutrosophic cardinality between all k-number-resolving sets is called neutrosophic k-number-resolving number and it's denoted by

$$\mathcal{N}_n^k(CYC) = \min_{|S|=k} \sum_{i=1}^{3} \sigma_i(x)_{x \in S},\ k = 2, 3, \ldots, \mathcal{O}(CYC);$$

and corresponded to k-number-resolving sets are

$$\{n_i, n_j\}^2_{\text{excluding antipodal vertices}},$$
$$\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5,$$
$$\{n_i, n_j, n_k, n_r, n_s, n_t\}^6;$$

Thus

$$\mathcal{N}_n^k(CYC) = \min_{|S|=k} \sum_{i=1}^{3} \sigma_i(x)_{x \in S},\ k = 2, 3, \ldots, \mathcal{O}(CYC).$$

□

The clarifications about results are in progress as follows. An odd-cycle-neutrosophic graph is related to previous result and it's studied to apply the definitions on it. To make it more clear, next part gives one special case to apply definitions and results on it. Some items are devised to make more sense about new notions. An even-cycle-neutrosophic graph is related to previous result and it's studied to apply the definitions on it, too.

Example 3.12. There are two sections for clarifications.

(a) In Figure (14), an even-cycle-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows.

  (i) For given neutrosophic vertex, s, there's only one path with other vertices;

  (ii) in the setting of cycle, a vertex of resolving set corresponded to resolving number resolves as if it doesn't k-number-resolve in the setting of resolving. In the setting of cycle, always $k > 1$. Antipodal vertices play roles when $k = 2$ such that they're excluded from k-number-resolving sets but they play no role when $k \neq 2$;

(iii) all minimal k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_i, n_j\}^2_{\text{excluding antipodal vertices}},$$
$$\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5,$$
$$\{n_i, n_j, n_k, n_r, n_s, n_t\}^6.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum cardinality between all k-number-resolving sets is called k-number-resolving number and it's denoted by $\mathcal{N}^k(CYC) = k,\ k = 2, 3, \ldots, \mathcal{O}(CYC)$; and corresponded to k-number-resolving sets are

$$\{n_i, n_j\}^2_{\text{excluding antipodal vertices}},$$
$$\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5,$$
$$\{n_i, n_j, n_k, n_r, n_s, n_t\}^6;$$

(iv) there are some k-number-resolving sets

$$\{n_i, n_j\}^2_{\text{excluding antipodal vertices}},$$
$$\{n_i, n_j, n_k\}^{2,3}, \{n_i, n_j, n_k, n_r\}^{2,3,4}, \{n_i, n_j, n_k, n_r, n_s\}^{2,3,4,5},$$
$$\{n_i, n_j, n_k, n_r, n_s, n_t\}^{2,3,4,5,6},$$

so as it's possible to have one of them as a set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is characteristic;

(v) there are some k-number-resolving sets

$$\{n_i, n_j\}^2_{\text{excluding antipodal vertices}},$$
$$\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5,$$
$$\{n_i, n_j, n_k, n_r, n_s, n_t\}^6,$$

corresponded to k-number-resolving number as if there's one k-number-resolving set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is the determiner;

(vi) all k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_i, n_j\}^2_{\text{excluding antipodal vertices}},$$
$$\{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4, \{n_i, n_j, n_k, n_r, n_s\}^5,$$
$$\{n_i, n_j, n_k, n_r, n_s, n_t\}^6.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum neutrosophic cardinality between all k-number-resolving sets is called neutrosophic k-number-resolving number and it's denoted by $\mathcal{N}_n^2(CYC) = 1.3, \mathcal{N}_n^3(CYC) = 2.6, \mathcal{N}_n^4(CYC) = 4.1, \mathcal{N}_n^5(CYC) = 6.0, \mathcal{N}_n^6(CYC) = 7.5$; and corresponded to k-number-resolving sets are

$$\{n_1, n_5\}^2,$$
$$\{n_1, n_5, n_4\}^3, \{n_1, n_5, n_4, n_6\}^4, \{n_1, n_5, n_4, n_6, n_3\}^5,$$
$$\{n_1, n_5, n_4, n_6, n_3, n_2\}^6.$$

(b) In Figure (15), an odd-cycle-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows.

(i) For given neutrosophic vertex, s, there's only one path with other vertices;

(ii) in the setting of cycle, a vertex of resolving set corresponded to resolving number resolves as if it doesn't k-number-resolve in the setting of resolving. In the setting of cycle, always $k > 1$;

(iii) all minimal k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_i, n_j\}^2, \{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4,$$
$$\{n_i, n_j, n_k, n_r, n_s\}^5.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum cardinality between all k-number-resolving sets is called k-number-resolving number and it's denoted by $\mathcal{N}^k(CYC) = k,\ k = 2, 3, \ldots, \mathcal{O}(CYC)$; and corresponded to k-number-resolving sets are

$$\{n_i, n_j\}^2, \{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4,$$
$$\{n_i, n_j, n_k, n_r, n_s\}^5;$$

(iv) there are some k-number-resolving sets

$$\{n_i, n_j\}^2, \{n_i, n_j, n_k\}^{2,3}, \{n_i, n_j, n_k, n_r\}^{2,3,4},$$
$$\{n_i, n_j, n_k, n_r, n_s\}^{2,3,4,5},$$

so as it's possible to have one of them as a set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is characteristic;

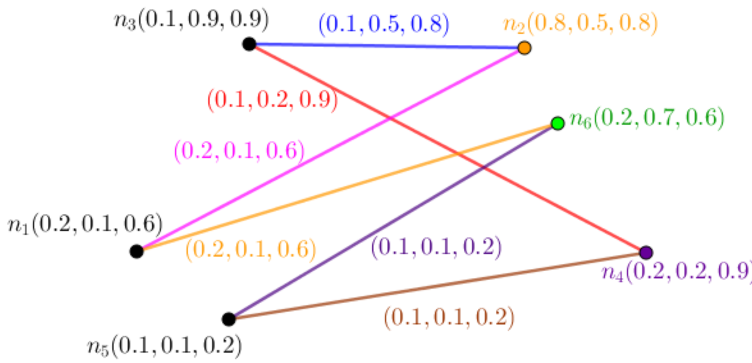

Figure 14. A Neutrosophic Graph in the Viewpoint of its k-number-resolving number and its neutrosophic k-number-resolving number.

(v) there are some k-number-resolving sets

$$\{n_i, n_j\}^2, \{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4,$$
$$\{n_i, n_j, n_k, n_r, n_s\}^5,$$

corresponded to k-number-resolving number as if there's one k-number-resolving set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is the determiner;

(vi) all k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_i, n_j\}^2, \{n_i, n_j, n_k\}^3, \{n_i, n_j, n_k, n_r\}^4,$$
$$\{n_i, n_j, n_k, n_r, n_s\}^5.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum neutrosophic cardinality between all k-number-resolving sets is called neutrosophic k-number-resolving number and it's denoted by
$\mathcal{N}_n^2(CYC) = 2.7, \mathcal{N}_n^3(CYC) = 4.2, \mathcal{N}_n^4(CYC) = 6.2, \mathcal{N}_n^5(CYC) = 8.5$; and corresponded to k-number-resolving sets are

$$\{n_1, n_5\}^2, \{n_1, n_5, n_2\}^3, \{n_1, n_5, n_2, n_4\}^4,$$
$$\{n_1, n_5, n_2, n_4, n_3\}^5.$$

Proposition 3.13. *Let $NTG : (V, E, \sigma, \mu)$ be a star-neutrosophic graph with center c. Then*

$$\mathcal{N}_n^{\mathcal{O}(STR_{1,\sigma_2})-2}(STR_{1,\sigma_2}) = \min_{S = V \setminus \{n_{\mathcal{O}(STR_{1,\sigma_2})}, n_i\}_{n_i \neq n_{\mathcal{O}(STR_{1,\sigma_2})}}} \sum_{i=1}^{3} \sigma_i(x)_{x \in S}.$$

$$\mathcal{N}_n^{\mathcal{O}(STR_{1,\sigma_2})-1}(STR_{1,\sigma_2}) = \min_{|S| = \mathcal{O}(STR_{1,\sigma_2})-1} \sum_{i=1}^{3} \sigma_i(x)_{x \in S}.$$

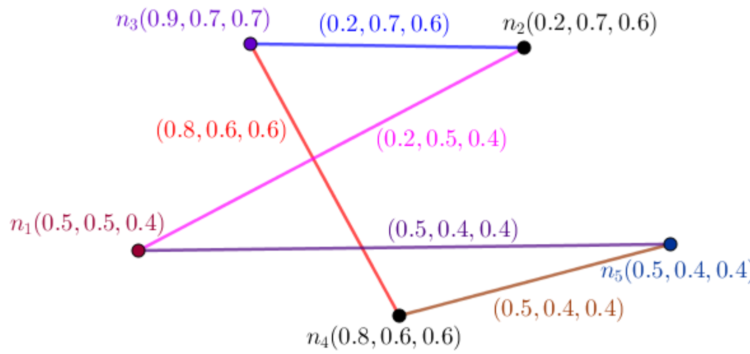

Figure 15. A Neutrosophic Graph in the Viewpoint of its k-number-resolving number and its neutrosophic k-number-resolving number.

$$\mathcal{N}_n^{\mathcal{O}(STR_{1,\sigma_2})}(STR_{1,\sigma_2}) = \mathcal{O}_n(STR_{1,\sigma_2}).$$
$$k = \mathcal{O}(STR_{1,\sigma_2}) - 2, \mathcal{O}(STR_{1,\sigma_2}) - 1, \mathcal{O}(STR_{1,\sigma_2}).$$

Proof. Suppose $STR_{1,\sigma_2} : (V, E, \sigma, \mu)$ is a star-neutrosophic graph. An edge always has center, c, as one of its endpoints where $n_{\mathcal{O}(STR_{1,\sigma_2})} = c$. All paths have one as their lengths, forever. In the setting of star, a vertex of resolving set corresponded to resolving number resolves as if it doesn't k-number-resolve in the setting of resolving. All minimal k-number-resolving sets corresponded to k-number-resolving number are

$$V \setminus \{n_{\mathcal{O}(STR_{1,\sigma_2})}, n_i\}_{n_i \neq n_{\mathcal{O}(STR_{1,\sigma_2})}}^{\mathcal{O}(STR_{1,\sigma_2})-2}, V \setminus \{n_i\}^{\mathcal{O}(STR_{1,\sigma_2})-1}, V^{\mathcal{O}(STR_{1,\sigma_2})}.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum neutrosophic cardinality between all k-number-resolving sets is called neutrosophic k-number-resolving number and it's denoted by

$$\mathcal{N}_n^{\mathcal{O}(STR_{1,\sigma_2})-2}(STR_{1,\sigma_2}) = \min_{S = V \setminus \{n_{\mathcal{O}(STR_{1,\sigma_2})}, n_i\}_{n_i \neq n_{\mathcal{O}(STR_{1,\sigma_2})}}} \sum_{i=1}^{3} \sigma_i(x)_{x \in S}.$$

$$\mathcal{N}_n^{\mathcal{O}(STR_{1,\sigma_2})-1}(STR_{1,\sigma_2}) = \min_{|S| = \mathcal{O}(STR_{1,\sigma_2})-1} \sum_{i=1}^{3} \sigma_i(x)_{x \in S}.$$
$$\mathcal{N}_n^{\mathcal{O}(STR_{1,\sigma_2})}(STR_{1,\sigma_2}) = \mathcal{O}_n(STR_{1,\sigma_2}).$$
$$k = \mathcal{O}(STR_{1,\sigma_2}) - 2, \mathcal{O}(STR_{1,\sigma_2}) - 1, \mathcal{O}(STR_{1,\sigma_2});$$

and corresponded to k-number-resolving sets are

$$V \setminus \{n_{\mathcal{O}(STR_{1,\sigma_2})}, n_i\}_{n_i \neq n_{\mathcal{O}(STR_{1,\sigma_2})}}^{\mathcal{O}(STR_{1,\sigma_2})-2}, V \setminus \{n_i\}^{\mathcal{O}(STR_{1,\sigma_2})-1}, V^{\mathcal{O}(STR_{1,\sigma_2})}.$$

Thus

$$\mathcal{N}_n^{\mathcal{O}(STR_{1,\sigma_2})-2}(STR_{1,\sigma_2}) = \min_{S = V \setminus \{n_{\mathcal{O}(STR_{1,\sigma_2})}, n_i\}_{n_i \neq n_{\mathcal{O}(STR_{1,\sigma_2})}}} \sum_{i=1}^{3} \sigma_i(x)_{x \in S}.$$

$$\mathcal{N}_n^{\mathcal{O}(STR_{1,\sigma_2})-1}(STR_{1,\sigma_2}) = \min_{|S|=\mathcal{O}(STR_{1,\sigma_2})-1} \sum_{i=1}^{3} \sigma_i(x)_{x\in S}.$$

$$\mathcal{N}_n^{\mathcal{O}(STR_{1,\sigma_2})}(STR_{1,\sigma_2}) = \mathcal{O}_n(STR_{1,\sigma_2}).$$

$$k = \mathcal{O}(STR_{1,\sigma_2}) - 2, \mathcal{O}(STR_{1,\sigma_2}) - 1, \mathcal{O}(STR_{1,\sigma_2}).$$

□

Proposition 3.14. *Let $NTG : (V, E, \sigma, \mu)$ be a star-neutrosophic graph. Then k-number-resolving number isn't equal to resolving number where $k \neq 1$.*

Proposition 3.15. *Let $NTG : (V, E, \sigma, \mu)$ be a star-neutrosophic graph with center c. Then*

(i) *the number of k-number-resolving sets is $\mathcal{O}(STR_{1,\sigma_2})$ choose $\mathcal{O}(STR_{1,\sigma_2}) - 2$ plus $\mathcal{O}(STR_{1,\sigma_2})$ plus one where $k = \mathcal{O}(STR_{1,\sigma_2}) - 2$;*

(ii) *the number of k-number-resolving sets is $\mathcal{O}(STR_{1,\sigma_2})$ plus one where $k = \mathcal{O}(STR_{1,\sigma_2}) - 1$;*

(iii) *the number of k-number-resolving sets is one where $k = \mathcal{O}(STR_{1,\sigma_2})$.*

Proposition 3.16. *Let $NTG : (V, E, \sigma, \mu)$ be a star-neutrosophic graph with center c. Then*

(i) *the number of k-number-resolving sets corresponded to k-number-resolving number is $\mathcal{O}(STR_{1,\sigma_2})$ choose $\mathcal{O}(STR_{1,\sigma_2}) - 2$ where $k = \mathcal{O}(STR_{1,\sigma_2}) - 2$;*

(ii) *the number of k-number-resolving sets corresponded to k-number-resolving number is $\mathcal{O}(STR_{1,\sigma_2})$ where $k = \mathcal{O}(STR_{1,\sigma_2}) - 1$;*

(iii) *the number of k-number-resolving sets corresponded to k-number-resolving number is one where $k = \mathcal{O}(STR_{1,\sigma_2})$.*

The clarifications about results are in progress as follows. A star-neutrosophic graph is related to previous result and it's studied to apply the definitions on it. To make it more clear, next part gives one special case to apply definitions and results on it. Some items are devised to make more sense about new notions. A star-neutrosophic graph is related to previous result and it's studied to apply the definitions on it, too.

Example 3.17. There is one section for clarifications. In Figure (16), a star-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows.

(i) For given two neutrosophic vertices, s and n_1, there's only one path, precisely one edge between them and there's no path despite them;

(ii) in the setting of star, a vertex of resolving set corresponded to resolving number resolves as if it doesn't k-number-resolve in the setting of resolving;

(iii) all minimal k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_2, n_3, n_4\}^3, \{n_2, n_3, n_5\}^3, \{n_2, n_4, n_5\}^3,$$
$$\{n_3, n_4, n_5\}^3, \{n_1, n_2, n_3, n_4\}^4, \{n_1, n_2, n_3, n_5\}^4,$$
$$\{n_1, n_2, n_4, n_5\}^4, \{n_1, n_3, n_4, n_5\}^4, \{n_2, n_3, n_4, n_5\}^4,$$
$$\{n_1, n_2, n_3, n_4, n_5\}^5.$$

For given vertices n and n' if

$$d(s_1,n) \neq d(s_1,n'), d(s_2,n) \neq d(s_2,n'), \ldots, d(s_k,n) \neq d(s_k,n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum cardinality between all k-number-resolving sets is called k-number-resolving number and it's denoted by
$\mathcal{N}^k(STR_{1,\sigma_2}) = k,\ k = \mathcal{O}(STR_{1,\sigma_2}) - 2, \mathcal{O}(STR_{1,\sigma_2}) - 1, \mathcal{O}(STR_{1,\sigma_2})$; and corresponded to k-number-resolving sets are

$$\begin{aligned}
&\{n_2,n_3,n_4\}^3, \{n_2,n_3,n_5\}^3, \{n_2,n_4,n_5\}^3,\\
&\{n_3,n_4,n_5\}^3, \{n_1,n_2,n_3,n_4\}^4, \{n_1,n_2,n_3,n_5\}^4,\\
&\{n_1,n_2,n_4,n_5\}^4, \{n_1,n_3,n_4,n_5\}^4, \{n_2,n_3,n_4,n_5\}^4,\\
&\{n_1,n_2,n_3,n_4,n_5\}^5;
\end{aligned}$$

(iv) there are ten k-number-resolving sets

$$\begin{aligned}
&\{n_2,n_3,n_4\}^3, \{n_2,n_3,n_5\}^3, \{n_2,n_4,n_5\}^3,\\
&\{n_3,n_4,n_5\}^3, \{n_1,n_2,n_3,n_4\}^4, \{n_1,n_2,n_3,n_5\}^4,\\
&\{n_1,n_2,n_4,n_5\}^4, \{n_1,n_3,n_4,n_5\}^4, \{n_2,n_3,n_4,n_5\}^4,\\
&\{n_1,n_2,n_3,n_4,n_5\}^5,
\end{aligned}$$

so as it's possible to have one of them as a set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is characteristic;

(v) there are ten k-number-resolving sets

$$\begin{aligned}
&\{n_2,n_3,n_4\}^3, \{n_2,n_3,n_5\}^3, \{n_2,n_4,n_5\}^3,\\
&\{n_3,n_4,n_5\}^3, \{n_1,n_2,n_3,n_4\}^4, \{n_1,n_2,n_3,n_5\}^4,\\
&\{n_1,n_2,n_4,n_5\}^4, \{n_1,n_3,n_4,n_5\}^4, \{n_2,n_3,n_4,n_5\}^4,\\
&\{n_1,n_2,n_3,n_4,n_5\}^5,
\end{aligned}$$

corresponded to k-number-resolving number as if there's one k-number-resolving set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is the determiner;

(vi) all k-number-resolving sets corresponded to k-number-resolving number are

$$\begin{aligned}
&\{n_i,n_j\}^2, \{n_i,n_j,n_k\}^3, \{n_i,n_j,n_k,n_r\}^4,\\
&\{n_i,n_j,n_k,n_r,n_s\}^5.
\end{aligned}$$

For given vertices n and n' if

$$d(s_1,n) \neq d(s_1,n'), d(s_2,n) \neq d(s_2,n'), \ldots, d(s_k,n) \neq d(s_k,n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then

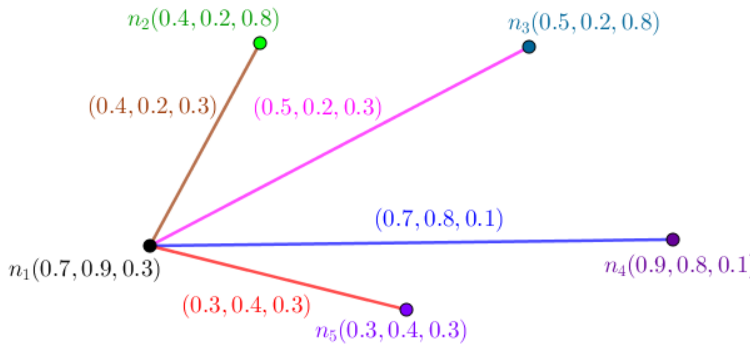

Figure 16. A Neutrosophic Graph in the Viewpoint of its k-number-resolving number and its neutrosophic k-number-resolving number.

the set of neutrosophic vertices, S is called k-number-resolving set. The minimum neutrosophic cardinality between all k-number-resolving sets is called neutrosophic k-number-resolving number and it's denoted by $\mathcal{N}_n^3(STR_{1,\sigma_2}) = 3.9, \mathcal{N}_n^4(STR_{1,\sigma_2}) = 5.8, \mathcal{N}_n^5(STR_{1,\sigma_2}) = 7.6$; and corresponded to k-number-resolving sets are

$$\{n_2, n_3, n_5\}^3, \{n_1, n_2, n_3, n_5\}^4, \{n_1, n_2, n_3, n_4, n_5\}^5.$$

Proposition 3.18. *Let $NTG : (V, E, \sigma, \mu)$ be a complete-bipartite-neutrosophic graph which isn't star-neutrosophic graph which means $|V_1|, |V_2| \geq 2$. Then*

$$\mathcal{N}_n^{\mathcal{O}(CMC_{\sigma_1,\sigma_2})-2}(CMC_{\sigma_1,\sigma_2}) = \min_{S=V\setminus\{n_i^1,n_j^2\}_{n_i^1\neq n_j^2}} \sum_{i=1}^{3} \sigma_i(x)_{x\in S}.$$

$$\mathcal{N}_n^{\mathcal{O}(CMC_{\sigma_1,\sigma_2})-1}(CMC_{\sigma_1,\sigma_2}) = \min_{|S|=\mathcal{O}(CMC_{\sigma_1,\sigma_2})-1} \sum_{i=1}^{3} \sigma_i(x)_{x\in S}.$$

$$\mathcal{N}_n^{\mathcal{O}(CMC_{\sigma_1,\sigma_2})}(CMC_{\sigma_1,\sigma_2}) = \mathcal{O}_n(CMC_{\sigma_1,\sigma_2}).$$

$$k = \mathcal{O}(CMC_{\sigma_1,\sigma_2}) - 2, \mathcal{O}(CMC_{\sigma_1,\sigma_2}) - 1, \mathcal{O}(CMC_{\sigma_1,\sigma_2}).$$

Proof. Suppose $CMC_{\sigma_1,\sigma_2} : (V, E, \sigma, \mu)$ is a complete-bipartite-neutrosophic graph. Every vertex in a part and another vertex in opposite part k-number-resolves any given vertex. Assume same parity for same partition of vertex set which means V_1 has odd indexes and V_2 has even indexes. In the setting of complete-bipartite, a vertex of resolving set corresponded to resolving number resolves as if it doesn't k-number-resolve so as resolving is different from k-number-resolving. All minimal k-number-resolving sets corresponded to k-number-resolving number are

$$V \setminus \{n_i^1, n_j^2\}_{n_i^1\neq n_j^2}^{\mathcal{O}(CMC_{\sigma_1,\sigma_2})-2}, V \setminus \{n_i\}^{\mathcal{O}(CMC_{\sigma_1,\sigma_2})-1}, V^{\mathcal{O}(CMC_{\sigma_1,\sigma_2})}.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices

$s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum neutrosophic cardinality between all k-number-resolving sets is called neutrosophic k-number-resolving number and it's denoted by

$$\mathcal{N}_n^{\mathcal{O}(CMC_{\sigma_1,\sigma_2})-2}(CMC_{\sigma_1,\sigma_2}) = \min_{S=V\setminus\{n_i^1,n_j^2\}_{n_i^1\neq n_j^2}} \sum_{i=1}^{3} \sigma_i(x)_{x\in S}.$$

$$\mathcal{N}_n^{\mathcal{O}(CMC_{\sigma_1,\sigma_2})-1}(CMC_{\sigma_1,\sigma_2}) = \min_{|S|=\mathcal{O}(CMC_{\sigma_1,\sigma_2})-1} \sum_{i=1}^{3} \sigma_i(x)_{x\in S}.$$

$$\mathcal{N}_n^{\mathcal{O}(CMC_{\sigma_1,\sigma_2})}(CMC_{\sigma_1,\sigma_2}) = \mathcal{O}_n(CMC_{\sigma_1,\sigma_2}).$$

$$k = \mathcal{O}(CMC_{\sigma_1,\sigma_2}) - 2, \mathcal{O}(CMC_{\sigma_1,\sigma_2}) - 1, \mathcal{O}(CMC_{\sigma_1,\sigma_2});$$

and corresponded to k-number-resolving sets are

$$V \setminus \{n_i^1, n_j^2\}_{n_i^1\neq n_j^2}^{\mathcal{O}(CMC_{\sigma_1,\sigma_2})-2}, V \setminus \{n_i\}^{\mathcal{O}(CMC_{\sigma_1,\sigma_2})-1}, V^{\mathcal{O}(CMC_{\sigma_1,\sigma_2})}.$$

Thus

$$\mathcal{N}_n^{\mathcal{O}(CMC_{\sigma_1,\sigma_2})-2}(CMC_{\sigma_1,\sigma_2}) = \min_{S=V\setminus\{n_i^1,n_j^2\}_{n_i^1\neq n_j^2}} \sum_{i=1}^{3} \sigma_i(x)_{x\in S}.$$

$$\mathcal{N}_n^{\mathcal{O}(CMC_{\sigma_1,\sigma_2})-1}(CMC_{\sigma_1,\sigma_2}) = \min_{|S|=\mathcal{O}(CMC_{\sigma_1,\sigma_2})-1} \sum_{i=1}^{3} \sigma_i(x)_{x\in S}.$$

$$\mathcal{N}_n^{\mathcal{O}(CMC_{\sigma_1,\sigma_2})}(CMC_{\sigma_1,\sigma_2}) = \mathcal{O}_n(CMC_{\sigma_1,\sigma_2}).$$

$$k = \mathcal{O}(CMC_{\sigma_1,\sigma_2}) - 2, \mathcal{O}(CMC_{\sigma_1,\sigma_2}) - 1, \mathcal{O}(CMC_{\sigma_1,\sigma_2}).$$

□

Proposition 3.19. *Let $NTG : (V, E, \sigma, \mu)$ be a complete-bipartite-neutrosophic graph. Then k-number-resolving number isn't equal to resolving number where $k \neq 1$.*

Proposition 3.20. *Let $NTG : (V, E, \sigma, \mu)$ be a complete-bipartite-neutrosophic graph with center c. Then*

(i) the number of k-number-resolving sets is $|V_1|$ multiplying $|V_2|$ plus $\mathcal{O}(CMC_{\sigma_1,\sigma_2})$ plus one where $k = \mathcal{O}(CMC_{\sigma_1,\sigma_2}) - 2$;

(ii) the number of k-number-resolving sets is $\mathcal{O}(CMC_{\sigma_1,\sigma_2})$ plus one where $k = \mathcal{O}(CMC_{\sigma_1,\sigma_2}) - 1$;

(iii) the number of k-number-resolving sets is one where $k = \mathcal{O}(CMC_{\sigma_1,\sigma_2})$.

Proposition 3.21. *Let $NTG : (V, E, \sigma, \mu)$ be a complete-bipartite-neutrosophic graph with center c. Then*

(i) the number of k-number-resolving sets corresponded to k-number-resolving number is $|V_1|$ multiplying $|V_2|$ where $k = \mathcal{O}(CMC_{\sigma_1,\sigma_2}) - 2$;

(ii) the number of k-number-resolving sets corresponded to k-number-resolving number is $\mathcal{O}(CMC_{\sigma_1,\sigma_2})$ where $k = \mathcal{O}(CMC_{\sigma_1,\sigma_2}) - 1$;

(iii) the number of k-number-resolving sets corresponded to k-number-resolving number is one where $k = \mathcal{O}(CMC_{\sigma_1,\sigma_2})$.

The clarifications about results are in progress as follows. A complete-bipartite-neutrosophic graph is related to previous result and it's studied to apply the definitions on it. To make it more clear, next part gives one special case to apply definitions and results on it. Some items are devised to make more senses about new notions. A complete-bipartite-neutrosophic graph is related to previous result and it's studied to apply the definitions on it, too.

Example 3.22. There is one section for clarifications. In Figure (17), a complete-bipartite-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows.

(i) For given two neutrosophic vertices, n and n', there is either one path with length one or one path with length two between them;

(ii) in the setting of complete-bipartite, a vertex of resolving set corresponded to resolving number resolves as if it doesn't k-number-resolve so as resolving is different from k-number-resolving;

(iii) all minimal k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_1,n_2\}^2,\{n_1,n_3\}^2,\{n_4,n_2\}^2,$$
$$\{n_4,n_3\}^2,\{n_1,n_2,n_3\}^3,\{n_1,n_2,n_4\}^3,$$
$$\{n_1,n_3,n_4\}^3,\{n_2,n_3,n_4\}^3,\{n_1,n_2,n_3,n_4\}^4.$$

For given vertices n and n' if

$$d(s_1,n)\neq d(s_1,n'),d(s_2,n)\neq d(s_2,n'),\ldots,d(s_k,n)\neq d(s_k,n'),$$

then $s_1,s_2,\ldots,s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V\setminus S$, there are at least neutrosophic vertices $s_1,s_2,\ldots,s_k$ in S such that $s_1,s_2,\ldots,s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum cardinality between all k-number-resolving sets is called k-number-resolving number and it's denoted by
$\mathcal{N}^k(CMC_{\sigma_1,\sigma_2})=k,\ k=\mathcal{O}(CMC_{\sigma_1,\sigma_2})-2,\mathcal{O}(CMC_{\sigma_1,\sigma_2})-1,\mathcal{O}(CMC_{\sigma_1,\sigma_2})$;
and corresponded to k-number-resolving sets are

$$\{n_1,n_2\}^2,\{n_1,n_3\}^2,\{n_4,n_2\}^2,$$
$$\{n_4,n_3\}^2,\{n_1,n_2,n_3\}^3,\{n_1,n_2,n_4\}^3,$$
$$\{n_1,n_3,n_4\}^3,\{n_2,n_3,n_4\}^3,\{n_1,n_2,n_3,n_4\}^4;$$

(iv) there are nine k-number-resolving sets

$$\{n_1,n_2\}^2,\{n_1,n_3\}^2,\{n_4,n_2\}^2,$$
$$\{n_4,n_3\}^2,\{n_1,n_2,n_3\}^{2,3},\{n_1,n_2,n_4\}^{2,3},$$
$$\{n_1,n_3,n_4\}^{2,3},\{n_2,n_3,n_4\}^{2,3},\{n_1,n_2,n_3,n_4\}^{2,3,4},$$

so as it's possible to have one of them as a set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is characteristic;

(v) there are nine k-number-resolving sets

$$\{n_1,n_2\}^2,\{n_1,n_3\}^2,\{n_4,n_2\}^2,$$
$$\{n_4,n_3\}^2,\{n_1,n_2,n_3\}^3,\{n_1,n_2,n_4\}^3,$$
$$\{n_1,n_3,n_4\}^3,\{n_2,n_3,n_4\}^3,\{n_1,n_2,n_3,n_4\}^4,$$

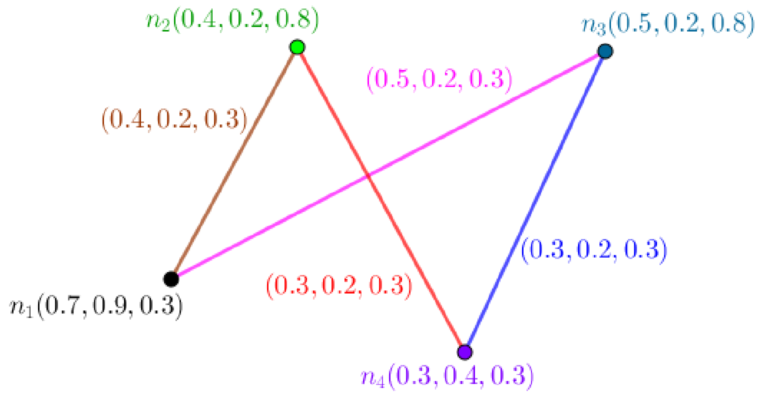

Figure 17. A Neutrosophic Graph in the Viewpoint of its k-number-resolving number and its neutrosophic k-number-resolving number.

corresponded to k-number-resolving number as if there's one k-number-resolving set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is the determiner;

(vi) all k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_1, n_2\}^2, \{n_1, n_3\}^2, \{n_4, n_2\}^2,$$
$$\{n_4, n_3\}^2, \{n_1, n_2, n_3\}^3, \{n_1, n_2, n_4\}^3,$$
$$\{n_1, n_3, n_4\}^3, \{n_2, n_3, n_4\}^3, \{n_1, n_2, n_3, n_4\}^4.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum neutrosophic cardinality between all k-number-resolving sets is called neutrosophic k-number-resolving number and it's denoted by
$\mathcal{N}_n^2(CMC_{\sigma_1,\sigma_2}) = 2.4, \mathcal{N}_n^3(CMC_{\sigma_1,\sigma_2}) = 3.9, \mathcal{N}_n^4(CMC_{\sigma_1,\sigma_2}) = 5.8$; and corresponded to k-number-resolving sets are

$$\{n_4, n_2\}^2, \{n_2, n_3, n_4\}^3, \{n_1, n_2, n_3, n_4\}^4.$$

Proposition 3.23. *Let $NTG : (V, E, \sigma, \mu)$ be a complete-t-partite-neutrosophic graph where $t \geq 3$ and $|V_i \geq 2$. Then*

$$\mathcal{N}_n^{\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})-2}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) = \min_{S=V\setminus\{n_i^r,n_j^s\}_{n_i^r\neq n_j^s}} \sum_{i=1}^{3} \sigma_i(x)_{x\in S}$$

$$\mathcal{N}_n^{\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})-1}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) = \min_{|S|=\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})-1} \sum_{i=1}^{3} \sigma_i(x)_{x\in S}.$$

$$\mathcal{N}_n^{\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) = \mathcal{O}_n(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}).$$

$$k = \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) - 2, \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) - 1, \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}).$$

Proof. Suppose $CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t} : (V, E, \sigma, \mu)$ is a complete-t-partite-neutrosophic graph. Every vertex in a part is k-number-resolved by another vertex in another part. Assume same parity for same partition of vertex set which means V_i has odd indexes and V_j has even indexes. In the setting of complete-t-partite, a vertex of resolving set corresponded to resolving number resolves as if it doesn't k-number-resolve so as resolving is different from k-number-resolving. All minimal k-number-resolving sets corresponded to k-number-resolving number are

$$V \setminus \{n_i^r, n_j^s\}_{n_i^r \neq n_j^s}^{\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})-2}, V \setminus \{n_i\}^{\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})-1}, V^{\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})}.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum neutrosophic cardinality between all k-number-resolving sets is called neutrosophic k-number-resolving number and it's denoted by

$$\mathcal{N}_n^{\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})-2}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) = \min_{S=V\setminus\{n_i^r,n_j^s\}_{n_i^r\neq n_j^s}} \sum_{i=1}^{3} \sigma_i(x)_{x\in S}$$

$$\mathcal{N}_n^{\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})-1}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) = \min_{|S|=\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})-1} \sum_{i=1}^{3} \sigma_i(x)_{x\in S}.$$

$$\mathcal{N}_n^{\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) = \mathcal{O}_n(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}).$$

$$k = \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) - 2, \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) - 1, \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t});$$

and corresponded to k-number-resolving sets are

$$V \setminus \{n_i^r, n_j^s\}_{n_i^r \neq n_j^s}^{\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})-2}, V \setminus \{n_i\}^{\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})-1}, V^{\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})}.$$

Thus

$$\mathcal{N}_n^{\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})-2}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) = \min_{S=V\setminus\{n_i^r,n_j^s\}_{n_i^r\neq n_j^s}} \sum_{i=1}^{3} \sigma_i(x)_{x\in S}$$

$$\mathcal{N}_n^{\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})-1}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) = \min_{|S|=\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})-1} \sum_{i=1}^{3} \sigma_i(x)_{x\in S}.$$

$$\mathcal{N}_n^{\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) = \mathcal{O}_n(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}).$$

$$k = \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) - 2, \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) - 1, \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}).$$

□

Proposition 3.24. *Let $NTG : (V, E, \sigma, \mu)$ be a complete-t-partite-neutrosophic graph. Then k-number-resolving number isn't equal to resolving number where $k \neq 1$.*

Proposition 3.25. *Let $NTG : (V, E, \sigma, \mu)$ be a complete-t-partite-neutrosophic graph with center c. Then* (*i*) *the number of k-number-resolving sets is* $|V_1|$ *multiplying* $|V_2|$ *plus* $\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})$ *plus one where* $k = \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) - 2$;

(*ii*) *the number of k-number-resolving sets is* $\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})$ *plus one where* $k = \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) - 1$;

(*iii*) *the number of k-number-resolving sets is one where* $k = \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})$.

Proposition 3.26. *Let* $NTG : (V, E, \sigma, \mu)$ *be a complete-t-partite-neutrosophic graph with center c. Then*

(*i*) *the number of k-number-resolving sets corresponded to k-number-resolving number is* $|V_1|$ *multiplying* $|V_2|$ *where* $k = \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) - 2$;

(*ii*) *the number of k-number-resolving sets corresponded to k-number-resolving number is* $\mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})$ *where* $k = \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) - 1$;

(*iii*) *the number of k-number-resolving sets corresponded to k-number-resolving number is one where* $k = \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})$.

Example 3.27. There is one section for clarifications. In Figure (18), a complete-t-partite-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows.

(*i*) For given two neutrosophic vertices, n and n', there is either one path with length one or one path with length two between them;

(*ii*) in the setting of complete-t-partite, a vertex of resolving set corresponded to resolving number resolves as if it doesn't k-number-resolve so as resolving is different from k-number-resolving;

(*iii*) all minimal k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_1, n_2, n_3\}^3, \{n_1, n_2, n_5\}^3, \{n_1, n_3, n_5\}^3,$$
$$\{n_4, n_2, n_3\}^3, \{n_4, n_2, n_5\}^3, \{n_4, n_3, n_5\}^3,$$
$$\{n_1, n_2, n_3, n_4\}^4, \{n_1, n_2, n_3, n_5\}^4, \{n_1, n_2, n_4, n_5\}^4,$$
$$\{n_1, n_3, n_4, n_5\}^4, \{n_2, n_3, n_4, n_5\}^4, \{n_1, n_2, n_3, n_4, n_5\}^5.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum cardinality between all k-number-resolving sets is called k-number-resolving number and it's denoted by $\mathcal{N}^k(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) = k,\ k = \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) - 2, \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) - 1, \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})$; and corresponded to k-number-resolving sets are

$$\{n_1, n_2, n_3\}^3, \{n_1, n_2, n_5\}^3, \{n_1, n_3, n_5\}^3,$$
$$\{n_4, n_2, n_3\}^3, \{n_4, n_2, n_5\}^3, \{n_4, n_3, n_5\}^3,$$
$$\{n_1, n_2, n_3, n_4\}^4, \{n_1, n_2, n_3, n_5\}^4, \{n_1, n_2, n_4, n_5\}^4,$$
$$\{n_1, n_3, n_4, n_5\}^4, \{n_2, n_3, n_4, n_5\}^4, \{n_1, n_2, n_3, n_4, n_5\}^5;$$

(iv) there are sixteen k-number-resolving sets

$$\{n_1,n_2,n_3\}^3,\{n_1,n_2,n_5\}^3,\{n_1,n_3,n_5\}^3,$$
$$\{n_4,n_2,n_3\}^3,\{n_4,n_2,n_5\}^3,\{n_4,n_3,n_5\}^3,$$
$$\{n_1,n_2,n_3,n_4\}^{3,4},\{n_1,n_2,n_3,n_5\}^{3,4},\{n_1,n_2,n_4,n_5\}^{3,4},$$
$$\{n_1,n_3,n_4,n_5\}^{3,4},\{n_2,n_3,n_4,n_5\}^{3,4},\{n_1,n_2,n_3,n_4,n_5\}^{3,4,5},$$

so as it's possible to have one of them as a set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is characteristic;

(v) there are sixteen k-number-resolving sets

$$\{n_1,n_2,n_3\}^3,\{n_1,n_2,n_5\}^3,\{n_1,n_3,n_5\}^3,$$
$$\{n_4,n_2,n_3\}^3,\{n_4,n_2,n_5\}^3,\{n_4,n_3,n_5\}^3,$$
$$\{n_1,n_2,n_3,n_4\}^4,\{n_1,n_2,n_3,n_5\}^4,\{n_1,n_2,n_4,n_5\}^4,$$
$$\{n_1,n_3,n_4,n_5\}^4,\{n_2,n_3,n_4,n_5\}^4,\{n_1,n_2,n_3,n_4,n_5\}^5,$$

corresponded to k-number-resolving number as if there's one k-number-resolving set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is the determiner;

(vi) all k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_1,n_2,n_3\}^3,\{n_1,n_2,n_5\}^3,\{n_1,n_3,n_5\}^3,$$
$$\{n_4,n_2,n_3\}^3,\{n_4,n_2,n_5\}^3,\{n_4,n_3,n_5\}^3,$$
$$\{n_1,n_2,n_3,n_4\}^4,\{n_1,n_2,n_3,n_5\}^4,\{n_1,n_2,n_4,n_5\}^4,$$
$$\{n_1,n_3,n_4,n_5\}^4,\{n_2,n_3,n_4,n_5\}^4,\{n_1,n_2,n_3,n_4,n_5\}^5.$$

For given vertices n and n' if

$$d(s_1,n)\neq d(s_1,n'),d(s_2,n)\neq d(s_2,n'),\ldots,d(s_k,n)\neq d(s_k,n'),$$

then $s_1,s_2,\ldots,s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V\setminus S$, there are at least neutrosophic vertices $s_1,s_2,\ldots,s_k$ in S such that $s_1,s_2,\ldots,s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum neutrosophic cardinality between all k-number-resolving sets is called neutrosophic k-number-resolving number and it's denoted by $\mathcal{N}_n^3(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})=3.8,\mathcal{N}_n^4(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})=5.3,\mathcal{N}_n^5(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})=7.2$; and corresponded to k-number-resolving sets are

$$\{n_4,n_2,n_5\}^3,\{n_2,n_3,n_4,n_5\}^4,\{n_1,n_2,n_3,n_4,n_5\}^5.$$

Proposition 3.28. *Let $NTG:(V,E,\sigma,\mu)$ be a wheel-neutrosophic graph. Then*

$$\mathcal{N}_n^1=\min_{S=V\setminus\{n_i^r,n_j^s,n_{\mathcal{O}(WHL_{1,\sigma_2})}\}_{n_i^rn_j^s\in E,n_i^r,n_j^s,n_{\mathcal{O}(WHL_{1,\sigma_2})}\text{ are pairwise disjoint.}}}\sum_{i=1}^{3}\sigma_i(x)_{x\in S}.$$

$$\mathcal{N}_n^{\mathcal{O}(WHL_{1,\sigma_2})-1}(WHL_{1,\sigma_2})=\min_{|S|=\mathcal{O}(WHL_{1,\sigma_2})-1}\sum_{i=1}^{3}\sigma_i(x)_{x\in S}.$$

$$\mathcal{N}_n^{\mathcal{O}(WHL_{1,\sigma_2})}(WHL_{1,\sigma_2})=\mathcal{O}_n(WHL_{1,\sigma_2}).$$
$$k=1,\mathcal{O}(WHL_{1,\sigma_2})-1,\mathcal{O}(WHL_{1,\sigma_2}).$$

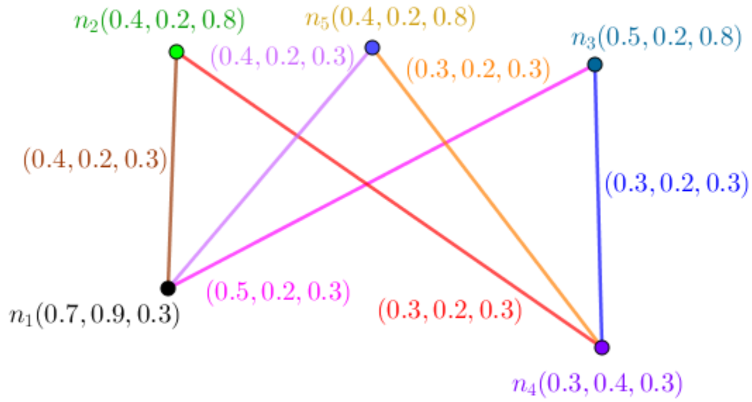

Figure 18. A Neutrosophic Graph in the Viewpoint of its k-number-resolving number and its neutrosophic k-number-resolving number.

Proof. Suppose $WHL_{1,\sigma_2} : (V, E, \sigma, \mu)$ is a wheel-neutrosophic graph. The argument is elementary. All vertices of a cycle

$$n_1, n_2, n_3, \cdots, n_{\mathcal{O}(WHL_{1,\sigma_2})-3}, n_{\mathcal{O}(WHL_{1,\sigma_2})-2}, n_{\mathcal{O}(WHL_{1,\sigma_2})-1}, n_1$$

join to one vertex, $c = n_{\mathcal{O}(WHL_{1,\sigma_2})}$. For every vertices, the minimum number of edges amid them is either one or two because of center and the notion of neighbors. In the setting of wheel, a vertex of resolving set corresponded to resolving number resolves as if it doesn't k-number-resolve so as resolving is different from k-number-resolving. All minimal k-number-resolving sets corresponded to k-number-resolving number are

$$V \setminus \{n_i^r, n_j^s, n_{\mathcal{O}(WHL_{1,\sigma_2})}\}^{\mathcal{O}(WHL_{1,\sigma_2})-3}_{n_i^r n_j^s \in E, n_i^r, n_j^s, n_{\mathcal{O}(WHL_{1,\sigma_2})} \text{are pairwise disjoint.}},$$
$$V \setminus \{n_i\}^{\mathcal{O}(WHL_{1,\sigma_2})-1}, V^{\mathcal{O}(WHL_{1,\sigma_2})}.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum neutrosophic cardinality between all k-number-resolving sets is called neutrosophic k-number-resolving number and it's denoted by

$$\mathcal{N}_n^1 = \min_{S = V \setminus \{n_i^r, n_j^s, n_{\mathcal{O}(WHL_{1,\sigma_2})}\}_{n_i^r n_j^s \in E, n_i^r, n_j^s, n_{\mathcal{O}(WHL_{1,\sigma_2})} \text{are pairwise disjoint.}}} \sum_{i=1}^{3} \sigma_i(x)_{x \in S}.$$

$$\mathcal{N}_n^{\mathcal{O}(WHL_{1,\sigma_2})-1}(WHL_{1,\sigma_2}) = \min_{|S| = \mathcal{O}(WHL_{1,\sigma_2})-1} \sum_{i=1}^{3} \sigma_i(x)_{x \in S}.$$

$$\mathcal{N}_n^{\mathcal{O}(WHL_{1,\sigma_2})}(WHL_{1,\sigma_2}) = \mathcal{O}_n(WHL_{1,\sigma_2}).$$

$$k = 1, \mathcal{O}(WHL_{1,\sigma_2}) - 1, \mathcal{O}(WHL_{1,\sigma_2});$$

and corresponded to k-number-resolving sets are

$$V \setminus \{n_i^r, n_j^s, n_{\mathcal{O}(WHL_{1,\sigma_2})}\}^{\mathcal{O}(WHL_{1,\sigma_2})-3}_{n_i^r n_j^s \in E, n_i^r, n_j^s, n_{\mathcal{O}(WHL_{1,\sigma_2})} \text{are pairwise disjoint.}},$$
$$V \setminus \{n_i\}^{\mathcal{O}(WHL_{1,\sigma_2})-1}, V^{\mathcal{O}(WHL_{1,\sigma_2})}.$$

Thus

$$\mathcal{N}_n^1 = \min_{S=V\setminus\{n_i^r,n_j^s,n_{\mathcal{O}(WHL_{1,\sigma_2})}\}_{n_i^r n_j^s \in E, n_i^r, n_j^s, n_{\mathcal{O}(WHL_{1,\sigma_2})} \text{are pairwise disjoint.}}} \sum_{i=1}^{3} \sigma_i(x)_{x\in S}.$$

$$\mathcal{N}_n^{\mathcal{O}(WHL_{1,\sigma_2})-1}(WHL_{1,\sigma_2}) = \min_{|S|=\mathcal{O}(WHL_{1,\sigma_2})-1} \sum_{i=1}^{3} \sigma_i(x)_{x\in S}.$$

$$\mathcal{N}_n^{\mathcal{O}(WHL_{1,\sigma_2})}(WHL_{1,\sigma_2}) = \mathcal{O}_n(WHL_{1,\sigma_2}).$$

$$k = 1, \mathcal{O}(WHL_{1,\sigma_2}) - 1, \mathcal{O}(WHL_{1,\sigma_2}).$$

□

Proposition 3.29. *Let $NTG : (V, E, \sigma, \mu)$ be a wheel-neutrosophic graph. Then k-number-resolving number isn't equal to resolving number where $k \neq 1$.*

Proposition 3.30. *Let $NTG : (V, E, \sigma, \mu)$ be a wheel-neutrosophic graph with center c. Then*

(i) *the number of k-number-resolving sets is $\mathcal{O}(WHL_{1,\sigma_2}) - 1$ plus $\mathcal{O}(WHL_{1,\sigma_2})$ plus one where $k = \mathcal{O}(WHL_{1,\sigma_2}) - 3$;*

(ii) *the number of k-number-resolving sets is $\mathcal{O}(WHL_{1,\sigma_2})$ plus one where $k = \mathcal{O}(WHL_{1,\sigma_2}) - 1$;*

(iii) *the number of k-number-resolving sets is one where $k = \mathcal{O}(WHL_{1,\sigma_2})$.*

Proposition 3.31. *Let $NTG : (V, E, \sigma, \mu)$ be a wheel-neutrosophic graph with center c. Then*

(i) *the number of k-number-resolving sets corresponded to k-number-resolving number is $\mathcal{O}(WHL_{1,\sigma_2}) - 1$ where $k = \mathcal{O}(WHL_{1,\sigma_2}) - 3$;*

(ii) *the number of k-number-resolving sets corresponded to k-number-resolving number is $\mathcal{O}(WHL_{1,\sigma_2})$ where $k = \mathcal{O}(WHL_{1,\sigma_2}) - 1$;*

(iii) *the number of k-number-resolving sets corresponded to k-number-resolving number is one where $k = \mathcal{O}(WHL_{1,\sigma_2})$.*

Example 3.32. There is one section for clarifications. In Figure (19), a wheel-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows.

(i) For given two neutrosophic vertices, n and n', there is either one path with length one or one path with length two between them;

(ii) in the setting of wheel, a vertex of resolving set corresponded to resolving number resolves as if it doesn't k-number-resolve so as resolving is different from k-number-resolving;

(*iii*) all minimal k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_4, n_5\}^1, \{n_5, n_2\}^1, \{n_2, n_3\}^1,$$
$$\{n_3, n_4\}^1, \{n_1, n_4, n_5\}^1, \{n_1, n_5, n_2\}^1,$$
$$\{n_1, n_2, n_3\}^1, \{n_1, n_3, n_4\}^1, \{n_1, n_2, n_3, n_4\}^4,$$
$$\{n_1, n_2, n_3, n_5\}^4, \{n_1, n_2, n_4, n_5\}^4, \{n_1, n_3, n_4, n_5\}^4,$$
$$\{n_2, n_3, n_4, n_5\}^4, \{n_1, n_2, n_3, n_4, n_5\}^5.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum cardinality between all k-number-resolving sets is called k-number-resolving number and it's denoted by

$$\mathcal{N}^1 = \mathcal{O}(WHL_{1,\sigma_2}) - 3.$$
$$\mathcal{N}^{\mathcal{O}(WHL_{1,\sigma_2})-1}(WHL_{1,\sigma_2}) = \mathcal{O}(WHL_{1,\sigma_2}) - 1.$$
$$\mathcal{N}^{\mathcal{O}(WHL_{1,\sigma_2})}(WHL_{1,\sigma_2}) = \mathcal{O}(WHL_{1,\sigma_2}).$$
$$k = 1, \mathcal{O}(WHL_{1,\sigma_2}) - 1, \mathcal{O}(WHL_{1,\sigma_2});$$

and corresponded to k-number-resolving sets are

$$\{n_4, n_5\}^1, \{n_5, n_2\}^1, \{n_2, n_3\}^1,$$
$$\{n_3, n_4\}^1, \{n_1, n_4, n_5\}^1, \{n_1, n_5, n_2\}^1,$$
$$\{n_1, n_2, n_3\}^1, \{n_1, n_3, n_4\}^1, \{n_1, n_2, n_3, n_4\}^4,$$
$$\{n_1, n_2, n_3, n_5\}^4, \{n_1, n_2, n_4, n_5\}^4, \{n_1, n_3, n_4, n_5\}^4,$$
$$\{n_2, n_3, n_4, n_5\}^4, \{n_1, n_2, n_3, n_4, n_5\}^5;$$

(*iv*) there are fourteen k-number-resolving sets

$$\{n_4, n_5\}^1, \{n_5, n_2\}^1, \{n_2, n_3\}^1,$$
$$\{n_3, n_4\}^1, \{n_1, n_4, n_5\}^1, \{n_1, n_5, n_2\}^1,$$
$$\{n_1, n_2, n_3\}^1, \{n_1, n_3, n_4\}^1, \{n_1, n_2, n_3, n_4\}^{1,2,3,4},$$
$$\{n_1, n_2, n_3, n_5\}^{1,2,3,4}, \{n_1, n_2, n_4, n_5\}^{1,2,3,4}, \{n_1, n_3, n_4, n_5\}^{1,2,3,4},$$
$$\{n_2, n_3, n_4, n_5\}^{1,2,3,4}, \{n_1, n_2, n_3, n_4, n_5\}^{1,2,3,4,5},$$

so as it's possible to have one of them as a set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is characteristic;

(*v*) there are fourteen k-number-resolving sets

$$\{n_4, n_5\}^1, \{n_5, n_2\}^1, \{n_2, n_3\}^1,$$
$$\{n_3, n_4\}^1, \{n_1, n_4, n_5\}^1, \{n_1, n_5, n_2\}^1,$$
$$\{n_1, n_2, n_3\}^1, \{n_1, n_3, n_4\}^1, \{n_1, n_2, n_3, n_4\}^4,$$
$$\{n_1, n_2, n_3, n_5\}^4, \{n_1, n_2, n_4, n_5\}^4, \{n_1, n_3, n_4, n_5\}^4,$$
$$\{n_2, n_3, n_4, n_5\}^4, \{n_1, n_2, n_3, n_4, n_5\}^5,$$

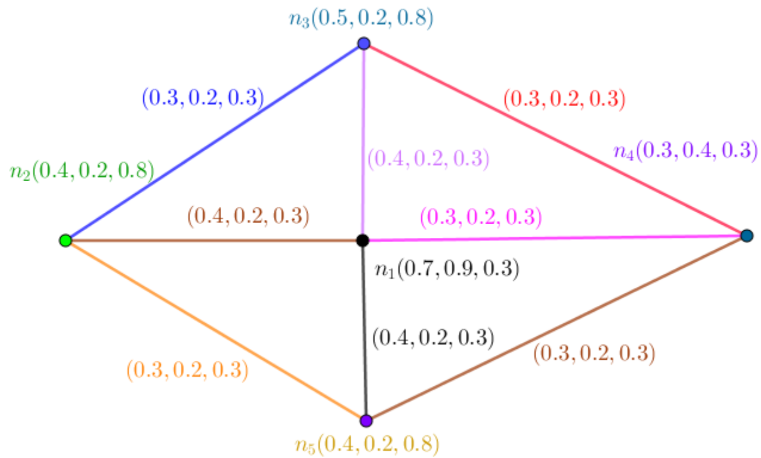

Figure 19. A Neutrosophic Graph in the Viewpoint of its k-number-resolving number and its neutrosophic k-number-resolving number.

corresponded to k-number-resolving number as if there's one k-number-resolving set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is the determiner;

(vi) all k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_4, n_5\}^1, \{n_5, n_2\}^1, \{n_2, n_3\}^1,$$
$$\{n_3, n_4\}^1, \{n_1, n_4, n_5\}^1, \{n_1, n_5, n_2\}^1,$$
$$\{n_1, n_2, n_3\}^1, \{n_1, n_3, n_4\}^1, \{n_1, n_2, n_3, n_4\}^4,$$
$$\{n_1, n_2, n_3, n_5\}^4, \{n_1, n_2, n_4, n_5\}^4, \{n_1, n_3, n_4, n_5\}^4,$$
$$\{n_2, n_3, n_4, n_5\}^4, \{n_1, n_2, n_3, n_4, n_5\}^5.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum neutrosophic cardinality between all k-number-resolving sets is called neutrosophic k-number-resolving number and it's denoted by

$$\mathcal{N}_n^1 = 2.4.$$

$$\mathcal{N}_n^{\mathcal{O}(WHL_{1,\sigma_2})-1}(WHL_{1,\sigma_2}) = 5.3.$$

$$\mathcal{N}_n^{\mathcal{O}(WHL_{1,\sigma_2})}(WHL_{1,\sigma_2}) = 7.2.$$

$$k = 1, \mathcal{O}(WHL_{1,\sigma_2}) - 1, \mathcal{O}(WHL_{1,\sigma_2});$$

and corresponded to k-number-resolving sets are

$$\{n_4, n_5\}^1, \{n_2, n_3, n_4, n_5\}^4, \{n_1, n_2, n_3, n_4, n_5\}^5.$$

4 Applications in Time Table and Scheduling

In this section, two applications for time table and scheduling are provided where the models are either complete models which mean complete connections are formed as individual and family of complete models with common neutrosophic vertex set or quasi-complete models which mean quasi-complete connections are formed as individual and family of quasi-complete models with common neutrosophic vertex set.

Designing the programs to achieve some goals is general approach to apply on some issues to function properly. Separation has key role in the context of this style. Separating the duration of work which are consecutive, is the matter and it has importance to avoid mixing up.

Step 1. (Definition) Time table is an approach to get some attributes to do the work fast and proper. The style of scheduling implies special attention to the tasks which are consecutive.

Step 2. (Issue) Scheduling of program has faced with difficulties to differ amid consecutive sections. Beyond that, sometimes sections are not the same.

Step 3. (Model) The situation is designed as a model. The model uses data to assign every section and to assign to relation amid sections, three numbers belong unit interval to state indeterminacy, possibilities and determinacy. There's one restriction in that, the numbers amid two sections are at least the number of the relations amid them. Table (1), clarifies about the assigned numbers to these situations.

Table 1. Scheduling concerns its Subjects and its Connections as a neutrosophic graph in a Model.

Sections of NTG	n_1	$n_2 \cdots$	n_5
Values	$(0.7, 0.9, 0.3)$	$(0.4, 0.2, 0.8) \cdots$	$(0.4, 0.2, 0.8)$
Connections of NTG	E_1	$E_2 \cdots$	E_6
Values	$(0.4, 0.2, 0.3)$	$(0.5, 0.2, 0.3) \cdots$	$(0.3, 0.2, 0.3)$

4.1 Case 1: Complete-t-partite Model alongside its k-number-resolving number and its neutrosophic k-number-resolving number

Step 4. (Solution) The neutrosophic graph alongside its k-number-resolving number and its neutrosophic k-number-resolving number as model, propose to use specific number. Every subject has connection with some subjects. Thus the connection is applied as possible and the model demonstrates quasi-full connections as quasi-possible. Using the notion of strong on the connection amid subjects, causes the importance of subject goes in the highest level such that the value amid two consecutive subjects, is determined by those subjects. If the configuration is star, the number is different. Also, it holds for other types such that complete, wheel, path, and cycle. The collection of situations is another application of its k-number-resolving number and its neutrosophic k-number-resolving number when the notion of family is applied in the way that all members of family are from same classes of neutrosophic graphs. As follows, there are five subjects which are represented as Figure (20). This model is strong and even more it's quasi-complete. And the study proposes using specific number which is called its k-number-resolving number and its neutrosophic k-number-resolving number.

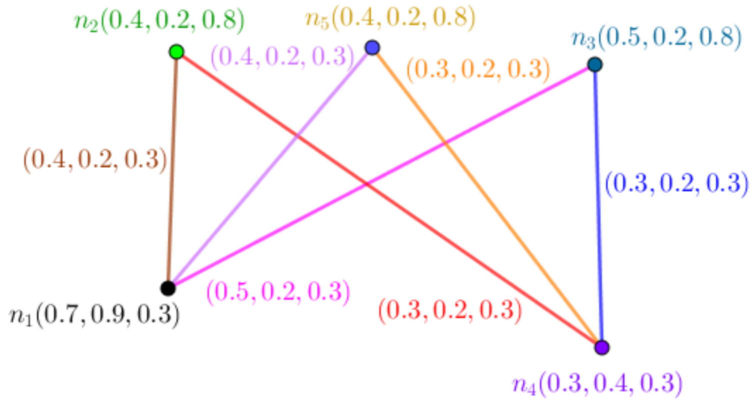

Figure 20. A Neutrosophic Graph in the Viewpoint of its k-number-resolving number and its neutrosophic k-number-resolving number

There are also some analyses on other numbers in the way that, the clarification is gained about being special number or not. Also, in the last part, there is one neutrosophic number to assign to this model and situation to compare them with same situations to get more precise. Consider Figure (20). In Figure (20), an complete-t-partite-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows.

(i) For given two neutrosophic vertices, n and n', there is either one path with length one or one path with length two between them;

(ii) in the setting of complete-t-partite, a vertex of resolving set corresponded to resolving number resolves as if it doesn't k-number-resolve so as resolving is different from k-number-resolving;

(iii) all minimal k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_1, n_2, n_3\}^3, \{n_1, n_2, n_5\}^3, \{n_1, n_3, n_5\}^3,$$
$$\{n_4, n_2, n_3\}^3, \{n_4, n_2, n_5\}^3, \{n_4, n_3, n_5\}^3,$$
$$\{n_1, n_2, n_3, n_4\}^4, \{n_1, n_2, n_3, n_5\}^4, \{n_1, n_2, n_4, n_5\}^4,$$
$$\{n_1, n_3, n_4, n_5\}^4, \{n_2, n_3, n_4, n_5\}^4, \{n_1, n_2, n_3, n_4, n_5\}^5.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum cardinality between all k-number-resolving sets is called k-number-resolving number and it's denoted by $\mathcal{N}^k(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) = k,\ k = \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) - 2, \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) - 1, \mathcal{O}(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t})$; and corresponded to k-number-resolving sets are

$$\{n_1, n_2, n_3\}^3, \{n_1, n_2, n_5\}^3, \{n_1, n_3, n_5\}^3,$$
$$\{n_4, n_2, n_3\}^3, \{n_4, n_2, n_5\}^3, \{n_4, n_3, n_5\}^3,$$
$$\{n_1, n_2, n_3, n_4\}^4, \{n_1, n_2, n_3, n_5\}^4, \{n_1, n_2, n_4, n_5\}^4,$$
$$\{n_1, n_3, n_4, n_5\}^4, \{n_2, n_3, n_4, n_5\}^4, \{n_1, n_2, n_3, n_4, n_5\}^5;$$

(iv) there are sixteen k-number-resolving sets

$$\{n_1, n_2, n_3\}^3, \{n_1, n_2, n_5\}^3, \{n_1, n_3, n_5\}^3,$$
$$\{n_4, n_2, n_3\}^3, \{n_4, n_2, n_5\}^3, \{n_4, n_3, n_5\}^3,$$
$$\{n_1, n_2, n_3, n_4\}^{3,4}, \{n_1, n_2, n_3, n_5\}^{3,4}, \{n_1, n_2, n_4, n_5\}^{3,4},$$
$$\{n_1, n_3, n_4, n_5\}^{3,4}, \{n_2, n_3, n_4, n_5\}^{3,4}, \{n_1, n_2, n_3, n_4, n_5\}^{3,4,5},$$

so as it's possible to have one of them as a set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is characteristic;

(v) there are sixteen k-number-resolving sets

$$\{n_1, n_2, n_3\}^3, \{n_1, n_2, n_5\}^3, \{n_1, n_3, n_5\}^3,$$
$$\{n_4, n_2, n_3\}^3, \{n_4, n_2, n_5\}^3, \{n_4, n_3, n_5\}^3,$$
$$\{n_1, n_2, n_3, n_4\}^4, \{n_1, n_2, n_3, n_5\}^4, \{n_1, n_2, n_4, n_5\}^4,$$
$$\{n_1, n_3, n_4, n_5\}^4, \{n_2, n_3, n_4, n_5\}^4, \{n_1, n_2, n_3, n_4, n_5\}^5,$$

corresponded to k-number-resolving number as if there's one k-number-resolving set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is the determiner;

(vi) all k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_1, n_2, n_3\}^3, \{n_1, n_2, n_5\}^3, \{n_1, n_3, n_5\}^3,$$
$$\{n_4, n_2, n_3\}^3, \{n_4, n_2, n_5\}^3, \{n_4, n_3, n_5\}^3,$$
$$\{n_1, n_2, n_3, n_4\}^4, \{n_1, n_2, n_3, n_5\}^4, \{n_1, n_2, n_4, n_5\}^4,$$
$$\{n_1, n_3, n_4, n_5\}^4, \{n_2, n_3, n_4, n_5\}^4, \{n_1, n_2, n_3, n_4, n_5\}^5.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum neutrosophic cardinality between all k-number-resolving sets is called neutrosophic k-number-resolving number and it's denoted by $\mathcal{N}_n^3(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) = 3.8, \mathcal{N}_n^4(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) = 5.3, \mathcal{N}_n^5(CMC_{\sigma_1,\sigma_2,\cdots,\sigma_t}) = 7.2$; and corresponded to k-number-resolving sets are

$$\{n_4, n_2, n_5\}^3, \{n_2, n_3, n_4, n_5\}^4, \{n_1, n_2, n_3, n_4, n_5\}^5.$$

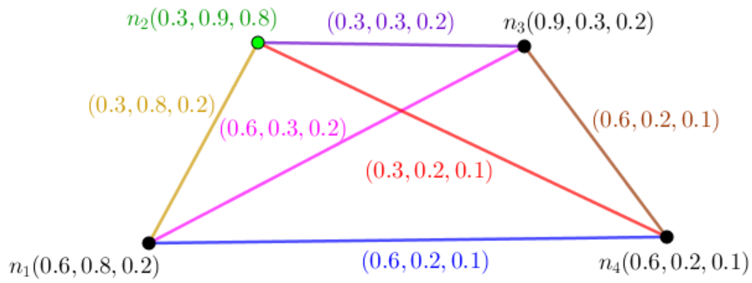

Figure 21. A Neutrosophic Graph in the Viewpoint of its k-number-resolving number and its neutrosophic k-number-resolving number

4.2 Case 2: Complete Model alongside its Neutrosophic Graph in the Viewpoint of its k-number-resolving number and its neutrosophic k-number-resolving number

Step 4. (Solution) The neutrosophic graph alongside its k-number-resolving number and its neutrosophic k-number-resolving number as model, propose to use specific number. Every subject has connection with every given subject in deemed way. Thus the connection applied as possible and the model demonstrates full connections as possible between parts but with different view where symmetry amid vertices and edges are the matters. Using the notion of strong on the connection amid subjects, causes the importance of subject goes in the highest level such that the value amid two consecutive subjects, is determined by those subjects. If the configuration is complete multipartite, the number is different. Also, it holds for other types such that star, wheel, path, and cycle. The collection of situations is another application of its k-number-resolving number and its neutrosophic k-number-resolving number when the notion of family is applied in the way that all members of family are from same classes of neutrosophic graphs. As follows, there are four subjects which are represented in the formation of one model as Figure (21). This model is neutrosophic strong as individual and even more it's complete. And the study proposes using specific number which is called its k-number-resolving number and its neutrosophic k-number-resolving number for this model. There are also some analyses on other numbers in the way that, the clarification is gained about being special number or not. Also, in the last part, there is one neutrosophic number to assign to these models as individual. A model as a collection of situations to compare them with another model as a collection of situations to get more precise. Consider Figure (21). There is one section for clarifications.

(i) For given neutrosophic vertex, s, there's an edge with other vertices;

(ii) in the setting of complete, a vertex of resolving set corresponded to resolving number resolves as if it doesn't k-number-resolve so as resolving is different from k-number-resolving. Resolving number and k-number-resolving number are the same if $k = 1$;

(iii) all minimal k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_1, n_2, n_3\}^3, \{n_1, n_2, n_4\}^3, \{n_1, n_3, n_4\}^3.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum cardinality between all k-number-resolving sets is called k-number-resolving number and it's denoted by $\mathcal{N}^k(CMT_\sigma) = k,\ k = \mathcal{O}(CMT_\sigma) - 1$; and corresponded to k-number-resolving sets are

$$\{n_1, n_2, n_3\}^3, \{n_1, n_2, n_4\}^3, \{n_1, n_3, n_4\}^3;$$

(*iv*) there are four k-number-resolving sets

$$\{n_1, n_2, n_3\}^3, \{n_1, n_2, n_4\}^3, \{n_1, n_3, n_4\}^3,$$
$$\{n_1, n_2, n_3, n_4\}^4,$$

so as it's possible to have one of them as a set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is characteristic;

(*v*) there are three k-number-resolving sets

$$\{n_1, n_2, n_3\}^3, \{n_1, n_2, n_4\}^3, \{n_1, n_3, n_4\}^3,$$

corresponded to k-number-resolving number as if there's one k-number-resolving set corresponded to neutrosophic k-number-resolving number so as neutrosophic cardinality is the determiner;

(*vi*) all k-number-resolving sets corresponded to k-number-resolving number are

$$\{n_1, n_2, n_3\}^3, \{n_1, n_2, n_4\}^3, \{n_1, n_3, n_4\}^3.$$

For given vertices n and n' if

$$d(s_1, n) \neq d(s_1, n'), d(s_2, n) \neq d(s_2, n'), \ldots, d(s_k, n) \neq d(s_k, n'),$$

then $s_1, s_2, \ldots, s_k$ k-number-resolve n and n'. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there are at least neutrosophic vertices $s_1, s_2, \ldots, s_k$ in S such that $s_1, s_2, \ldots, s_k$ k-number-resolve n and n', then the set of neutrosophic vertices, S is called k-number-resolving set. The minimum neutrosophic cardinality between all k-number-resolving sets is called neutrosophic k-number-resolving number and it's denoted by $\mathcal{N}_n^k(CMT_\sigma) = 3.9,\ k = \mathcal{O}(CMT_\sigma) - 1$; and corresponded to k-number-resolving sets are

$$\{n_1, n_3, n_4\}^3.$$

5 Open Problems

In this section, some questions and problems are proposed to give some avenues to pursue this study. The structures of the definitions and results give some ideas to make new settings which are eligible to extend and to create new study.

Notion concerning its k-number-resolving number and its neutrosophic k-number-resolving number are defined in neutrosophic graphs. Thus,

Question 5.1. *Is it possible to use other types of its k-number-resolving number and its neutrosophic k-number-resolving number?*

Question 5.2. *Are existed some connections amid different types of its k-number-resolving number and its neutrosophic k-number-resolving number in neutrosophic graphs?*

Question 5.3. *Is it possible to construct some classes of neutrosophic graphs which have "nice" behavior?*

Question 5.4. *Which mathematical notions do make an independent study to apply these types in neutrosophic graphs?*

Problem 5.5. *Which parameters are related to this parameter?*

Problem 5.6. *Which approaches do work to construct applications to create independent study?*

Problem 5.7. *Which approaches do work to construct definitions which use all definitions and the relations amid them instead of separate definitions to create independent study?*

6 Conclusion and Closing Remarks

In this section, concluding remarks and closing remarks are represented. The drawbacks of this article are illustrated. Some benefits and advantages of this study are highlighted.

This study uses two definitions concerning k-number-resolving number and neutrosophic k-number-resolving number arising from k-number-resolved vertices in neutrosophic graphs assigned to neutrosophic graphs. Minimum number of k-number-resolved vertices, is a number which is representative based on those vertices. Minimum neutrosophic number of k-number-resolved vertices corresponded to k-number-resolving set is called neutrosophic k-number-resolving number. The connections of vertices which aren't clarified by minimum number of edges amid them differ them from each other and put them in different categories to represent a number

Table 2. A Brief Overview about Advantages and Limitations of this Study

Advantages	Limitations
1. k-number-resolving Number of Model	1. Connections amid Classes
2. Neutrosophic k-number-resolving Number of Model	
3. Minimal k-number-resolving Sets	2. Study on Families
4. k-number-resolved Vertices amid all Vertices	
5. Acting on All Vertices	3. Same Models in Family

which is called k-number-resolving number and neutrosophic k-number-resolving number arising from k-number-resolved vertices in neutrosophic graphs assigned to neutrosophic graphs. Further studies could be about changes in the settings to compare these notions amid different settings of neutrosophic graphs theory. One way is finding some relations amid all definitions of notions to make sensible definitions. In Table (2), some limitations and advantages of this study are pointed out.

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