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Complete Connections Between Vertices in Neutrosophic Graphs

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Abstract

New setting is introduced to study total-dominating number and neutrosophic total-dominating number arising from total-dominated vertices in neutrosophic graphs assigned to neutrosophic graphs. Minimum number of total-dominated vertices, is a number which is representative based on those vertices. Minimum neutrosophic number of total-dominated vertices corresponded to total-dominating set is called neutrosophic total-dominating number. Forming sets from total-dominated vertices to figure out different types of number of vertices in the sets from total-dominated sets in the terms of minimum number of vertices to get minimum number to assign to neutrosophic graphs is key type of approach to have these notions namely total-dominating number and neutrosophic total-dominating number arising from total-dominated vertices in neutrosophic graphs assigned to neutrosophic graphs. Two numbers and one set are assigned to a neutrosophic graph, are obtained but now both settings lead to approach is on demand which is to compute and to find representatives of sets having smallest number of total-dominated vertices from different types of sets in the terms of minimum number and minimum neutrosophic number forming it to get minimum number to assign to a neutrosophic graph. Let $NTG : (V, E, \sigma, \mu)$ be a neutrosophic graph. Then for given vertices n and n' if $d(s, n) \neq d(s, n')$, then s total-dominates n and n' where s is the unique vertex and d is minimum number of edges amid two vertices. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there's only one neutrosophic vertex s in S such that s total-dominates n and n' , then the set of neutrosophic vertices, S is called total-dominating set. The minimum cardinality between all total-dominating sets is called total-dominating number and it's denoted by $\mathcal{T}(NTG)$; for given vertices n and n' if $d(s, n) \neq d(s, n')$, then s total-dominates n and n' where s is the unique vertex and d is minimum number of edges amid two vertices. Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertices n and n' in $V \setminus S$, there's only one neutrosophic vertex s in S such that s total-dominates n and n' , then the set of neutrosophic vertices, S is called total-dominating set. The minimum neutrosophic cardinality between all total-dominating sets is called neutrosophic total-dominating number and it's denoted by $\mathcal{T}_n(NTG)$. As concluding results, there are some statements, remarks, examples and clarifications about some classes of neutrosophic graphs namely path-neutrosophic graphs, cycle-neutrosophic graphs, complete-neutrosophic graphs, star-neutrosophic graphs, complete-bipartite-neutrosophic graphs,

complete-t-partite-neutrosophic graphs, and wheel-neutrosophic graphs. The clarifications are also presented in both sections “Setting of total-dominating number,” and “Setting of neutrosophic total-dominating number,” for introduced results and used classes. This approach facilitates identifying sets which form total-dominating number and neutrosophic total-dominating number arising from total-dominated vertices in neutrosophic graphs assigned to neutrosophic graphs. In both settings, some classes of well-known neutrosophic graphs are studied. Some clarifications for each result and each definition are provided. The cardinality of set of total-dominated vertices and neutrosophic cardinality of set of total-dominated vertices corresponded to total-dominating set have eligibility to define total-dominating number and neutrosophic total-dominating number but different types of set of total-dominated vertices to define total-dominating sets. Some results get more frameworks and more perspectives about these definitions. The way in that, different types of set of total-dominated vertices in the terms of minimum number to assign to neutrosophic graphs, opens the way to do some approaches. These notions are applied into neutrosophic graphs as individuals but not family of them as drawbacks for these notions. Finding special neutrosophic graphs which are well-known, is an open way to pursue this study. Neutrosophic total-dominating notion is applied to different settings and classes of neutrosophic graphs. Some problems are proposed to pursue this study. Basic familiarities with graph theory and neutrosophic graph theory are proposed for this article.

Keywords: Total-Dominating Number, Neutrosophic Total-Dominating Number, Classes of Neutrosophic Graphs

AMS Subject Classification: 05C17, 05C22, 05E45

1 Background

Fuzzy set in **Ref. [22]** by Zadeh (1965), intuitionistic fuzzy sets in **Ref. [5]** by Atanassov (1986), a first step to a theory of the intuitionistic fuzzy graphs in **Ref. [19]** by Shannon and Atanassov (1994), a unifying field in logics neutrosophy: neutrosophic probability, set and logic, rehoboth in **Ref. [20]** by Smarandache (1998), single-valued neutrosophic sets in **Ref. [21]** by Wang et al. (2010), single-valued neutrosophic graphs in **Ref. [9]** by Broumi et al. (2016), operations on single-valued neutrosophic graphs in **Ref. [1]** by Akram and Shahzadi (2017), neutrosophic soft graphs in **Ref. [18]** by Shah and Hussain (2016), bounds on the average and minimum attendance in preference-based activity scheduling in **Ref. [3]** by Aronshtam and Ilani (2022), investigating the recoverable robust single machine scheduling problem under interval uncertainty in **Ref. [8]** by Bold and Goerigk (2022), polyhedra associated with locating-dominating, open locating-dominating and locating total-dominating sets in graphs in **Ref. [2]** by G. Argiroffo et al. (2022), a Vizing-type result for semi-total domination in **Ref. [4]** by J. Asplund et al. (2020), total domination cover rubbing in **Ref. [6]** by R.A. Beeler et al. (2020), on the global total k-domination number of graphs in **Ref. [7]** by S. Bermudo et al. (2019), maker–breaker total domination game in **Ref. [10]** by V. Gledel et al. (2020), a new upper bound on the total domination number in graphs with minimum degree six in **Ref. [11]** by M.A. Henning, and A. Yeo (2021), effect of predomination and vertex removal on the game total domination number of a graph in **Ref. [16]** by V. Irsic (2019), hardness results of global total k-domination problem in graphs in **Ref. [17]** by B.S. Panda, and P. Goyal (2021), dimension and coloring alongside domination in neutrosophic hypergraphs in **Ref. [13]** by Henry Garrett (2022), three types of neutrosophic alliances based on connectedness and (strong) edges in **Ref. [15]** by Henry Garrett (2022), properties of SuperHyperGraph and neutrosophic SuperHyperGraph in **Ref. [14]** by Henry Garrett (2022), are studied. Also, some studies and researches about

neutrosophic graphs, are proposed as a book in **Ref. [12]** by Henry Garrett (2022).

In this section, I use two subsections to illustrate a perspective about the background of this study.

1.1 Motivation and Contributions

In this study, there's an idea which could be considered as a motivation.

Question 1.1. *Is it possible to use mixed versions of ideas concerning “total-dominating number”, “neutrosophic total-dominating number” and “Neutrosophic Graph” to define some notions which are applied to neutrosophic graphs?*

It's motivation to find notions to use in any classes of neutrosophic graphs. Real-world applications about time table and scheduling are another thoughts which lead to be considered as motivation. Having connection amid two vertices have key roles to assign total-dominating number and neutrosophic total-dominating number arising from total-dominated vertices in neutrosophic graphs assigned to neutrosophic graphs. Thus they're used to define new ideas which conclude to the structure of total-dominating number and neutrosophic total-dominating number arising from total-dominated vertices in neutrosophic graphs assigned to neutrosophic graphs. The concept of having smallest number of total-dominated vertices in the terms of crisp setting and in the terms of neutrosophic setting inspires us to study the behavior of all total-dominated vertices in the way that, some types of numbers, total-dominating number and neutrosophic total-dominating number arising from total-dominated vertices in neutrosophic graphs assigned to neutrosophic graphs, are the cases of study in the setting of individuals. In both settings, corresponded numbers conclude the discussion. Also, there are some avenues to extend these notions.

The framework of this study is as follows. In the beginning, I introduce basic definitions to clarify about preliminaries. In subsection “Preliminaries”, new notions of total-dominating number and neutrosophic total-dominating number arising from total-dominated vertices in neutrosophic graphs assigned to neutrosophic graphs, are highlighted, are introduced and are clarified as individuals. In section “Preliminaries”, minimum number of total-dominated vertices, is a number which is representative based on those vertices, have the key role in this way. General results are obtained and also, the results about the basic notions of total-dominating number and neutrosophic total-dominating number arising from total-dominated vertices in neutrosophic graphs assigned to neutrosophic graphs, are elicited. Some classes of neutrosophic graphs are studied in the terms of total-dominating number and neutrosophic total-dominating number arising from total-dominated vertices in neutrosophic graphs assigned to neutrosophic graphs, in section “Setting of total-dominating number,” as individuals. In section “Setting of total-dominating number,” total-dominating number is applied into individuals. As concluding results, there are some statements, remarks, examples and clarifications about some classes of neutrosophic graphs namely path-neutrosophic graphs, cycle-neutrosophic graphs, complete-neutrosophic graphs, star-neutrosophic graphs, complete-bipartite-neutrosophic graphs, complete-t-partite-neutrosophic graphs, and wheel-neutrosophic graphs. The clarifications are also presented in both sections “Setting of total-dominating number,” and “Setting of neutrosophic total-dominating number,” for introduced results and used classes. In section “Applications in Time Table and Scheduling”, two applications are posed for quasi-complete and complete notions, namely complete-neutrosophic graphs and complete-t-partite-neutrosophic graphs concerning time table and scheduling when the suspicions are about choosing some subjects and the mentioned models are considered as individual. In section “Open Problems”, some problems and questions for further studies are proposed. In section “Conclusion and Closing Remarks”, gentle discussion about results and applications is

featured. In section “Conclusion and Closing Remarks”, a brief overview concerning advantages and limitations of this study alongside conclusions is formed.

1.2 Preliminaries

In this subsection, basic material which is used in this article, is presented. Also, new ideas and their clarifications are elicited.

Basic idea is about the model which is used. First definition introduces basic model.

Definition 1.2. (Graph).

$G = (V, E)$ is called a **graph** if V is a set of objects and E is a subset of $V \times V$ (E is a set of 2-subsets of V) where V is called **vertex set** and E is called **edge set**. Every two vertices have been corresponded to at most one edge.

Neutrosophic graph is the foundation of results in this paper which is defined as follows. Also, some related notions are demonstrated.

Definition 1.3. (Neutrosophic Graph And Its Special Case).

$NTG = (V, E, \sigma = (\sigma_1, \sigma_2, \sigma_3), \mu = (\mu_1, \mu_2, \mu_3))$ is called a **neutrosophic graph** if it's graph, $\sigma_i : V \rightarrow [0, 1]$, and $\mu_i : E \rightarrow [0, 1]$. We add one condition on it and we use **special case** of neutrosophic graph but with same name. The added condition is as follows, for every $v_i v_j \in E$,

$$\mu(v_i v_j) \leq \sigma(v_i) \wedge \sigma(v_j).$$

(i) : σ is called **neutrosophic vertex set**.

(ii) : μ is called **neutrosophic edge set**.

(iii) : $|V|$ is called **order** of NTG and it's denoted by $\mathcal{O}(NTG)$.

(iv) : $\sum_{v \in V} \sum_{i=1}^3 \sigma_i(v)$ is called **neutrosophic order** of NTG and it's denoted by $\mathcal{O}_n(NTG)$.

(v) : $|E|$ is called **size** of NTG and it's denoted by $\mathcal{S}(NTG)$.

(vi) : $\sum_{e \in E} \sum_{i=1}^3 \mu_i(e)$ is called **neutrosophic size** of NTG and it's denoted by $\mathcal{S}_n(NTG)$.

Some classes of well-known neutrosophic graphs are defined. These classes of neutrosophic graphs are used to form this study and the most results are about them.

Definition 1.4. Let $NTG : (V, E, \sigma, \mu)$ be a neutrosophic graph. Then

(i) : a sequence of consecutive vertices $P : x_0, x_1, \dots, x_{\mathcal{O}(NTG)}$ is called **path** where $x_i x_{i+1} \in E$, $i = 0, 1, \dots, \mathcal{O}(NTG) - 1$;

(ii) : **strength** of path $P : x_0, x_1, \dots, x_{\mathcal{O}(NTG)}$ is $\bigwedge_{i=0, \dots, \mathcal{O}(NTG)-1} \mu(x_i x_{i+1})$;

(iii) : **connectedness** amid vertices x_0 and x_t is

$$\mu^\infty(x_0, x_t) = \bigvee_{P: x_0, x_1, \dots, x_t} \bigwedge_{i=0, \dots, t-1} \mu(x_i x_{i+1});$$

(iv) : a sequence of consecutive vertices $P : x_0, x_1, \dots, x_{\mathcal{O}(NTG)}, x_0$ is called **cycle** where $x_i x_{i+1} \in E$, $i = 0, 1, \dots, \mathcal{O}(NTG) - 1$, $x_{\mathcal{O}(NTG)} x_0 \in E$ and there are two edges xy and uv such that $\mu(xy) = \mu(uv) = \bigwedge_{i=0, 1, \dots, n-1} \mu(v_i v_{i+1})$;

(v) : it's **t-partite** where V is partitioned to t parts, $V_1^{s_1}, V_2^{s_2}, \dots, V_t^{s_t}$ and the edge xy implies $x \in V_i^{s_i}$ and $y \in V_j^{s_j}$ where $i \neq j$. If it's complete, then it's denoted by $K_{\sigma_1, \sigma_2, \dots, \sigma_t}$ where σ_i is σ on $V_i^{s_i}$ instead V which mean $x \notin V_i$ induces $\sigma_i(x) = 0$. Also, $|V_j^{s_j}| = s_j$;

(vi) : t-partite is **complete bipartite** if $t = 2$, and it's denoted by K_{σ_1, σ_2} ;

(vii) : complete bipartite is **star** if $|V_1| = 1$, and it's denoted by S_{1, σ_2} ;

(viii) : a vertex in V is **center** if the vertex joins to all vertices of a cycle. Then it's **wheel** and it's denoted by W_{1, σ_2} ;

(ix) : it's **complete** where $\forall uv \in V, \mu(uv) = \sigma(u) \wedge \sigma(v)$;

(x) : it's **strong** where $\forall uv \in E, \mu(uv) = \sigma(u) \wedge \sigma(v)$.

To make them concrete, I bring preliminaries of this article in two upcoming definitions in other ways.

Definition 1.5. (Neutrosophic Graph And Its Special Case).

$NTG = (V, E, \sigma = (\sigma_1, \sigma_2, \sigma_3), \mu = (\mu_1, \mu_2, \mu_3))$ is called a **neutrosophic graph** if it's graph, $\sigma_i : V \rightarrow [0, 1]$, and $\mu_i : E \rightarrow [0, 1]$. We add one condition on it and we use **special case** of neutrosophic graph but with same name. The added condition is as follows, for every $v_i v_j \in E$,

$$\mu(v_i v_j) \leq \sigma(v_i) \wedge \sigma(v_j).$$

$|V|$ is called **order** of NTG and it's denoted by $\mathcal{O}(NTG)$. $\sum_{v \in V} \sigma(v)$ is called **neutrosophic order** of NTG and it's denoted by $\mathcal{O}_n(NTG)$.

Definition 1.6. Let $NTG : (V, E, \sigma, \mu)$ be a neutrosophic graph. Then it's **complete** and denoted by CMT_σ if $\forall x, y \in V, xy \in E$ and $\mu(xy) = \sigma(x) \wedge \sigma(y)$; a sequence of consecutive vertices $P : x_0, x_1, \dots, x_{\mathcal{O}(NTG)}$ is called **path** and it's denoted by PTH where $x_i x_{i+1} \in E, i = 0, 1, \dots, n-1$; a sequence of consecutive vertices $P : x_0, x_1, \dots, x_{\mathcal{O}(NTG)}, x_0$ is called **cycle** and denoted by CYC where $x_i x_{i+1} \in E, i = 0, 1, \dots, n-1, x_{\mathcal{O}(NTG)} x_0 \in E$ and there are two edges xy and uv such that $\mu(xy) = \mu(uv) = \bigwedge_{i=0,1,\dots,n-1} \mu(v_i v_{i+1})$; it's **t-partite** where V is partitioned to t parts, $V_1^{s_1}, V_2^{s_2}, \dots, V_t^{s_t}$ and the edge xy implies $x \in V_i^{s_i}$ and $y \in V_j^{s_j}$ where $i \neq j$. If it's **complete**, then it's denoted by $CMT_{\sigma_1, \sigma_2, \dots, \sigma_t}$ where σ_i is σ on $V_i^{s_i}$ instead V which mean $x \notin V_i$ induces $\sigma_i(x) = 0$. Also, $|V_j^{s_j}| = s_j$; t-partite is **complete bipartite** if $t = 2$, and it's denoted by CMT_{σ_1, σ_2} ; complete bipartite is **star** if $|V_1| = 1$, and it's denoted by STR_{1, σ_2} ; a vertex in V is **center** if the vertex joins to all vertices of a cycle. Then it's **wheel** and it's denoted by WHL_{1, σ_2} .

Remark 1.7. Using notations which is mixed with literatures, are reviewed.

1. $NTG = (V, E, \sigma = (\sigma_1, \sigma_2, \sigma_3), \mu = (\mu_1, \mu_2, \mu_3)), \mathcal{O}(NTG)$, and $\mathcal{O}_n(NTG)$;

2. $CMT_\sigma, PTH, CYC, STR_{1, \sigma_2}, CMT_{\sigma_1, \sigma_2}, CMT_{\sigma_1, \sigma_2, \dots, \sigma_t}$, and WHL_{1, σ_2} .

Definition 1.8. (total-dominating numbers).

Let $NTG : (V, E, \sigma, \mu)$ be a neutrosophic graph. Then

(i) for given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called **total-dominating set**. The minimum cardinality between all total-dominating sets is called **total-dominating number** and it's denoted by $\mathcal{T}(NTG)$;

(ii) for given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called **total-dominating set**. The minimum neutrosophic cardinality between all total-dominating sets is called **neutrosophic total-dominating number** and it's denoted by $\mathcal{T}_n(NTG)$.

For convenient usages, the word neutrosophic which is used in previous definition, won't be used, usually.

Proposition 1.9. Let $NTG : (V, E, \sigma, \mu)$ be a neutrosophic graph. Then $|S| \geq 2$.

In next part, clarifications about main definition are given. To avoid confusion and for convenient usages, examples are usually used after every part and names are used in the way that, abbreviation, simplicity, and summarization are the matters of mind.

Example 1.10. In Figure (1), a complete-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows.

- (i) For given neutrosophic vertex, s , there's an edge with other vertices;
- (ii) in the setting of complete, a vertex of dominating set corresponded to dominating number dominates as if it doesn't total-dominate since a vertex couldn't dominate itself;
- (iii) all total-dominating sets corresponded to total-dominating number are

$$\begin{aligned} &\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ &\{n_2, n_3\}, \{n_2, n_4\}, \{n_3, n_4\}. \end{aligned}$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum cardinality between all total-dominating sets is called total-dominating number and it's denoted by $\mathcal{T}(NTG) = 2$ and corresponded to total-dominating sets are

$$\begin{aligned} &\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ &\{n_2, n_3\}, \{n_2, n_4\}, \{n_3, n_4\}; \end{aligned}$$

- (iv) there are eleven total-dominating sets

$$\begin{aligned} &\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ &\{n_2, n_3\}, \{n_2, n_4\}, \{n_3, n_4\}, \\ &\{n_1, n_2, n_3\}, \{n_1, n_2, n_4\}, \{n_1, n_3, n_4\}, \\ &\{n_2, n_3, n_4\}, \{n_1, n_2, n_3, n_4\}, \end{aligned}$$

as if it's possible to have one of them as a set corresponded to neutrosophic total-dominating number so as neutrosophic cardinality is characteristic;

- (v) there are six total-dominating sets

$$\begin{aligned} &\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ &\{n_2, n_3\}, \{n_2, n_4\}, \{n_3, n_4\}, \end{aligned}$$

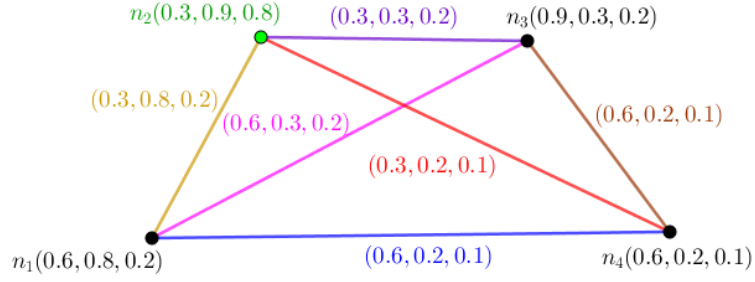


Figure 1. A Neutrosophic Graph in the Viewpoint of its total-dominating number and its neutrosophic total-dominating number.

corresponded to total-dominating number as if there's one total-dominating set
 corresponded to neutrosophic total-dominating number so as neutrosophic
 cardinality is the determiner;

(vi) all total-dominating sets corresponded to total-dominating number are

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ \{n_2, n_3\}, \{n_2, n_4\}, \{n_3, n_4\}.$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of
 neutrosophic vertices [a vertex alongside triple pair of its values is called
 neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a
 neutrosophic vertex s in S such that s total-dominates n , then the set of
 neutrosophic vertices, S is called total-dominating set. The minimum
 neutrosophic cardinality between all total-dominating sets is called neutrosophic
 total-dominating number and it's denoted by $\mathcal{T}_n(NTG) = 2.3$ and corresponded
 to neutrosophic total-dominating sets are

$$\{n_3, n_4\}.$$

2 Setting of total-dominating number

In this section, I provide some results in the setting of total-dominating number. Some
 classes of neutrosophic graphs are chosen. Complete-neutrosophic graph,
 path-neutrosophic graph, cycle-neutrosophic graph, star-neutrosophic graph,
 bipartite-neutrosophic graph, t-partite-neutrosophic graph, and wheel-neutrosophic
 graph, are both of cases of study and classes which the results are about them.

Proposition 2.1. *Let $NTG : (V, E, \sigma, \mu)$ be a complete-neutrosophic graph. Then*

$$\mathcal{T}(CMT_\sigma) = 2.$$

Proof. Suppose $CMT_\sigma : (V, E, \sigma, \mu)$ is a complete-neutrosophic graph. By
 $CMT_\sigma : (V, E, \sigma, \mu)$ is a complete-neutrosophic graph, all vertices are connected to each
 other. So there's one edge between two vertices. In the setting of complete, a vertex of
 dominating set corresponded to dominating number dominates as if it doesn't
 total-dominate since a vertex couldn't dominate itself. All total-dominating sets

corresponded to total-dominating number are

$$\begin{aligned} & \{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \dots, \{n_1, n_{\mathcal{O}(CMT_\sigma)-2}\}, \{n_1, n_{\mathcal{O}(CMT_\sigma)-1}\}, \{n_1, n_{\mathcal{O}(CMT_\sigma)}\} \\ & \{n_2, n_3\}, \{n_2, n_4\}, \{n_2, n_5\}, \dots, \{n_2, n_{\mathcal{O}(CMT_\sigma)-2}\}, \{n_2, n_{\mathcal{O}(CMT_\sigma)-1}\}, \{n_2, n_{\mathcal{O}(CMT_\sigma)}\} \\ & \{n_3, n_4\}, \{n_3, n_5\}, \{n_3, n_6\}, \dots, \{n_3, n_{\mathcal{O}(CMT_\sigma)-2}\}, \{n_3, n_{\mathcal{O}(CMT_\sigma)-1}\}, \{n_3, n_{\mathcal{O}(CMT_\sigma)}\} \\ & \dots \\ & \{n_{\mathcal{O}(CMT_\sigma)-3}, n_{\mathcal{O}(CMT_\sigma)-2}\}, \{n_{\mathcal{O}(CMT_\sigma)-3}, n_{\mathcal{O}(CMT_\sigma)-1}\}, \{n_{\mathcal{O}(CMT_\sigma)-3}, n_{\mathcal{O}(CMT_\sigma)}\} \\ & \{n_{\mathcal{O}(CMT_\sigma)-2}, n_{\mathcal{O}(CMT_\sigma)-1}\}, \{n_{\mathcal{O}(CMT_\sigma)-2}, n_{\mathcal{O}(CMT_\sigma)}\} \\ & \{n_{\mathcal{O}(CMT_\sigma)-1}, n_{\mathcal{O}(CMT_\sigma)}\} \end{aligned}$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum cardinality between all total-dominating sets is called total-dominating number and it's denoted by

$$\mathcal{T}(NTG) = 2$$

and corresponded to total-dominating sets are

$$\begin{aligned} & \{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \dots, \{n_1, n_{\mathcal{O}(CMT_\sigma)-2}\}, \{n_1, n_{\mathcal{O}(CMT_\sigma)-1}\}, \{n_1, n_{\mathcal{O}(CMT_\sigma)}\} \\ & \{n_2, n_3\}, \{n_2, n_4\}, \{n_2, n_5\}, \dots, \{n_2, n_{\mathcal{O}(CMT_\sigma)-2}\}, \{n_2, n_{\mathcal{O}(CMT_\sigma)-1}\}, \{n_2, n_{\mathcal{O}(CMT_\sigma)}\} \\ & \{n_3, n_4\}, \{n_3, n_5\}, \{n_3, n_6\}, \dots, \{n_3, n_{\mathcal{O}(CMT_\sigma)-2}\}, \{n_3, n_{\mathcal{O}(CMT_\sigma)-1}\}, \{n_3, n_{\mathcal{O}(CMT_\sigma)}\} \\ & \dots \\ & \{n_{\mathcal{O}(CMT_\sigma)-3}, n_{\mathcal{O}(CMT_\sigma)-2}\}, \{n_{\mathcal{O}(CMT_\sigma)-3}, n_{\mathcal{O}(CMT_\sigma)-1}\}, \{n_{\mathcal{O}(CMT_\sigma)-3}, n_{\mathcal{O}(CMT_\sigma)}\} \\ & \{n_{\mathcal{O}(CMT_\sigma)-2}, n_{\mathcal{O}(CMT_\sigma)-1}\}, \{n_{\mathcal{O}(CMT_\sigma)-2}, n_{\mathcal{O}(CMT_\sigma)}\} \\ & \{n_{\mathcal{O}(CMT_\sigma)-1}, n_{\mathcal{O}(CMT_\sigma)}\} \end{aligned}$$

Thus

$$\mathcal{T}(CMT_\sigma) = 2.$$

□ 204

Proposition 2.2. Let $NTG : (V, E, \sigma, \mu)$ be a complete-neutrosophic graph. Then total-dominating number isn't equal to dominating number. 205

Proposition 2.3. Let $NTG : (V, E, \sigma, \mu)$ be a complete-neutrosophic graph. Then the number of total-dominating sets corresponded to total-dominating number is equal to $\mathcal{O}(CMT_\sigma)$ choose two. 207
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Proposition 2.4. Let $NTG : (V, E, \sigma, \mu)$ be a complete-neutrosophic graph. Then the number of total-dominating sets is equal to $\mathcal{O}(CMT_\sigma)$ choose two plus $\mathcal{O}(CMT_\sigma)$ choose three plus one. 210
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The clarifications about results are in progress as follows. A complete-neutrosophic graph is related to previous result and it's studied to apply the definitions on it. To make it more clear, next part gives one special case to apply definitions and results on it. Some items are devised to make more sense about new notions. A complete-neutrosophic graph is related to previous result and it's studied to apply the definitions on it, too. 213
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Example 2.5. In Figure (2), a complete-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows. 219
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- (i) For given neutrosophic vertex, s , there's an edge with other vertices; 221
- (ii) in the setting of complete, a vertex of dominating set corresponded to dominating number dominates as if it doesn't total-dominate since a vertex couldn't dominate itself; 222
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- (iii) all total-dominating sets corresponded to total-dominating number are 225

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ \{n_2, n_3\}, \{n_2, n_4\}, \{n_3, n_4\}.$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum cardinality between all total-dominating sets is called total-dominating number and it's denoted by $\mathcal{T}(CMT_\sigma) = 2$ and corresponded to total-dominating sets are 226
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$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ \{n_2, n_3\}, \{n_2, n_4\}, \{n_3, n_4\};$$

- (iv) there are eleven total-dominating sets 233

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ \{n_2, n_3\}, \{n_2, n_4\}, \{n_3, n_4\}, \\ \{n_1, n_2, n_3\}, \{n_1, n_2, n_4\}, \{n_1, n_3, n_4\}, \\ \{n_2, n_3, n_4\}, \{n_1, n_2, n_3, n_4\},$$

as if it's possible to have one of them as a set corresponded to neutrosophic total-dominating number so as neutrosophic cardinality is characteristic; 234
235

- (v) there are six total-dominating sets 236

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ \{n_2, n_3\}, \{n_2, n_4\}, \{n_3, n_4\},$$

corresponded to total-dominating number as if there's one total-dominating set corresponded to neutrosophic total-dominating number so as neutrosophic cardinality is the determiner; 237
238
239

- (vi) all total-dominating sets corresponded to total-dominating number are 240

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ \{n_2, n_3\}, \{n_2, n_4\}, \{n_3, n_4\}.$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum neutrosophic cardinality between all total-dominating sets is called neutrosophic total-dominating number and it's denoted by $\mathcal{T}_n(CMT_\sigma) = 2.3$ and corresponded to neutrosophic total-dominating sets are 241
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$$\{n_3, n_4\}.$$

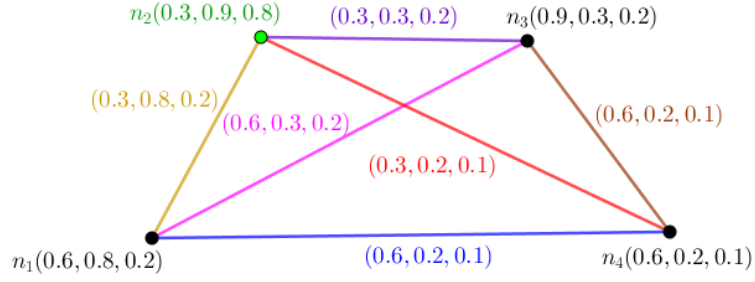


Figure 2. A Neutrosophic Graph in the Viewpoint of its total-dominating number and its neutrosophic total-dominating number.

Another class of neutrosophic graphs is addressed to path-neutrosophic graph. 249

Proposition 2.6. Let $NTG : (V, E, \sigma, \mu)$ be a path-neutrosophic graph. Then

$$\mathcal{T}(PTH) = (|V| \lceil \frac{\mathcal{O}(PTH)}{2} \rceil (|V| + 1)).$$

Proof. Suppose $PTH : (V, E, \sigma, \mu)$ is a path-neutrosophic graph. Let $n_1, n_2, \dots, n_{\mathcal{O}(PTH)}$ be a path-neutrosophic graph. For given two vertices, x and y , there's one path from x to y . In the setting of path, a vertex of dominating set corresponded to dominating number dominates as if it doesn't total-dominate since a vertex couldn't dominate itself. Thus two neighbors are necessary in S . All total-dominating sets corresponded to total-dominating number are 250
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254
255

$$\begin{aligned} & \{n_1, n_2, n_5, n_6, n_9, n_{10} \dots\}, \{n_2, n_3, n_6, n_7, n_{10}, n_{11} \dots\}, \{n_2, n_3, n_4, n_7, n_8, \dots\}, \\ & \dots \\ & \{\dots, n_{\mathcal{O}(PTH)-10}, n_{\mathcal{O}(PTH)-9}, n_{\mathcal{O}(PTH)-6}, n_{\mathcal{O}(PTH)-5}, n_{\mathcal{O}(PTH)-2}, n_{\mathcal{O}(PTH)-1}\} \\ & \{\dots, n_{\mathcal{O}(PTH)-9}, n_{\mathcal{O}(PTH)-8}, n_{\mathcal{O}(PTH)-5}, n_{\mathcal{O}(PTH)-4}, n_{\mathcal{O}(PTH)-1}, n_{\mathcal{O}(PTH)}\}. \end{aligned}$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum cardinality between all total-dominating sets is called total-dominating number and it's denoted by

$$\mathcal{T}(PTH) = (|V| \lceil \frac{\mathcal{O}(PTH)}{2} \rceil (|V| + 1))$$

and corresponded to total-dominating sets are 256

$$\begin{aligned} & \{n_1, n_2, n_5, n_6, n_9, n_{10} \dots\}, \{n_2, n_3, n_6, n_7, n_{10}, n_{11} \dots\}, \{n_2, n_3, n_4, n_7, n_8, \dots\}, \\ & \dots \\ & \{\dots, n_{\mathcal{O}(PTH)-10}, n_{\mathcal{O}(PTH)-9}, n_{\mathcal{O}(PTH)-6}, n_{\mathcal{O}(PTH)-5}, n_{\mathcal{O}(PTH)-2}, n_{\mathcal{O}(PTH)-1}\} \\ & \{\dots, n_{\mathcal{O}(PTH)-9}, n_{\mathcal{O}(PTH)-8}, n_{\mathcal{O}(PTH)-5}, n_{\mathcal{O}(PTH)-4}, n_{\mathcal{O}(PTH)-1}, n_{\mathcal{O}(PTH)}\}. \end{aligned}$$

Thus

$$\mathcal{T}(PTH) = (|V| \lceil \frac{\mathcal{O}(PTH)}{2} \rceil (|V| + 1)).$$

□ 257

Proposition 2.7. Let $NTG : (V, E, \sigma, \mu)$ be a path-neutrosophic graph. Then total-dominating number isn't equal to dominating number.

Example 2.8. There are two sections for clarifications.

(a) In Figure (3), an odd-path-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows.

- (i) For given neutrosophic vertex, s , there's only one path with other vertices;
- (ii) in the setting of path, a vertex of dominating set corresponded to dominating number dominates as if it doesn't total-dominate since a vertex couldn't dominate itself. Thus two neighbors are necessary in S ;
- (iii) all total-dominating sets corresponded to total-dominating number are

$$\{n_2, n_3, n_4\},$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum cardinality between all total-dominating sets is called total-dominating number and it's denoted by $\mathcal{T}(PTH) = 3$ and corresponded to total-dominating sets are

$$\{n_2, n_3, n_4\};$$

(iv) there are five total-dominating sets

$$\{n_2, n_3, n_4\}, \{n_1, n_2, n_3, n_4\}, \{n_5, n_2, n_3, n_4\}, \\ \{n_1, n_2, n_3, n_4, n_5\}, \{n_1, n_2, n_4, n_5\},$$

as if it's possible to have one of them as a set corresponded to neutrosophic total-dominating number so as neutrosophic cardinality is characteristic;

(v) there's one total-dominating set

$$\{n_2, n_3, n_4\},$$

corresponded to total-dominating number as if there's one total-dominating set corresponded to neutrosophic total-dominating number so as neutrosophic cardinality is the determiner;

(vi) all total-dominating sets corresponded to total-dominating number are

$$\{n_2, n_3, n_4\},$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum cardinality between all total-dominating sets is called total-dominating number and it's denoted by $\mathcal{T}(PTH) = 3.7$ and corresponded to total-dominating sets are

$$\{n_2, n_3, n_4\}.$$

(b) In Figure (4), an even-path-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows. 292
293

- (i) For given neutrosophic vertex, s , there's only one path with other vertices; 294
- (ii) in the setting of path, a vertex of dominating set corresponded to dominating number dominates as if it doesn't total-dominate since a vertex couldn't dominate itself. Thus two neighbors are necessary in S ; 295
296
297
- (iii) all total-dominating sets corresponded to total-dominating number are 298

$$\{n_1, n_2, n_5, n_6\}, \{n_2, n_3, n_5, n_6\}, \{n_2, n_3, n_4, n_5\},$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum cardinality between all total-dominating sets is called total-dominating number and it's denoted by $\mathcal{T}(PTH) = 4$ and corresponded to total-dominating sets are 299
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301
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$$\{n_1, n_2, n_5, n_6\}, \{n_2, n_3, n_5, n_6\}, \{n_2, n_3, n_4, n_5\};$$

- (iv) there are eight total-dominating sets 307

$$\begin{aligned} &\{n_1, n_2, n_5, n_6\}, \{n_2, n_3, n_5, n_6\}, \{n_2, n_3, n_4, n_5\}, \\ &\{n_1, n_2, n_5, n_6, n_3\}, \{n_1, n_2, n_5, n_6, n_4\}, \{n_1, n_2, n_5, n_6, n_4, n_3\}, \\ &\{n_2, n_3, n_5, n_6, n_4\}, \{n_2, n_3, n_4, n_5, n_1\}, \end{aligned}$$

as if it's possible to have one of them as a set corresponded to neutrosophic total-dominating number so as neutrosophic cardinality is characteristic; 308
309

- (v) there are three total-dominating sets 310

$$\{n_1, n_2, n_5, n_6\}, \{n_2, n_3, n_5, n_6\}, \{n_2, n_3, n_4, n_5\},$$

corresponded to total-dominating number as if there's one total-dominating set corresponded to neutrosophic total-dominating number so as neutrosophic cardinality is the determiner; 311
312
313

- (vi) all total-dominating sets corresponded to total-dominating number are 314

$$\{n_1, n_2, n_5, n_6\}, \{n_2, n_3, n_5, n_6\}, \{n_2, n_3, n_4, n_5\},$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum neutrosophic cardinality between all total-dominating sets is called neutrosophic total-dominating number and it's denoted by $\mathcal{T}_n(PTH) = 6$ and corresponded to total-dominating sets are 315
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$$\{n_2, n_3, n_4, n_5\}.$$

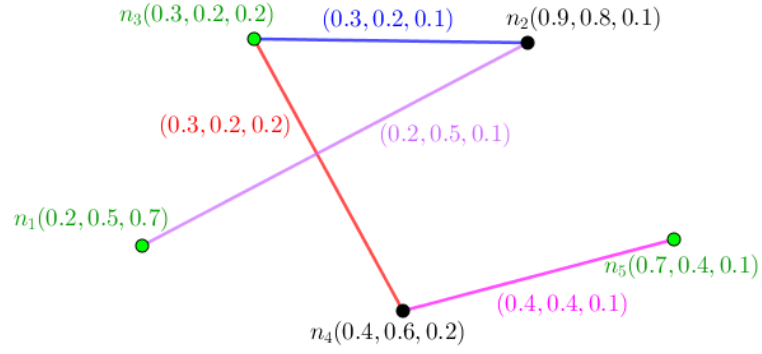


Figure 3. A Neutrosophic Graph in the Viewpoint of its total-dominating number and its neutrosophic total-dominating number.

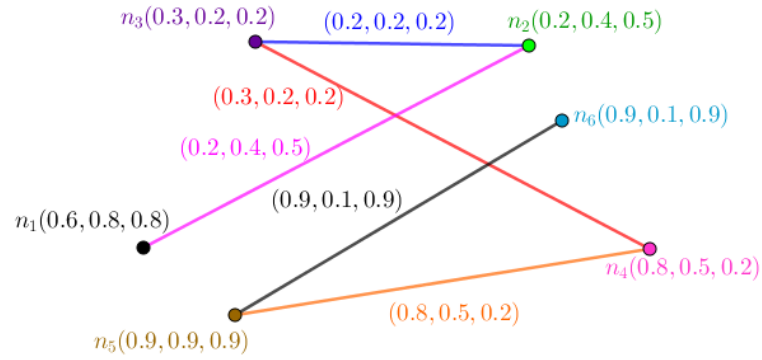


Figure 4. A Neutrosophic Graph in the Viewpoint of its total-dominating number and its neutrosophic total-dominating number.

Proposition 2.9. Let $NTG : (V, E, \sigma, \mu)$ be a cycle-neutrosophic graph where $\mathcal{O}(CYC) \geq 3$. Then

$$\mathcal{T}(CYC) = (\lfloor \lceil \frac{\mathcal{O}(CYC)}{2} \rceil \rfloor)(+1).$$

Proof. Suppose $CYC : (V, E, \sigma, \mu)$ is a cycle-neutrosophic graph. For given two vertices, x and y , there are only two paths with distinct edges from x to y . Let

$$x_1, x_2, \dots, x_{\mathcal{O}(CYC)-1}, x_{\mathcal{O}(CYC)}, x_1$$

be a cycle-neutrosophic graph $CYC : (V, E, \sigma, \mu)$. In the setting of cycle, a vertex of dominating set corresponded to dominating number dominates as if it doesn't total-dominate since a vertex couldn't dominate itself. Thus two neighbors are necessary in S . All total-dominating sets corresponded to total-dominating number are

$$\begin{aligned} & \{n_1, n_2, n_5, n_6, n_9, n_{10} \dots\}, \{n_2, n_3, n_6, n_7, n_{10}, n_{11} \dots\}, \{n_2, n_3, n_4, n_7, n_8, \dots\}, \\ & \dots \\ & \{\dots, n_{\mathcal{O}(CYC)-10}, n_{\mathcal{O}(CYC)-9}, n_{\mathcal{O}(CYC)-6}, n_{\mathcal{O}(CYC)-5}, n_{\mathcal{O}(CYC)-2}, n_{\mathcal{O}(CYC)-1}\} \\ & \{\dots, n_{\mathcal{O}(CYC)-9}, n_{\mathcal{O}(CYC)-8}, n_{\mathcal{O}(CYC)-5}, n_{\mathcal{O}(CYC)-4}, n_{\mathcal{O}(CYC)-1}, n_{\mathcal{O}(CYC)}\}. \end{aligned}$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum cardinality between all total-dominating sets is called total-dominating number and it's denoted by

$$\mathcal{T}(CYC) = (\lfloor \lceil \frac{\mathcal{O}(CYC)}{2} \rceil \rfloor)(+1)$$

and corresponded to total-dominating sets are

$$\begin{aligned} & \{n_1, n_2, n_5, n_6, n_9, n_{10} \dots\}, \{n_2, n_3, n_6, n_7, n_{10}, n_{11} \dots\}, \{n_2, n_3, n_4, n_7, n_8, \dots\}, \\ & \dots \\ & \{\dots, n_{\mathcal{O}(CYC)-10}, n_{\mathcal{O}(CYC)-9}, n_{\mathcal{O}(CYC)-6}, n_{\mathcal{O}(CYC)-5}, n_{\mathcal{O}(CYC)-2}, n_{\mathcal{O}(CYC)-1}\} \\ & \{\dots, n_{\mathcal{O}(CYC)-9}, n_{\mathcal{O}(CYC)-8}, n_{\mathcal{O}(CYC)-5}, n_{\mathcal{O}(CYC)-4}, n_{\mathcal{O}(CYC)-1}, n_{\mathcal{O}(CYC)}\}. \end{aligned}$$

Thus

$$\mathcal{T}(CYC) = (\lfloor \lceil \frac{\mathcal{O}(CYC)}{2} \rceil \rfloor)(+1).$$

□ 328

Proposition 2.10. Let $NTG : (V, E, \sigma, \mu)$ be a cycle-neutrosophic graph. Then total-dominating number isn't equal to dominating number.

The clarifications about results are in progress as follows. An odd-cycle-neutrosophic graph is related to previous result and it's studied to apply the definitions on it. To make it more clear, next part gives one special case to apply definitions and results on it. Some items are devised to make more sense about new notions. An even-cycle-neutrosophic graph is related to previous result and it's studied to apply the definitions on it, too.

Example 2.11. There are two sections for clarifications.

(a) In Figure (5), an even-cycle-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows.

- (i) For given neutrosophic vertex, s , there are only two paths with other vertices;
- (ii) in the setting of cycle, a vertex of dominating set corresponded to dominating number dominates as if it doesn't total-dominate since a vertex couldn't dominate itself. Thus two neighbors are necessary in S ;
- (iii) all total-dominating sets corresponded to total-dominating number are

$$\begin{aligned} &\{n_1, n_2, n_5, n_6\}, \{n_2, n_3, n_6, n_1\}, \{n_3, n_4, n_1, n_2\}, \\ &\{n_3, n_4, n_5, n_6\}, \{n_4, n_5, n_2, n_3\}, \{n_4, n_5, n_1, n_6\}, \\ &\{n_1, n_2, n_4, n_5\}, \{n_2, n_3, n_5, n_6\}, \{n_3, n_4, n_6, n_1\}, \end{aligned}$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum cardinality between all total-dominating sets is called total-dominating number and it's denoted by $\mathcal{T}(CYC) = 4$ and corresponded to total-dominating sets are

$$\begin{aligned} &\{n_1, n_2, n_5, n_6\}, \{n_2, n_3, n_6, n_1\}, \{n_3, n_4, n_1, n_2\}, \\ &\{n_3, n_4, n_5, n_6\}, \{n_4, n_5, n_2, n_3\}, \{n_4, n_5, n_1, n_6\}, \\ &\{n_1, n_2, n_4, n_5\}, \{n_2, n_3, n_5, n_6\}, \{n_3, n_4, n_6, n_1\}; \end{aligned}$$

- (iv) there are sixteen total-dominating sets

$$\begin{aligned} &\{n_1, n_2, n_5, n_6\}, \{n_2, n_3, n_6, n_1\}, \{n_3, n_4, n_1, n_2\}, \\ &\{n_3, n_4, n_5, n_6\}, \{n_4, n_5, n_2, n_3\}, \{n_4, n_5, n_1, n_6\}, \\ &\{n_1, n_2, n_4, n_5\}, \{n_2, n_3, n_5, n_6\}, \{n_3, n_4, n_6, n_1\}, \\ &\{n_1, n_2, n_3, n_5, n_6\}, \{n_1, n_2, n_4, n_5, n_6\}, \{n_1, n_2, n_3, n_4, n_5, n_6\}, \\ &\{n_6, n_2, n_3, n_4, n_5\}, \{n_6, n_1, n_3, n_4, n_5\}, \{n_6, n_1, n_2, n_3, n_4\}, \\ &\{n_5, n_1, n_2, n_3, n_4\}, \end{aligned}$$

as if it's possible to have one of them as a set corresponded to neutrosophic total-dominating number so as neutrosophic cardinality is characteristic;

- (v) there are nine total-dominating sets

$$\begin{aligned} &\{n_1, n_2, n_5, n_6\}, \{n_2, n_3, n_6, n_1\}, \{n_3, n_4, n_1, n_2\}, \\ &\{n_3, n_4, n_5, n_6\}, \{n_4, n_5, n_2, n_3\}, \{n_4, n_5, n_1, n_6\}, \\ &\{n_1, n_2, n_4, n_5\}, \{n_2, n_3, n_5, n_6\}, \{n_3, n_4, n_6, n_1\}, \end{aligned}$$

corresponded to total-dominating number as if there's one total-dominating set corresponded to neutrosophic total-dominating number so as neutrosophic cardinality is the determiner;

- (vi) all total-dominating sets corresponded to total-dominating number are

$$\begin{aligned} &\{n_1, n_2, n_5, n_6\}, \{n_2, n_3, n_6, n_1\}, \{n_3, n_4, n_1, n_2\}, \\ &\{n_3, n_4, n_5, n_6\}, \{n_4, n_5, n_2, n_3\}, \{n_4, n_5, n_1, n_6\}, \\ &\{n_1, n_2, n_4, n_5\}, \{n_2, n_3, n_5, n_6\}, \{n_3, n_4, n_6, n_1\}, \end{aligned}$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum neutrosophic cardinality between all total-dominating sets is called neutrosophic total-dominating number and it's denoted by $\mathcal{T}_n(CYC) = 4.1$ and corresponded to total-dominating sets are

$$\{n_4, n_5, n_1, n_6\}.$$

(b) In Figure (6), an odd-cycle-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows.

- (i) For given neutrosophic vertex, s , there are only two paths with other vertices;
- (ii) in the setting of cycle, a vertex of dominating set corresponded to dominating number dominates as if it doesn't total-dominate since a vertex couldn't dominate itself. Thus two neighbors are necessary in S ;
- (iii) all total-dominating sets corresponded to total-dominating number are

$$\{n_1, n_2, n_5\}, \{n_2, n_3, n_1\}, \{n_3, n_4, n_2\}, \\ \{n_4, n_5, n_3\}, \{n_5, n_1, n_4\},$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum cardinality between all total-dominating sets is called total-dominating number and it's denoted by $\mathcal{T}(CYC) = 3$ and corresponded to total-dominating sets are

$$\{n_1, n_2, n_5\}, \{n_2, n_3, n_1\}, \{n_3, n_4, n_2\}, \\ \{n_4, n_5, n_3\}, \{n_5, n_1, n_4\};$$

(iv) there are eleven total-dominating sets

$$\{n_1, n_2, n_5\}, \{n_2, n_3, n_1\}, \{n_3, n_4, n_2\}, \\ \{n_4, n_5, n_3\}, \{n_5, n_1, n_4\}, \{n_1, n_2, n_3, n_4\}, \\ \{n_1, n_2, n_3, n_5\}, \{n_1, n_2, n_4, n_5\}, \{n_1, n_3, n_4, n_5\}, \\ \{n_2, n_3, n_4, n_5\}, \{n_1, n_2, n_3, n_4, n_5\},$$

as if it's possible to have one of them as a set corresponded to neutrosophic total-dominating number so as neutrosophic cardinality is characteristic;

(v) there are five total-dominating sets

$$\{n_1, n_2, n_5\}, \{n_2, n_3, n_1\}, \{n_3, n_4, n_2\}, \\ \{n_4, n_5, n_3\}, \{n_5, n_1, n_4\},$$

corresponded to total-dominating number as if there's one total-dominating set corresponded to neutrosophic total-dominating number so as neutrosophic cardinality is the determiner;

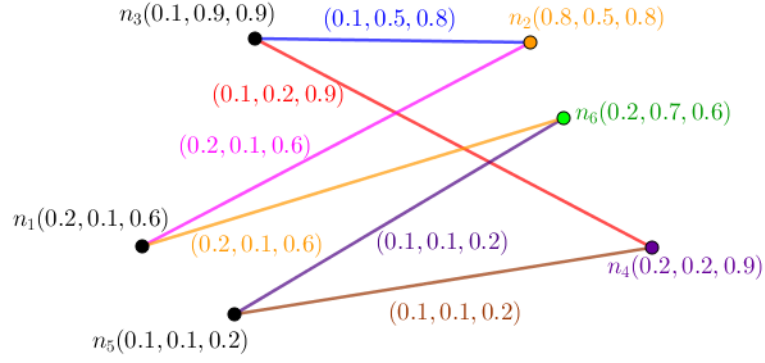


Figure 5. A Neutrosophic Graph in the Viewpoint of its total-dominating number and its neutrosophic total-dominating number.

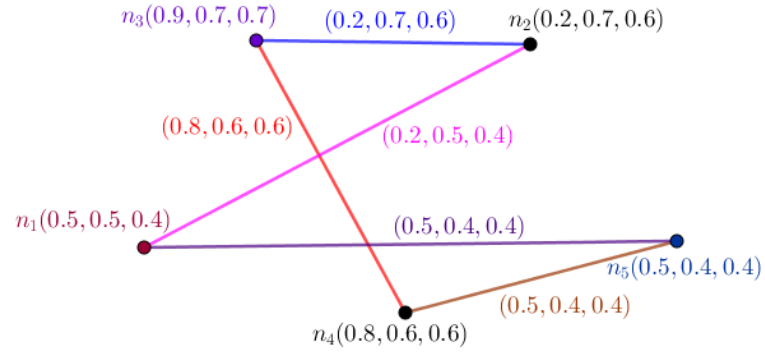


Figure 6. A Neutrosophic Graph in the Viewpoint of its total-dominating number and its neutrosophic total-dominating number.

(vi) all total-dominating sets corresponded to total-dominating number are

$$\{n_1, n_2, n_5\}, \{n_2, n_3, n_1\}, \{n_3, n_4, n_2\}, \\ \{n_4, n_5, n_3\}, \{n_5, n_1, n_4\},$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum neutrosophic cardinality between all total-dominating sets is called neutrosophic total-dominating number and it's denoted by $\mathcal{T}_n(CYC) = 4.2$ and corresponded to total-dominating sets are

$$\{n_1, n_2, n_5\}.$$

Proposition 2.12. Let $NTG : (V, E, \sigma, \mu)$ be a star-neutrosophic graph with center c . Then

$$\mathcal{T}(STR_{1, \sigma_2}) = 2.$$

Proof. Suppose $STR_{1, \sigma_2} : (V, E, \sigma, \mu)$ is a star-neutrosophic graph. An edge always has center, c , as one of its endpoints. All paths have one as their lengths, forever. in the setting of star, a vertex of dominating set corresponded to dominating number dominates as if it doesn't total-dominate since a vertex couldn't dominate itself. Thus

two neighbors are necessary in S . All total-dominating sets corresponded to total-dominating number are

$$\{c(n_1), n_2\}, \{c(n_1), n_3\}, \{c(n_1), n_4\}, \dots, \{c(n_1), n_{\mathcal{O}(STR_{1,\sigma_2})-1}\}, \{c(n_1), n_{\mathcal{O}(STR_{1,\sigma_2})}\}.$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum cardinality between all total-dominating sets is called total-dominating number and it's denoted by

$$\mathcal{T}(STR_{1,\sigma_2}) = 2$$

and corresponded to total-dominating sets are

$$\{c(n_1), n_2\}, \{c(n_1), n_3\}, \{c(n_1), n_4\}, \dots, \{c(n_1), n_{\mathcal{O}(STR_{1,\sigma_2})-1}\}, \{c(n_1), n_{\mathcal{O}(STR_{1,\sigma_2})}\}.$$

Thus

$$\mathcal{T}(STR_{1,\sigma_2}) = 2.$$

□ 407

Proposition 2.13. *Let $NTG : (V, E, \sigma, \mu)$ be a star-neutrosophic graph. Then total-dominating number isn't equal to dominating number.*

Proposition 2.14. *Let $NTG : (V, E, \sigma, \mu)$ be a star-neutrosophic graph with center c . Then there are $2^{\mathcal{O}(STR_{1,\sigma_2})-1} - 2$ total-dominating sets.*

Proposition 2.15. *Let $NTG : (V, E, \sigma, \mu)$ be a star-neutrosophic graph with center c . Then there are $\mathcal{O}(STR_{1,\sigma_2}) - 1$ total-dominating sets corresponded to total-dominating number.*

The clarifications about results are in progress as follows. A star-neutrosophic graph is related to previous result and it's studied to apply the definitions on it. To make it more clear, next part gives one special case to apply definitions and results on it. Some items are devised to make more sense about new notions. A star-neutrosophic graph is related to previous result and it's studied to apply the definitions on it, too.

Example 2.16. There is one section for clarifications. In Figure (7), a star-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows.

- (i) For given two neutrosophic vertices, s and n_1 , there's only one path, precisely one edge between them and there's no path despite them;
- (ii) in the setting of star, a vertex of dominating set corresponded to dominating number dominates as if it doesn't total-dominate since a vertex couldn't dominate itself. Thus two neighbors are necessary in S ;
- (iii) all total-dominating sets corresponded to total-dominating number are

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ \{n_1, n_5\},$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a

neutrosophic vertex s in S such that s total-dominates n , then the set of
neutrosophic vertices, S is called total-dominating set. The minimum cardinality
between all total-dominating sets is called total-dominating number and it's
denoted by $\mathcal{T}(STR_{1,\sigma_2}) = 2$ and corresponded to total-dominating sets are

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ \{n_1, n_5\};$$

(iv) there are fourteen total-dominating sets

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ \{n_1, n_5\}, \{n_1, n_2, n_3\}, \{n_1, n_2, n_4\}, \\ \{n_1, n_2, n_5\}, \{n_1, n_3, n_4\}, \{n_1, n_3, n_5\}, \\ \{n_1, n_4, n_5\}, \{n_1, n_2, n_3, n_4\}, \{n_1, n_2, n_3, n_5\}, \\ \{n_1, n_3, n_4, n_5\}, \{n_1, n_2, n_3, n_4, n_5\},$$

as if it's possible to have one of them as a set corresponded to neutrosophic
total-dominating number so as neutrosophic cardinality is characteristic;

(v) there are four total-dominating sets

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ \{n_1, n_5\},$$

corresponded to total-dominating number as if there's one total-dominating set
corresponded to neutrosophic total-dominating number so as neutrosophic
cardinality is the determiner;

(vi) all total-dominating sets corresponded to total-dominating number are

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ \{n_1, n_5\},$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of
neutrosophic vertices [a vertex alongside triple pair of its values is called
neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a
neutrosophic vertex s in S such that s total-dominates n , then the set of
neutrosophic vertices, S is called total-dominating set. The minimum
neutrosophic cardinality between all total-dominating sets is called neutrosophic
total-dominating number and it's denoted by $\mathcal{T}_n(STR_{1,\sigma_2}) = 2.9$ and
corresponded to total-dominating sets are

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ \{n_1, n_5\}.$$

Proposition 2.17. *Let $NTG : (V, E, \sigma, \mu)$ be a complete-bipartite-neutrosophic graph
which isn't star-neutrosophic graph which means $|V_1|, |V_2| \geq 2$. Then*

$$\mathcal{T}(CMC_{\sigma_1, \sigma_2}) = 2.$$

Proof. Suppose $CMC_{\sigma_1, \sigma_2} : (V, E, \sigma, \mu)$ is a complete-bipartite-neutrosophic graph.
Every vertex in a part and another vertex in opposite part total-dominates any given
vertex. Assume same parity for same partition of vertex set which means V_1 has odd

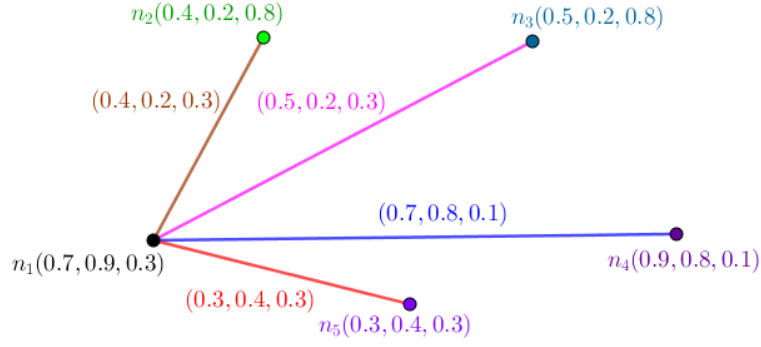


Figure 7. A Neutrosophic Graph in the Viewpoint of its total-dominating number and its neutrosophic total-dominating number.

indexes and V_2 has even indexes. In the setting of complete-bipartite, a vertex of dominating set corresponded to dominating number dominates if and only if it total-dominates since a vertex couldn't dominate itself. Thus two neighbors are necessary in S . All total-dominating sets corresponded to total-dominating number are

$$\begin{aligned} & \{n_1, n_2\}, \{n_1, n_4\}, \dots, \{n_1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-4}\}, \{n_1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-2}\}, \{n_1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})}\}, \\ & \{n_3, n_2\}, \{n_3, n_4\}, \dots, \{n_3, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-4}\}, \{n_3, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-2}\}, \{n_3, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})}\}, \\ & \dots \\ & \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-1}, n_2\}, \dots, \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-1}, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})}\}, \\ & \{n_2, n_1\}, \{n_2, n_1\}, \dots, \{n_2, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-5}\}, \{n_2, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-3}\}, \{n_2, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-1}\}, \\ & \{n_4, n_1\}, \{n_4, n_1\}, \dots, \{n_4, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-5}\}, \{n_4, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-3}\}, \{n_4, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-1}\}, \\ & \dots \\ & \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})}, n_1\}, \dots, \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})}, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-3}\}, \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})}, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-1}\}. \end{aligned}$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum cardinality between all total-dominating sets is called total-dominating number and it's denoted by

$$\mathcal{T}(CMC_{\sigma_1, \sigma_2}) = 2$$

and corresponded to total-dominating sets are

$$\begin{aligned} & \{n_1, n_2\}, \{n_1, n_4\}, \dots, \{n_1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-4}\}, \{n_1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-2}\}, \{n_1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})}\}, \\ & \{n_3, n_2\}, \{n_3, n_4\}, \dots, \{n_3, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-4}\}, \{n_3, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-2}\}, \{n_3, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})}\}, \\ & \dots \\ & \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-1}, n_2\}, \dots, \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-1}, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})}\}, \\ & \{n_2, n_1\}, \{n_2, n_1\}, \dots, \{n_2, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-5}\}, \{n_2, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-3}\}, \{n_2, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-1}\}, \\ & \{n_4, n_1\}, \{n_4, n_1\}, \dots, \{n_4, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-5}\}, \{n_4, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-3}\}, \{n_4, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-1}\}, \\ & \dots \\ & \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})}, n_1\}, \dots, \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})}, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-3}\}, \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})}, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-1}\}, \end{aligned}$$

Thus

$$\mathcal{T}(CMC_{\sigma_1, \sigma_2}) = 2.$$

□ 460

Proposition 2.18. Let $NTG : (V, E, \sigma, \mu)$ be a complete-bipartite-neutrosophic graph. Then total-dominating number is equal to dominating number.

Proposition 2.19. Let $NTG : (V, E, \sigma, \mu)$ be a complete-bipartite-neutrosophic graph. Then there are at least $2^{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-2} - 1 + |V_1| \times |V_2|$ total-dominating sets.

Proposition 2.20. Let $NTG : (V, E, \sigma, \mu)$ be a complete-bipartite-neutrosophic graph. Then there are $|V_1| \times |V_2|$ total-dominating sets corresponded to total-dominating number.

The clarifications about results are in progress as follows. A complete-bipartite-neutrosophic graph is related to previous result and it's studied to apply the definitions on it. To make it more clear, next part gives one special case to apply definitions and results on it. Some items are devised to make more senses about new notions. A complete-bipartite-neutrosophic graph is related to previous result and it's studied to apply the definitions on it, too.

Example 2.21. There is one section for clarifications. In Figure (8), a complete-bipartite-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows.

- (i) For given two neutrosophic vertices, n and n' , there is either one path with length one or one path with length two between them;
- (ii) in the setting of complete-bipartite, a vertex of dominating set corresponded to dominating number dominates if and only if it total-dominates since a vertex couldn't dominate itself. Thus two neighbors are necessary in S ;
- (iii) all total-dominating sets corresponded to total-dominating number are

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_4, n_2\}, \\ \{n_4, n_3\},$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum cardinality between all total-dominating sets is called total-dominating number and it's denoted by $\mathcal{T}(CMC_{\sigma_1, \sigma_2}) = 2$ and corresponded to total-dominating sets are

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_4, n_2\}, \\ \{n_4, n_3\};$$

- (iv) there are nine total-dominating sets

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_4, n_2\}, \\ \{n_4, n_3\}, \{n_1, n_2, n_3\}, \{n_1, n_2, n_4\}, \\ \{n_1, n_3, n_4\}, \{n_4, n_2, n_3\}, \{n_1, n_2, n_3, n_4\},$$

as if it's possible to have one of them as a set corresponded to neutrosophic total-dominating number so as neutrosophic cardinality is characteristic;

- (v) there are four total-dominating sets

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_4, n_2\}, \\ \{n_4, n_3\},$$

corresponded to total-dominating number as if there's one total-dominating set corresponded to neutrosophic total-dominating number so as neutrosophic cardinality is the determiner;

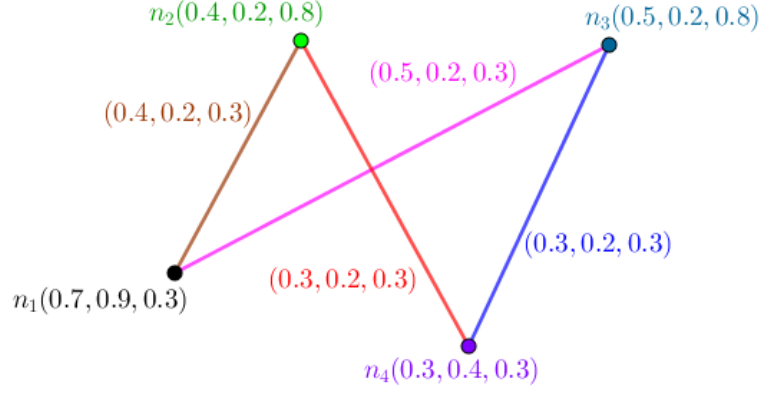


Figure 8. A Neutrosophic Graph in the Viewpoint of its total-dominating number and its neutrosophic total-dominating number.

(vi) all total-dominating sets corresponded to total-dominating number are

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_4, n_2\}, \\ \{n_4, n_3\},$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum neutrosophic cardinality between all total-dominating sets is called neutrosophic total-dominating number and it's denoted by $\mathcal{T}_n(CMC_{\sigma_1, \sigma_2}) = 2.4$ and corresponded to total-dominating sets are

$$\{n_4, n_2\}.$$

Proposition 2.22. Let $NTG : (V, E, \sigma, \mu)$ be a complete- t -partite-neutrosophic graph where $t \geq 3$. Then

$$\mathcal{T}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t}) = 2.$$

Proof. Suppose $CMC_{\sigma_1, \sigma_2, \dots, \sigma_t} : (V, E, \sigma, \mu)$ is a complete- t -partite-neutrosophic graph. Every vertex in a part is total-dominated by another vertex in another part. In the setting of complete- t -partite, a vertex of dominating set corresponded to dominating number dominates if and only if it total-dominates since a vertex couldn't dominate itself. Thus two neighbors are necessary in S . Two vertices from different parts are neighbors and they total-dominates all vertices. All total-dominating sets corresponded

to total-dominating number are

511

$$\begin{aligned}
& \{n_1^1, n_1^2\}, \{n_1^1, n_1^3\}, \dots, \{n_1^1, n_1^t\}, \\
& \{n_1^1, n_2^2\}, \{n_1^1, n_2^3\}, \dots, \{n_1^1, n_2^t\}, \\
& \dots \\
& \{n_1^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^2\}, \{n_1^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^3\}, \dots, \{n_1^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^t\}, \\
& \{n_2^1, n_1^2\}, \{n_2^1, n_1^3\}, \dots, \{n_2^1, n_1^t\}, \\
& \{n_2^1, n_2^2\}, \{n_2^1, n_2^3\}, \dots, \{n_2^1, n_2^t\}, \\
& \dots \\
& \{n_2^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^2\}, \{n_2^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^3\}, \dots, \{n_2^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^t\}, \\
& \dots \\
& \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_1^2\}, \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_1^3\}, \dots, \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_1^t\}, \\
& \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_2^2\}, \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_2^3\}, \dots, \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_2^t\}, \\
& \dots \\
& \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^2\}, \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^3\}, \dots, \\
& \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^t\},
\end{aligned}$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum cardinality between all total-dominating sets is called total-dominating number and it's denoted by

$$\mathcal{T}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t}) = 2$$

and corresponded to total-dominating sets are

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$$\begin{aligned}
& \{n_1^1, n_1^2\}, \{n_1^1, n_1^3\}, \dots, \{n_1^1, n_1^t\}, \\
& \{n_1^1, n_2^2\}, \{n_1^1, n_2^3\}, \dots, \{n_1^1, n_2^t\}, \\
& \dots \\
& \{n_1^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^2\}, \{n_1^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^3\}, \dots, \{n_1^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^t\}, \\
& \{n_2^1, n_1^2\}, \{n_2^1, n_1^3\}, \dots, \{n_2^1, n_1^t\}, \\
& \{n_2^1, n_2^2\}, \{n_2^1, n_2^3\}, \dots, \{n_2^1, n_2^t\}, \\
& \dots \\
& \{n_2^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^2\}, \{n_2^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^3\}, \dots, \{n_2^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^t\}, \\
& \dots \\
& \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_1^2\}, \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_1^3\}, \dots, \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_1^t\}, \\
& \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_2^2\}, \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_2^3\}, \dots, \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_2^t\}, \\
& \dots \\
& \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^2\}, \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^3\}, \dots, \\
& \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^t\},
\end{aligned}$$

Thus

$$\mathcal{T}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t}) = 2.$$

□ 513

Proposition 2.23. Let $NTG : (V, E, \sigma, \mu)$ be a complete- t -partite-neutrosophic graph. Then total-dominating number is equal to dominating number.

Proposition 2.24. Let $NTG : (V, E, \sigma, \mu)$ be a complete- t -partite-neutrosophic graph. Then there are at least $2^{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})-2} - 1$ total-dominating sets.

Proposition 2.25. Let $NTG : (V, E, \sigma, \mu)$ be a complete- t -partite-neutrosophic graph. Then there are at least $|V_1| \times |V_2|$ total-dominating sets corresponded to total-dominating number.

The clarifications about results are in progress as follows. A complete- t -partite-neutrosophic graph is related to previous result and it's studied to apply the definitions on it. To make it more clear, next part gives one special case to apply definitions and results on it. Some items are devised to make more sense about new notions. A complete- t -partite-neutrosophic graph is related to previous result and it's studied to apply the definitions on it, too.

Example 2.26. There is one section for clarifications. In Figure (9), a complete- t -partite-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows.

- (i) For given two neutrosophic vertices, n and n' , there is either one path with length one or one path with length two between them;
- (ii) in the setting of complete- t -partite, a vertex of dominating set corresponded to dominating number dominates if and only if it total-dominates since a vertex couldn't dominate itself. Thus two neighbors are necessary in S . Two vertices from different parts are neighbors and they total-dominates all vertices;
- (iii) all total-dominating sets corresponded to total-dominating number are

$$\begin{aligned} &\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_5\}, \\ &\{n_4, n_2\}, \{n_4, n_3\}, \{n_4, n_5\}, \end{aligned}$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum cardinality between all total-dominating sets is called total-dominating number and it's denoted by $\mathcal{T}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t}) = 2$ and corresponded to total-dominating sets are

$$\begin{aligned} &\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_5\}, \\ &\{n_4, n_2\}, \{n_4, n_3\}, \{n_4, n_5\}; \end{aligned}$$

- (iv) there are twenty-one total-dominating sets

$$\begin{aligned} &\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_5\}, \\ &\{n_4, n_2\}, \{n_4, n_3\}, \{n_4, n_5\}, \\ &\{n_1, n_2, n_3\}, \{n_1, n_2, n_4\}, \{n_1, n_2, n_5\}, \\ &\{n_1, n_3, n_4\}, \{n_1, n_3, n_5\}, \{n_1, n_5, n_4\}, \\ &\{n_4, n_2, n_3\}, \{n_4, n_2, n_5\}, \{n_4, n_3, n_5\}, \\ &\{n_1, n_2, n_3, n_4\}, \{n_1, n_2, n_3, n_5\}, \{n_1, n_2, n_4, n_5\}, \\ &\{n_1, n_3, n_4, n_5\}, \{n_2, n_3, n_4, n_5\}, \{n_1, n_2, n_3, n_4, n_5\}, \end{aligned}$$

as if it's possible to have one of them as a set corresponded to neutrosophic total-dominating number so as neutrosophic cardinality is characteristic;

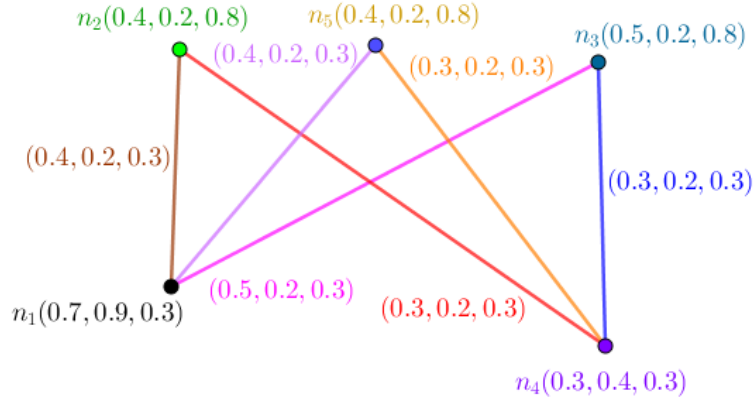


Figure 9. A Neutrosophic Graph in the Viewpoint of its total-dominating number and its neutrosophic total-dominating number.

(v) there are six total-dominating sets

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_5\}, \\ \{n_4, n_2\}, \{n_4, n_3\}, \{n_4, n_5\},$$

corresponded to total-dominating number as if there's one total-dominating set
corresponded to neutrosophic total-dominating number so as neutrosophic
cardinality is the determiner;

(vi) all total-dominating sets corresponded to total-dominating number are

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_5\}, \\ \{n_4, n_2\}, \{n_4, n_3\}, \{n_4, n_5\}.$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of
neutrosophic vertices [a vertex alongside triple pair of its values is called
neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a
neutrosophic vertex s in S such that s total-dominates n , then the set of
neutrosophic vertices, S is called total-dominating set. The minimum
neutrosophic cardinality between all total-dominating sets is called neutrosophic
total-dominating number and it's denoted by $\mathcal{T}_n(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t}) = 2.4$ and
corresponded to total-dominating sets are

$$\{n_4, n_2\}, \{n_4, n_5\}.$$

Proposition 2.27. Let $NTG : (V, E, \sigma, \mu)$ be a wheel-neutrosophic graph. Then

$$\mathcal{T}(WHL_{1, \sigma_2}) = 2.$$

Proof. Suppose $WHL_{1, \sigma_2} : (V, E, \sigma, \mu)$ is a wheel-neutrosophic graph. The argument is
elementary. All vertices of a cycle join to one vertex, c . For every vertices, the minimum
number of edges amid them is either one or two because of center and the notion of
neighbors. In the setting of wheel, a vertex of dominating set corresponded to
dominating number dominates as if it doesn't total-dominate since a vertex couldn't
dominate itself. Thus two neighbors are necessary in S . Two vertices including center
and other vertex are neighbors and they total-dominates all vertices. All
total-dominating sets corresponded to total-dominating number are

$$\{n_1(c), n_2\}, \{n_1(c), n_3\}, \{n_1(c), n_4\}, \dots, \{n_1(c), n_{\mathcal{O}(WHL_{1, \sigma_2})-1}\}, \{n_1(c), n_{\mathcal{O}(WHL_{1, \sigma_2})}\}.$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum cardinality between all total-dominating sets is called total-dominating number and it's denoted by

$$\mathcal{T}(WHL_{1,\sigma_2}) = 2$$

and corresponded to total-dominating sets are

$$\{n_1(c), n_2\}, \{n_1(c), n_3\}, \{n_1(c), n_4\}, \dots, \{n_1(c), n_{\mathcal{O}(WHL_{1,\sigma_2})-1}\}, \{n_1(c), n_{\mathcal{O}(WHL_{1,\sigma_2})}\}.$$

Thus

$$\mathcal{T}(WHL_{1,\sigma_2}) = \mathcal{O}(WHL_{1,\sigma_2}) - 1.$$

□ 569

Proposition 2.28. *Let $NTG : (V, E, \sigma, \mu)$ be a wheel-neutrosophic graph. Then total-dominating number isn't equal to dominating number.*

Proposition 2.29. *Let $NTG : (V, E, \sigma, \mu)$ be a wheel-neutrosophic graph with center c . Then there are $2^{\mathcal{O}(WHL_{1,\sigma_2})-1} - 1$ total-dominating sets.*

Proposition 2.30. *Let $NTG : (V, E, \sigma, \mu)$ be a wheel-neutrosophic graph with center c . Then there are $\mathcal{O}(WHL_{1,\sigma_2})$ total-dominating sets corresponded to total-dominating number.*

The clarifications about results are in progress as follows. A wheel-neutrosophic graph is related to previous result and it's studied to apply the definitions on it. To make it more clear, next part gives one special case to apply definitions and results on it. Some items are devised to make more sense about new notions. A wheel-neutrosophic graph is related to previous result and it's studied to apply the definitions on it, too.

Example 2.31. There is one section for clarifications. In Figure (10), a wheel-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows.

- (i) For given two neutrosophic vertices, s and n_1 , there's only one edge between them;
- (ii) in the setting of wheel, a vertex of dominating set corresponded to dominating number dominates as if it doesn't total-dominate since a vertex couldn't dominate itself. Thus two neighbors are necessary in S . Two vertices including center and other vertex are neighbors and they total-dominates all vertices;
- (iii) all total-dominating sets corresponded to total-dominating number are

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \{n_1, n_5\}.$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum cardinality between all total-dominating sets is called total-dominating number and it's denoted by $\mathcal{T}(WHL_{1,\sigma_2}) = 2$ and corresponded to total-dominating sets are

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \{n_1, n_5\};$$

(iv) there are fifteen total-dominating sets

$$\begin{aligned} &\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ &\{n_1, n_5\}, \{n_1, n_2, n_3\}, \{n_1, n_2, n_4\}, \\ &\{n_1, n_2, n_5\}, \{n_1, n_3, n_4\}, \{n_1, n_3, n_5\}, \\ &\{n_1, n_4, n_5\}, \{n_1, n_2, n_3, n_4\}, \{n_1, n_2, n_3, n_5\}, \\ &\{n_1, n_2, n_4, n_5\}, \{n_1, n_3, n_4, n_5\}, \{n_1, n_2, n_3, n_4, n_5\}, \end{aligned}$$

as if it's possible to have one of them as a set corresponded to neutrosophic total-dominating number so as neutrosophic cardinality is characteristic;

(v) there are four total-dominating sets

$$\begin{aligned} &\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ &\{n_1, n_5\}, \end{aligned}$$

corresponded to total-dominating number as if there's one total-dominating set corresponded to neutrosophic total-dominating number so as neutrosophic cardinality is the determiner;

(vi) all total-dominating sets corresponded to total-dominating number are

$$\begin{aligned} &\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ &\{n_1, n_5\}. \end{aligned}$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum neutrosophic cardinality between all total-dominating sets is called neutrosophic total-dominating number and it's denoted by $\mathcal{T}_n(WHL_{1,\sigma_2}) = 2.9$ and corresponded to total-dominating sets are

$$\{n_1, n_4\}.$$

3 Setting of neutrosophic total-dominating number

In this section, I provide some results in the setting of neutrosophic total-dominating number. Some classes of neutrosophic graphs are chosen. Complete-neutrosophic graph, path-neutrosophic graph, cycle-neutrosophic graph, star-neutrosophic graph, bipartite-neutrosophic graph, t-partite-neutrosophic graph, and wheel-neutrosophic graph, are both of cases of study and classes which the results are about them.

Proposition 3.1. *Let $NTG : (V, E, \sigma, \mu)$ be a complete-neutrosophic graph. Then*

$$\mathcal{T}_n(CMT_\sigma) = \min_{x,y \in V} \sum_{i=1}^3 (\sigma_i(x) + \sigma_i(y)).$$

Proof. Suppose $CMT_\sigma : (V, E, \sigma, \mu)$ is a complete-neutrosophic graph. By $CMT_\sigma : (V, E, \sigma, \mu)$ is a complete-neutrosophic graph, all vertices are connected to each other. So there's one edge between two vertices. In the setting of complete, a vertex of

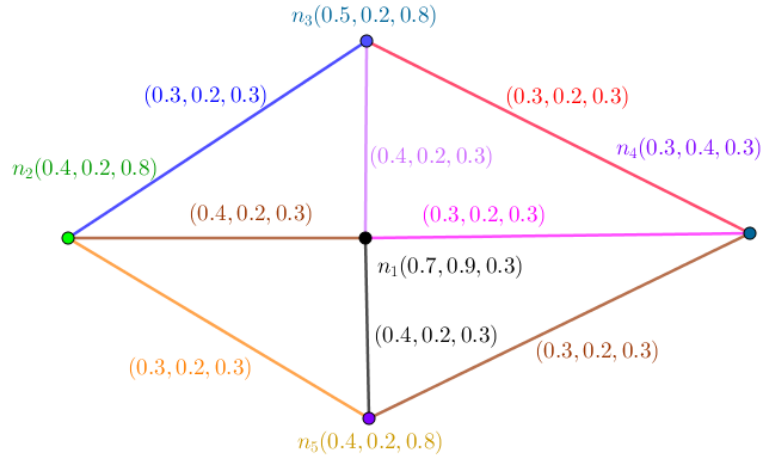


Figure 10. A Neutrosophic Graph in the Viewpoint of its total-dominating number and its neutrosophic total-dominating number.

dominating set corresponded to dominating number dominates as if it doesn't total-dominate since a vertex couldn't dominate itself. All total-dominating sets corresponded to total-dominating number are

$$\begin{aligned} & \{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \dots, \{n_1, n_{\mathcal{O}(CMT_\sigma)-2}\}, \{n_1, n_{\mathcal{O}(CMT_\sigma)-1}\}, \{n_1, n_{\mathcal{O}(CMT_\sigma)}\} \\ & \{n_2, n_3\}, \{n_2, n_4\}, \{n_2, n_5\}, \dots, \{n_2, n_{\mathcal{O}(CMT_\sigma)-2}\}, \{n_2, n_{\mathcal{O}(CMT_\sigma)-1}\}, \{n_2, n_{\mathcal{O}(CMT_\sigma)}\} \\ & \{n_3, n_4\}, \{n_3, n_5\}, \{n_3, n_6\}, \dots, \{n_3, n_{\mathcal{O}(CMT_\sigma)-2}\}, \{n_3, n_{\mathcal{O}(CMT_\sigma)-1}\}, \{n_3, n_{\mathcal{O}(CMT_\sigma)}\} \\ & \dots \\ & \{n_{\mathcal{O}(CMT_\sigma)-3}, n_{\mathcal{O}(CMT_\sigma)-2}\}, \{n_{\mathcal{O}(CMT_\sigma)-3}, n_{\mathcal{O}(CMT_\sigma)-1}\}, \{n_{\mathcal{O}(CMT_\sigma)-3}, n_{\mathcal{O}(CMT_\sigma)}\} \\ & \{n_{\mathcal{O}(CMT_\sigma)-2}, n_{\mathcal{O}(CMT_\sigma)-1}\}, \{n_{\mathcal{O}(CMT_\sigma)-2}, n_{\mathcal{O}(CMT_\sigma)}\} \\ & \{n_{\mathcal{O}(CMT_\sigma)-1}, n_{\mathcal{O}(CMT_\sigma)}\} \end{aligned}$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum neutrosophic cardinality between all total-dominating sets is called neutrosophic total-dominating number and it's denoted by

$$\mathcal{T}_n(CMT_\sigma) = \min_{x, y \in V} \sum_{i=1}^3 (\sigma_i(x) + \sigma_i(y))$$

and corresponded to total-dominating sets are

$$\begin{aligned} & \{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \dots, \{n_1, n_{\mathcal{O}(CMT_\sigma)-2}\}, \{n_1, n_{\mathcal{O}(CMT_\sigma)-1}\}, \{n_1, n_{\mathcal{O}(CMT_\sigma)}\} \\ & \{n_2, n_3\}, \{n_2, n_4\}, \{n_2, n_5\}, \dots, \{n_2, n_{\mathcal{O}(CMT_\sigma)-2}\}, \{n_2, n_{\mathcal{O}(CMT_\sigma)-1}\}, \{n_2, n_{\mathcal{O}(CMT_\sigma)}\} \\ & \{n_3, n_4\}, \{n_3, n_5\}, \{n_3, n_6\}, \dots, \{n_3, n_{\mathcal{O}(CMT_\sigma)-2}\}, \{n_3, n_{\mathcal{O}(CMT_\sigma)-1}\}, \{n_3, n_{\mathcal{O}(CMT_\sigma)}\} \\ & \dots \\ & \{n_{\mathcal{O}(CMT_\sigma)-3}, n_{\mathcal{O}(CMT_\sigma)-2}\}, \{n_{\mathcal{O}(CMT_\sigma)-3}, n_{\mathcal{O}(CMT_\sigma)-1}\}, \{n_{\mathcal{O}(CMT_\sigma)-3}, n_{\mathcal{O}(CMT_\sigma)}\} \\ & \{n_{\mathcal{O}(CMT_\sigma)-2}, n_{\mathcal{O}(CMT_\sigma)-1}\}, \{n_{\mathcal{O}(CMT_\sigma)-2}, n_{\mathcal{O}(CMT_\sigma)}\} \\ & \{n_{\mathcal{O}(CMT_\sigma)-1}, n_{\mathcal{O}(CMT_\sigma)}\} \end{aligned}$$

Thus

$$\mathcal{T}_n(CMT_\sigma) = \min_{x,y \in V} \sum_{i=1}^3 (\sigma_i(x) + \sigma_i(y)).$$

□ 628

Proposition 3.2. *Let $NTG : (V, E, \sigma, \mu)$ be a complete-neutrosophic graph. Then total-dominating number isn't equal to dominating number.* 629 630

Proposition 3.3. *Let $NTG : (V, E, \sigma, \mu)$ be a complete-neutrosophic graph. Then the number of total-dominating sets corresponded to total-dominating number is equal to $\mathcal{O}(CMT_\sigma)$ choose two.* 631 632 633

Proposition 3.4. *Let $NTG : (V, E, \sigma, \mu)$ be a complete-neutrosophic graph. Then the number of total-dominating sets is equal to $\mathcal{O}(CMT_\sigma)$ choose two plus $\mathcal{O}(CMT_\sigma)$ choose three plus one.* 634 635 636

The clarifications about results are in progress as follows. A complete-neutrosophic graph is related to previous result and it's studied to apply the definitions on it. To make it more clear, next part gives one special case to apply definitions and results on it. Some items are devised to make more sense about new notions. A complete-neutrosophic graph is related to previous result and it's studied to apply the definitions on it, too. 637 638 639 640 641 642

Example 3.5. In Figure (11), a complete-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows. 643 644

- (i) For given neutrosophic vertex, s , there's an edge with other vertices; 645
- (ii) in the setting of complete, a vertex of dominating set corresponded to dominating number dominates as if it doesn't total-dominate since a vertex couldn't dominate itself; 646 647 648
- (iii) all total-dominating sets corresponded to total-dominating number are 649

$$\begin{aligned} &\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ &\{n_2, n_3\}, \{n_2, n_4\}, \{n_3, n_4\}. \end{aligned}$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum cardinality between all total-dominating sets is called total-dominating number and it's denoted by $\mathcal{T}(CMT_\sigma) = 2$ and corresponded to total-dominating sets are 650 651 652 653 654 655 656

$$\begin{aligned} &\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ &\{n_2, n_3\}, \{n_2, n_4\}, \{n_3, n_4\}; \end{aligned}$$

- (iv) there are eleven total-dominating sets 657

$$\begin{aligned} &\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ &\{n_2, n_3\}, \{n_2, n_4\}, \{n_3, n_4\}, \\ &\{n_1, n_2, n_3\}, \{n_1, n_2, n_4\}, \{n_1, n_3, n_4\}, \\ &\{n_2, n_3, n_4\}, \{n_1, n_2, n_3, n_4\}, \end{aligned}$$

as if it's possible to have one of them as a set corresponded to neutrosophic total-dominating number so as neutrosophic cardinality is characteristic; 658 659

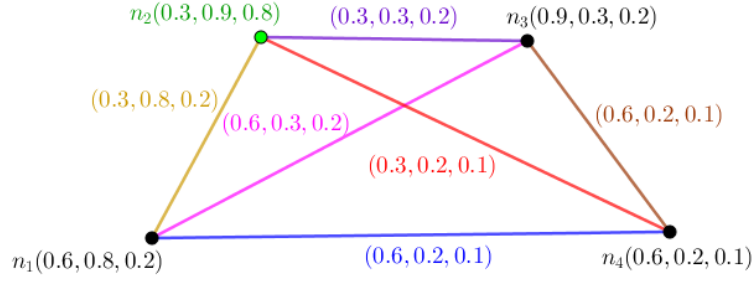


Figure 11. A Neutrosophic Graph in the Viewpoint of its total-dominating number and its neutrosophic total-dominating number.

(v) there are six total-dominating sets

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ \{n_2, n_3\}, \{n_2, n_4\}, \{n_3, n_4\},$$

corresponded to total-dominating number as if there's one total-dominating set
corresponded to neutrosophic total-dominating number so as neutrosophic
cardinality is the determiner;

(vi) all total-dominating sets corresponded to total-dominating number are

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ \{n_2, n_3\}, \{n_2, n_4\}, \{n_3, n_4\}.$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of
neutrosophic vertices [a vertex alongside triple pair of its values is called
neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a
neutrosophic vertex s in S such that s total-dominates n , then the set of
neutrosophic vertices, S is called total-dominating set. The minimum
neutrosophic cardinality between all total-dominating sets is called neutrosophic
total-dominating number and it's denoted by $\mathcal{T}_n(CMT_\sigma) = 2.3$ and corresponded
to neutrosophic total-dominating sets are

$$\{n_3, n_4\}.$$

Another class of neutrosophic graphs is addressed to path-neutrosophic graph.

Proposition 3.6. Let $NTG : (V, E, \sigma, \mu)$ be a path-neutrosophic graph. Then

$$\mathcal{T}_n(PTH) = \min_{|S|=(\lfloor \frac{\mathcal{O}(PTH)}{2} \rfloor)(\lfloor \lfloor \frac{\mathcal{O}(PTH)}{2} \rfloor + 1))} \sum_{x \in S} \sum_{i=1}^3 \sigma_i(x).$$

Proof. Suppose $PTH : (V, E, \sigma, \mu)$ is a path-neutrosophic graph. Let
 $n_1, n_2, \dots, n_{\mathcal{O}(PTH)}$ be a path-neutrosophic graph. For given two vertices, x and y ,
there's one path from x to y . In the setting of path, a vertex of dominating set
corresponded to dominating number dominates as if it doesn't total-dominate since a
vertex couldn't dominate itself. Thus two neighbors are necessary in S . All
total-dominating sets corresponded to total-dominating number are

$$\{n_1, n_2, n_5, n_6, n_9, n_{10} \dots\}, \{n_2, n_3, n_6, n_7, n_{10}, n_{11} \dots\}, \{n_2, n_3, n_4, n_7, n_8, \dots\}, \\ \dots \\ \{\dots, n_{\mathcal{O}(PTH)-10}, n_{\mathcal{O}(PTH)-9}, n_{\mathcal{O}(PTH)-6}, n_{\mathcal{O}(PTH)-5}, n_{\mathcal{O}(PTH)-2}, n_{\mathcal{O}(PTH)-1}\} \\ \{\dots, n_{\mathcal{O}(PTH)-9}, n_{\mathcal{O}(PTH)-8}, n_{\mathcal{O}(PTH)-5}, n_{\mathcal{O}(PTH)-4}, n_{\mathcal{O}(PTH)-1}, n_{\mathcal{O}(PTH)}\}.$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum neutrosophic cardinality between all total-dominating sets is called neutrosophic total-dominating number and it's denoted by

$$\mathcal{T}_n(PTH) = \min_{|S|=(\lfloor \lceil \frac{\mathcal{O}(PTH)}{2} \rceil)(\lfloor \rfloor)+1)} \sum_{x \in S} \sum_{i=1}^3 \sigma_i(x)$$

and corresponded to total-dominating sets are

$$\begin{aligned} & \{n_1, n_2, n_5, n_6, n_9, n_{10} \dots\}, \{n_2, n_3, n_6, n_7, n_{10}, n_{11} \dots\}, \{n_2, n_3, n_4, n_7, n_8, \dots\}, \\ & \dots \\ & \{\dots, n_{\mathcal{O}(PTH)-10}, n_{\mathcal{O}(PTH)-9}, n_{\mathcal{O}(PTH)-6}, n_{\mathcal{O}(PTH)-5}, n_{\mathcal{O}(PTH)-2}, n_{\mathcal{O}(PTH)-1}\} \\ & \{\dots, n_{\mathcal{O}(PTH)-9}, n_{\mathcal{O}(PTH)-8}, n_{\mathcal{O}(PTH)-5}, n_{\mathcal{O}(PTH)-4}, n_{\mathcal{O}(PTH)-1}, n_{\mathcal{O}(PTH)}\}. \end{aligned}$$

Thus

$$\mathcal{T}_n(PTH) = \min_{|S|=(\lfloor \lceil \frac{\mathcal{O}(PTH)}{2} \rceil)(\lfloor \rfloor)+1)} \sum_{x \in S} \sum_{i=1}^3 \sigma_i(x).$$

□ 681

Proposition 3.7. Let $NTG : (V, E, \sigma, \mu)$ be a path-neutrosophic graph. Then total-dominating number isn't equal to dominating number.

Example 3.8. There are two sections for clarifications.

- (a) In Figure (12), an odd-path-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows.
 - (i) For given neutrosophic vertex, s , there's only one path with other vertices;
 - (ii) in the setting of path, a vertex of dominating set corresponded to dominating number dominates as if it doesn't total-dominate since a vertex couldn't dominate itself. Thus two neighbors are necessary in S ;
 - (iii) all total-dominating sets corresponded to total-dominating number are

$$\{n_2, n_3, n_4\},$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum cardinality between all total-dominating sets is called total-dominating number and it's denoted by $\mathcal{T}(PTH) = 3$ and corresponded to total-dominating sets are

$$\{n_2, n_3, n_4\};$$

- (iv) there are five total-dominating sets

$$\begin{aligned} & \{n_2, n_3, n_4\}, \{n_1, n_2, n_3, n_4\}, \{n_5, n_2, n_3, n_4\}, \\ & \{n_1, n_2, n_3, n_4, n_5\}, \{n_1, n_2, n_4, n_5\}, \end{aligned}$$

as if it's possible to have one of them as a set corresponded to neutrosophic total-dominating number so as neutrosophic cardinality is characteristic;

(v) there's one total-dominating set

$$\{n_2, n_3, n_4\},$$

corresponded to total-dominating number as if there's one total-dominating set corresponded to neutrosophic total-dominating number so as neutrosophic cardinality is the determiner;

(vi) all total-dominating sets corresponded to total-dominating number are

$$\{n_2, n_3, n_4\},$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum cardinality between all total-dominating sets is called total-dominating number and it's denoted by $\mathcal{T}(PTH) = 3.7$ and corresponded to total-dominating sets are

$$\{n_2, n_3, n_4\}.$$

(b) In Figure (13), an even-path-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows.

- (i) For given neutrosophic vertex, s , there's only one path with other vertices;
- (ii) in the setting of path, a vertex of dominating set corresponded to dominating number dominates as if it doesn't total-dominate since a vertex couldn't dominate itself. Thus two neighbors are necessary in S ;
- (iii) all total-dominating sets corresponded to total-dominating number are

$$\{n_1, n_2, n_5, n_6\}, \{n_2, n_3, n_5, n_6\}, \{n_2, n_3, n_4, n_5\},$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum cardinality between all total-dominating sets is called total-dominating number and it's denoted by $\mathcal{T}(PTH) = 4$ and corresponded to total-dominating sets are

$$\{n_1, n_2, n_5, n_6\}, \{n_2, n_3, n_5, n_6\}, \{n_2, n_3, n_4, n_5\};$$

(iv) there are eight total-dominating sets

$$\begin{aligned} &\{n_1, n_2, n_5, n_6\}, \{n_2, n_3, n_5, n_6\}, \{n_2, n_3, n_4, n_5\}, \\ &\{n_1, n_2, n_5, n_6, n_3\}, \{n_1, n_2, n_5, n_6, n_4\}, \{n_1, n_2, n_5, n_6, n_4, n_3\}, \\ &\{n_2, n_3, n_5, n_6, n_4\}, \{n_2, n_3, n_4, n_5, n_1\}, \end{aligned}$$

as if it's possible to have one of them as a set corresponded to neutrosophic total-dominating number so as neutrosophic cardinality is characteristic;

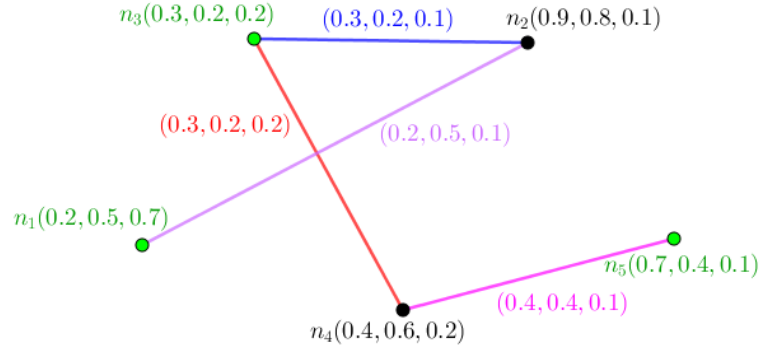


Figure 12. A Neutrosophic Graph in the Viewpoint of its total-dominating number and its neutrosophic total-dominating number.

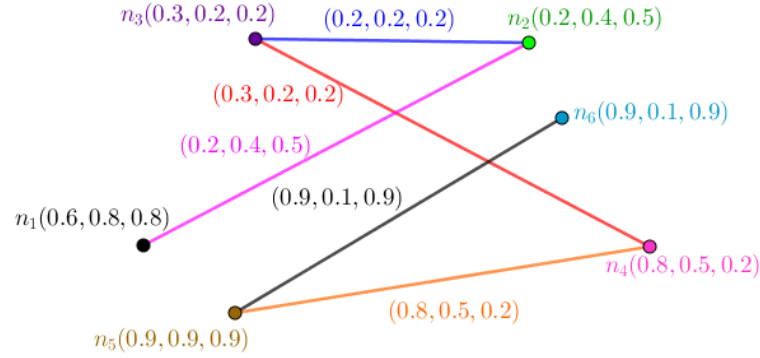


Figure 13. A Neutrosophic Graph in the Viewpoint of its total-dominating number and its neutrosophic total-dominating number.

(v) there are three total-dominating sets

$$\{n_1, n_2, n_5, n_6\}, \{n_2, n_3, n_5, n_6\}, \{n_2, n_3, n_4, n_5\},$$

corresponded to total-dominating number as if there's one total-dominating set corresponded to neutrosophic total-dominating number so as neutrosophic cardinality is the determiner;

(vi) all total-dominating sets corresponded to total-dominating number are

$$\{n_1, n_2, n_5, n_6\}, \{n_2, n_3, n_5, n_6\}, \{n_2, n_3, n_4, n_5\},$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum neutrosophic cardinality between all total-dominating sets is called neutrosophic total-dominating number and it's denoted by $\mathcal{T}_n(PTH) = 6$ and corresponded to total-dominating sets are

$$\{n_2, n_3, n_4, n_5\}.$$

Proposition 3.9. Let $NTG : (V, E, \sigma, \mu)$ be a cycle-neutrosophic graph where

$\mathcal{O}(CYC) \geq 3$. Then

$$\mathcal{T}_n(CYC) = \min_{|S|=(\lfloor \frac{\mathcal{O}(CYC)}{2} \rfloor)(+1)} \sum_{x \in S} \sum_{i=1}^3 \sigma_i(x).$$

Proof. Suppose $CYC : (V, E, \sigma, \mu)$ is a cycle-neutrosophic graph. For given two vertices, x and y , there are only two paths with distinct edges from x to y . Let

$$x_1, x_2, \dots, x_{\mathcal{O}(CYC)-1}, x_{\mathcal{O}(CYC)}, x_1$$

be a cycle-neutrosophic graph $CYC : (V, E, \sigma, \mu)$. In the setting of cycle, a vertex of dominating set corresponded to dominating number dominates as if it doesn't total-dominate since a vertex couldn't dominate itself. Thus two neighbors are necessary in S . All total-dominating sets corresponded to total-dominating number are

$$\begin{aligned} & \{n_1, n_2, n_5, n_6, n_9, n_{10} \dots\}, \{n_2, n_3, n_6, n_7, n_{10}, n_{11} \dots\}, \{n_2, n_3, n_4, n_7, n_8, \dots\}, \\ & \dots \\ & \{\dots, n_{\mathcal{O}(CYC)-10}, n_{\mathcal{O}(CYC)-9}, n_{\mathcal{O}(CYC)-6}, n_{\mathcal{O}(CYC)-5}, n_{\mathcal{O}(CYC)-2}, n_{\mathcal{O}(CYC)-1}\} \\ & \{\dots, n_{\mathcal{O}(CYC)-9}, n_{\mathcal{O}(CYC)-8}, n_{\mathcal{O}(CYC)-5}, n_{\mathcal{O}(CYC)-4}, n_{\mathcal{O}(CYC)-1}, n_{\mathcal{O}(CYC)}\}. \end{aligned}$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum neutrosophic cardinality between all total-dominating sets is called neutrosophic total-dominating number and it's denoted by

$$\mathcal{T}_n(CYC) = \min_{|S|=(\lfloor \frac{\mathcal{O}(CYC)}{2} \rfloor)(+1)} \sum_{x \in S} \sum_{i=1}^3 \sigma_i(x)$$

and corresponded to total-dominating sets are

$$\begin{aligned} & \{n_1, n_2, n_5, n_6, n_9, n_{10} \dots\}, \{n_2, n_3, n_6, n_7, n_{10}, n_{11} \dots\}, \{n_2, n_3, n_4, n_7, n_8, \dots\}, \\ & \dots \\ & \{\dots, n_{\mathcal{O}(CYC)-10}, n_{\mathcal{O}(CYC)-9}, n_{\mathcal{O}(CYC)-6}, n_{\mathcal{O}(CYC)-5}, n_{\mathcal{O}(CYC)-2}, n_{\mathcal{O}(CYC)-1}\} \\ & \{\dots, n_{\mathcal{O}(CYC)-9}, n_{\mathcal{O}(CYC)-8}, n_{\mathcal{O}(CYC)-5}, n_{\mathcal{O}(CYC)-4}, n_{\mathcal{O}(CYC)-1}, n_{\mathcal{O}(CYC)}\}. \end{aligned}$$

Thus

$$\mathcal{T}_n(CYC) = \min_{|S|=(\lfloor \frac{\mathcal{O}(CYC)}{2} \rfloor)(+1)} \sum_{x \in S} \sum_{i=1}^3 \sigma_i(x).$$

□

Proposition 3.10. Let $NTG : (V, E, \sigma, \mu)$ be a cycle-neutrosophic graph. Then total-dominating number isn't equal to dominating number.

The clarifications about results are in progress as follows. An odd-cycle-neutrosophic graph is related to previous result and it's studied to apply the definitions on it. To make it more clear, next part gives one special case to apply definitions and results on it. Some items are devised to make more sense about new notions. An even-cycle-neutrosophic graph is related to previous result and it's studied to apply the definitions on it, too.

Example 3.11. There are two sections for clarifications. 761

- (a) In Figure (14), an even-cycle-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows. 762
- (i) For given neutrosophic vertex, s , there are only two paths with other vertices; 764
- (ii) in the setting of cycle, a vertex of dominating set corresponded to dominating number dominates as if it doesn't total-dominate since a vertex couldn't dominate itself. Thus two neighbors are necessary in S ; 765
- (iii) all total-dominating sets corresponded to total-dominating number are 766

$$\begin{aligned} &\{n_1, n_2, n_5, n_6\}, \{n_2, n_3, n_6, n_1\}, \{n_3, n_4, n_1, n_2\}, \\ &\{n_3, n_4, n_5, n_6\}, \{n_4, n_5, n_2, n_3\}, \{n_4, n_5, n_1, n_6\}, \\ &\{n_1, n_2, n_4, n_5\}, \{n_2, n_3, n_5, n_6\}, \{n_3, n_4, n_6, n_1\}, \end{aligned}$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum cardinality between all total-dominating sets is called total-dominating number and it's denoted by $\mathcal{T}(CYC) = 4$ and corresponded to total-dominating sets are 769

$$\begin{aligned} &\{n_1, n_2, n_5, n_6\}, \{n_2, n_3, n_6, n_1\}, \{n_3, n_4, n_1, n_2\}, \\ &\{n_3, n_4, n_5, n_6\}, \{n_4, n_5, n_2, n_3\}, \{n_4, n_5, n_1, n_6\}, \\ &\{n_1, n_2, n_4, n_5\}, \{n_2, n_3, n_5, n_6\}, \{n_3, n_4, n_6, n_1\}; \end{aligned}$$

- (iv) there are sixteen total-dominating sets 777

$$\begin{aligned} &\{n_1, n_2, n_5, n_6\}, \{n_2, n_3, n_6, n_1\}, \{n_3, n_4, n_1, n_2\}, \\ &\{n_3, n_4, n_5, n_6\}, \{n_4, n_5, n_2, n_3\}, \{n_4, n_5, n_1, n_6\}, \\ &\{n_1, n_2, n_4, n_5\}, \{n_2, n_3, n_5, n_6\}, \{n_3, n_4, n_6, n_1\}, \\ &\{n_1, n_2, n_3, n_5, n_6\}, \{n_1, n_2, n_4, n_5, n_6\}, \{n_1, n_2, n_3, n_4, n_5, n_6\}, \\ &\{n_6, n_2, n_3, n_4, n_5\}, \{n_6, n_1, n_3, n_4, n_5\}, \{n_6, n_1, n_2, n_3, n_4\}, \\ &\{n_5, n_1, n_2, n_3, n_4\}, \end{aligned}$$

as if it's possible to have one of them as a set corresponded to neutrosophic total-dominating number so as neutrosophic cardinality is characteristic; 778

- (v) there are nine total-dominating sets 780

$$\begin{aligned} &\{n_1, n_2, n_5, n_6\}, \{n_2, n_3, n_6, n_1\}, \{n_3, n_4, n_1, n_2\}, \\ &\{n_3, n_4, n_5, n_6\}, \{n_4, n_5, n_2, n_3\}, \{n_4, n_5, n_1, n_6\}, \\ &\{n_1, n_2, n_4, n_5\}, \{n_2, n_3, n_5, n_6\}, \{n_3, n_4, n_6, n_1\}, \end{aligned}$$

corresponded to total-dominating number as if there's one total-dominating set corresponded to neutrosophic total-dominating number so as neutrosophic cardinality is the determiner; 781

- (vi) all total-dominating sets corresponded to total-dominating number are 782

$$\begin{aligned} &\{n_1, n_2, n_5, n_6\}, \{n_2, n_3, n_6, n_1\}, \{n_3, n_4, n_1, n_2\}, \\ &\{n_3, n_4, n_5, n_6\}, \{n_4, n_5, n_2, n_3\}, \{n_4, n_5, n_1, n_6\}, \\ &\{n_1, n_2, n_4, n_5\}, \{n_2, n_3, n_5, n_6\}, \{n_3, n_4, n_6, n_1\}, \end{aligned}$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum neutrosophic cardinality between all total-dominating sets is called neutrosophic total-dominating number and it's denoted by $\mathcal{T}_n(CYC) = 4.1$ and corresponded to total-dominating sets are

$$\{n_4, n_5, n_1, n_6\}.$$

(b) In Figure (15), an odd-cycle-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows.

- (i) For given neutrosophic vertex, s , there are only two paths with other vertices;
- (ii) in the setting of cycle, a vertex of dominating set corresponded to dominating number dominates as if it doesn't total-dominate since a vertex couldn't dominate itself. Thus two neighbors are necessary in S ;
- (iii) all total-dominating sets corresponded to total-dominating number are

$$\{n_1, n_2, n_5\}, \{n_2, n_3, n_1\}, \{n_3, n_4, n_2\}, \\ \{n_4, n_5, n_3\}, \{n_5, n_1, n_4\},$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum cardinality between all total-dominating sets is called total-dominating number and it's denoted by $\mathcal{T}(CYC) = 3$ and corresponded to total-dominating sets are

$$\{n_1, n_2, n_5\}, \{n_2, n_3, n_1\}, \{n_3, n_4, n_2\}, \\ \{n_4, n_5, n_3\}, \{n_5, n_1, n_4\};$$

(iv) there are eleven total-dominating sets

$$\{n_1, n_2, n_5\}, \{n_2, n_3, n_1\}, \{n_3, n_4, n_2\}, \\ \{n_4, n_5, n_3\}, \{n_5, n_1, n_4\}, \{n_1, n_2, n_3, n_4\}, \\ \{n_1, n_2, n_3, n_5\}, \{n_1, n_2, n_4, n_5\}, \{n_1, n_3, n_4, n_5\}, \\ \{n_2, n_3, n_4, n_5\}, \{n_1, n_2, n_3, n_4, n_5\},$$

as if it's possible to have one of them as a set corresponded to neutrosophic total-dominating number so as neutrosophic cardinality is characteristic;

(v) there are five total-dominating sets

$$\{n_1, n_2, n_5\}, \{n_2, n_3, n_1\}, \{n_3, n_4, n_2\}, \\ \{n_4, n_5, n_3\}, \{n_5, n_1, n_4\},$$

corresponded to total-dominating number as if there's one total-dominating set corresponded to neutrosophic total-dominating number so as neutrosophic cardinality is the determiner;

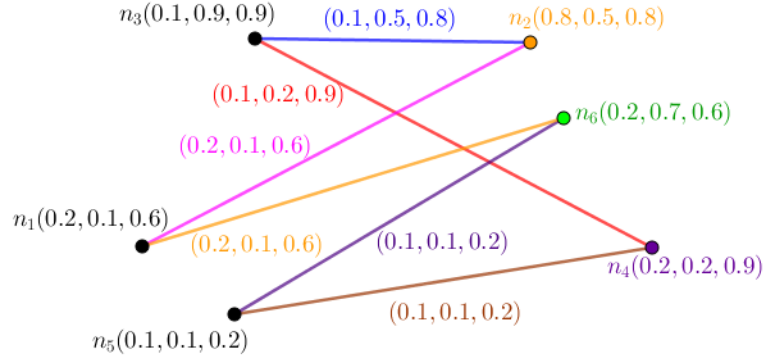


Figure 14. A Neutrosophic Graph in the Viewpoint of its total-dominating number and its neutrosophic total-dominating number.

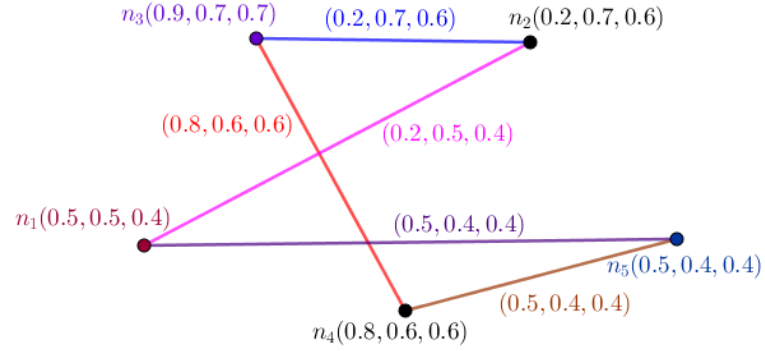


Figure 15. A Neutrosophic Graph in the Viewpoint of its total-dominating number and its neutrosophic total-dominating number.

(vi) all total-dominating sets corresponded to total-dominating number are

$$\{n_1, n_2, n_5\}, \{n_2, n_3, n_1\}, \{n_3, n_4, n_2\}, \\ \{n_4, n_5, n_3\}, \{n_5, n_1, n_4\},$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum neutrosophic cardinality between all total-dominating sets is called neutrosophic total-dominating number and it's denoted by $\mathcal{T}_n(CYC) = 4.2$ and corresponded to total-dominating sets are

$$\{n_1, n_2, n_5\}.$$

Proposition 3.12. Let $NTG : (V, E, \sigma, \mu)$ be a star-neutrosophic graph with center c . Then

$$\mathcal{T}_n(STR_{1,\sigma_2}) = \min_{x \in V} \sum_{i=1}^3 (\sigma_i(c) + \sigma_i(x)).$$

Proof. Suppose $STR_{1,\sigma_2} : (V, E, \sigma, \mu)$ is a star-neutrosophic graph. An edge always has center, c , as one of its endpoints. All paths have one as their lengths, forever. in the

setting of star, a vertex of dominating set corresponded to dominating number dominates as if it doesn't total-dominate since a vertex couldn't dominate itself. Thus two neighbors are necessary in S . All total-dominating sets corresponded to total-dominating number are

$$\{c(n_1), n_2\}, \{c(n_1), n_3\}, \{c(n_1), n_4\}, \dots, \{c(n_1), n_{\mathcal{O}(STR_{1,\sigma_2})-1}\}, \{c(n_1), n_{\mathcal{O}(STR_{1,\sigma_2})}\}.$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum neutrosophic cardinality between all total-dominating sets is called neutrosophic total-dominating number and it's denoted by

$$\mathcal{T}_n(STR_{1,\sigma_2}) = \min_{x \in V} \sum_{i=1}^3 (\sigma_i(c) + \sigma_i(x))$$

and corresponded to total-dominating sets are

$$\{c(n_1), n_2\}, \{c(n_1), n_3\}, \{c(n_1), n_4\}, \dots, \{c(n_1), n_{\mathcal{O}(STR_{1,\sigma_2})-1}\}, \{c(n_1), n_{\mathcal{O}(STR_{1,\sigma_2})}\}.$$

Thus

$$\mathcal{T}_n(STR_{1,\sigma_2}) = \min_{x \in V} \sum_{i=1}^3 (\sigma_i(c) + \sigma_i(x)).$$

□

Proposition 3.13. *Let $NTG : (V, E, \sigma, \mu)$ be a star-neutrosophic graph. Then total-dominating number isn't equal to dominating number.*

Proposition 3.14. *Let $NTG : (V, E, \sigma, \mu)$ be a star-neutrosophic graph with center c . Then there are $2^{\mathcal{O}(STR_{1,\sigma_2})-1} - 2$ total-dominating sets.*

Proposition 3.15. *Let $NTG : (V, E, \sigma, \mu)$ be a star-neutrosophic graph with center c . Then there are $\mathcal{O}(STR_{1,\sigma_2}) - 1$ total-dominating sets corresponded to total-dominating number.*

The clarifications about results are in progress as follows. A star-neutrosophic graph is related to previous result and it's studied to apply the definitions on it. To make it more clear, next part gives one special case to apply definitions and results on it. Some items are devised to make more sense about new notions. A star-neutrosophic graph is related to previous result and it's studied to apply the definitions on it, too.

Example 3.16. There is one section for clarifications. In Figure (16), a star-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows.

- (i) For given two neutrosophic vertices, s and n_1 , there's only one path, precisely one edge between them and there's no path despite them;
- (ii) in the setting of star, a vertex of dominating set corresponded to dominating number dominates as if it doesn't total-dominate since a vertex couldn't dominate itself. Thus two neighbors are necessary in S ;
- (iii) all total-dominating sets corresponded to total-dominating number are

$$\begin{aligned} &\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ &\{n_1, n_5\}, \end{aligned}$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum cardinality between all total-dominating sets is called total-dominating number and it's denoted by $\mathcal{T}(STR_{1,\sigma_2}) = 2$ and corresponded to total-dominating sets are

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ \{n_1, n_5\};$$

(iv) there are fourteen total-dominating sets

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ \{n_1, n_5\}, \{n_1, n_2, n_3\}, \{n_1, n_2, n_4\}, \\ \{n_1, n_2, n_5\}, \{n_1, n_3, n_4\}, \{n_1, n_3, n_5\}, \\ \{n_1, n_4, n_5\}, \{n_1, n_2, n_3, n_4\}, \{n_1, n_2, n_3, n_5\}, \\ \{n_1, n_3, n_4, n_5\}, \{n_1, n_2, n_3, n_4, n_5\},$$

as if it's possible to have one of them as a set corresponded to neutrosophic total-dominating number so as neutrosophic cardinality is characteristic;

(v) there are four total-dominating sets

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ \{n_1, n_5\},$$

corresponded to total-dominating number as if there's one total-dominating set corresponded to neutrosophic total-dominating number so as neutrosophic cardinality is the determiner;

(vi) all total-dominating sets corresponded to total-dominating number are

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ \{n_1, n_5\},$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum neutrosophic cardinality between all total-dominating sets is called neutrosophic total-dominating number and it's denoted by $\mathcal{T}_n(STR_{1,\sigma_2}) = 2.9$ and corresponded to total-dominating sets are

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ \{n_1, n_5\}.$$

Proposition 3.17. *Let $NTG : (V, E, \sigma, \mu)$ be a complete-bipartite-neutrosophic graph which isn't star-neutrosophic graph which means $|V_1|, |V_2| \geq 2$. Then*

$$\mathcal{T}_n(CMC_{\sigma_1, \sigma_2}) = \min_{x \in V_1, y \in V_2} \sum_{i=1}^3 (\sigma_i(x) + \sigma_i(y)).$$

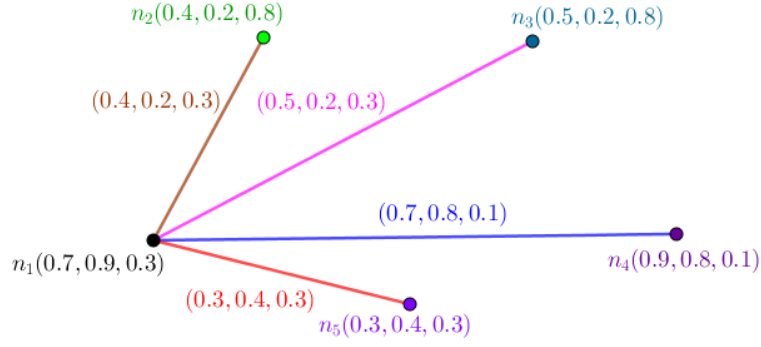


Figure 16. A Neutrosophic Graph in the Viewpoint of its total-dominating number and its neutrosophic total-dominating number.

Proof. Suppose $CMC_{\sigma_1, \sigma_2} : (V, E, \sigma, \mu)$ is a complete-bipartite-neutrosophic graph. Every vertex in a part and another vertex in opposite part total-dominates any given vertex. Assume same parity for same partition of vertex set which means V_1 has odd indexes and V_2 has even indexes. In the setting of complete-bipartite, a vertex of dominating set corresponded to dominating number dominates if and only if it total-dominates since a vertex couldn't dominate itself. Thus two neighbors are necessary in S . All total-dominating sets corresponded to total-dominating number are

$$\begin{aligned} & \{n_1, n_2\}, \{n_1, n_4\}, \dots, \{n_1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-4}\}, \{n_1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-2}\}, \{n_1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})}\}, \\ & \{n_3, n_2\}, \{n_3, n_4\}, \dots, \{n_3, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-4}\}, \{n_3, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-2}\}, \{n_3, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})}\}, \\ & \dots \\ & \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-1}, n_2\}, \dots, \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-1}, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})}\}, \\ & \{n_2, n_1\}, \{n_2, n_3\}, \dots, \{n_2, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-5}\}, \{n_2, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-3}\}, \{n_2, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-1}\}, \\ & \{n_4, n_1\}, \{n_4, n_3\}, \dots, \{n_4, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-5}\}, \{n_4, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-3}\}, \{n_4, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-1}\}, \\ & \dots \\ & \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})}, n_1\}, \dots, \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})}, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-3}\}, \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})}, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-1}\}. \end{aligned}$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum neutrosophic cardinality between all total-dominating sets is called neutrosophic total-dominating number and it's denoted by

$$\mathcal{T}_n(CMC_{\sigma_1, \sigma_2}) = \min_{x \in V_1, y \in V_2} \sum_{i=1}^3 (\sigma_i(x) + \sigma_i(y))$$

and corresponded to total-dominating sets are

$$\begin{aligned} & \{n_1, n_2\}, \{n_1, n_4\}, \dots, \{n_1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-4}\}, \{n_1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-2}\}, \{n_1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})}\}, \\ & \{n_3, n_2\}, \{n_3, n_4\}, \dots, \{n_3, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-4}\}, \{n_3, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-2}\}, \{n_3, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})}\}, \\ & \dots \\ & \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-1}, n_2\}, \dots, \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-1}, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})}\}, \\ & \{n_2, n_1\}, \{n_2, n_3\}, \dots, \{n_2, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-5}\}, \{n_2, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-3}\}, \{n_2, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-1}\}, \\ & \{n_4, n_1\}, \{n_4, n_3\}, \dots, \{n_4, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-5}\}, \{n_4, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-3}\}, \{n_4, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-1}\}, \\ & \dots \\ & \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})}, n_1\}, \dots, \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})}, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-3}\}, \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})}, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-1}\}, \end{aligned}$$

Thus

$$\mathcal{T}_n(CMC_{\sigma_1, \sigma_2}) = \min_{x \in V_1, y \in V_2} \sum_{i=1}^3 (\sigma_i(x) + \sigma_i(y)).$$

□ 884

Proposition 3.18. *Let $NTG : (V, E, \sigma, \mu)$ be a complete-bipartite-neutrosophic graph. Then total-dominating number is equal to dominating number.* 885 886

Proposition 3.19. *Let $NTG : (V, E, \sigma, \mu)$ be a complete-bipartite-neutrosophic graph. Then there are at least $2^{\mathcal{O}(CMC_{\sigma_1, \sigma_2})-2} - 1 + |V_1| \times |V_2|$ total-dominating sets.* 887 888

Proposition 3.20. *Let $NTG : (V, E, \sigma, \mu)$ be a complete-bipartite-neutrosophic graph. Then there are $|V_1| \times |V_2|$ total-dominating sets corresponded to total-dominating number.* 889 890

The clarifications about results are in progress as follows. A complete-bipartite-neutrosophic graph is related to previous result and it's studied to apply the definitions on it. To make it more clear, next part gives one special case to apply definitions and results on it. Some items are devised to make more senses about new notions. A complete-bipartite-neutrosophic graph is related to previous result and it's studied to apply the definitions on it, too. 891 892 893 894 895 896

Example 3.21. There is one section for clarifications. In Figure (17), a complete-bipartite-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows. 897 898 899

- (i) For given two neutrosophic vertices, n and n' , there is either one path with length one or one path with length two between them; 900 901
- (ii) in the setting of complete-bipartite, a vertex of dominating set corresponded to dominating number dominates if and only if it total-dominates since a vertex couldn't dominate itself. Thus two neighbors are necessary in S ; 902 903 904
- (iii) all total-dominating sets corresponded to total-dominating number are 905

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_4, n_2\}, \\ \{n_4, n_3\},$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum cardinality between all total-dominating sets is called total-dominating number and it's denoted by $\mathcal{T}(CMC_{\sigma_1, \sigma_2}) = 2$ and corresponded to total-dominating sets are 906 907 908 909 910 911 912

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_4, n_2\}, \\ \{n_4, n_3\};$$

- (iv) there are nine total-dominating sets 913

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_4, n_2\}, \\ \{n_4, n_3\}, \{n_1, n_2, n_3\}, \{n_1, n_2, n_4\}, \\ \{n_1, n_3, n_4\}, \{n_4, n_2, n_3\}, \{n_1, n_2, n_3, n_4\},$$

as if it's possible to have one of them as a set corresponded to neutrosophic total-dominating number so as neutrosophic cardinality is characteristic; 914 915

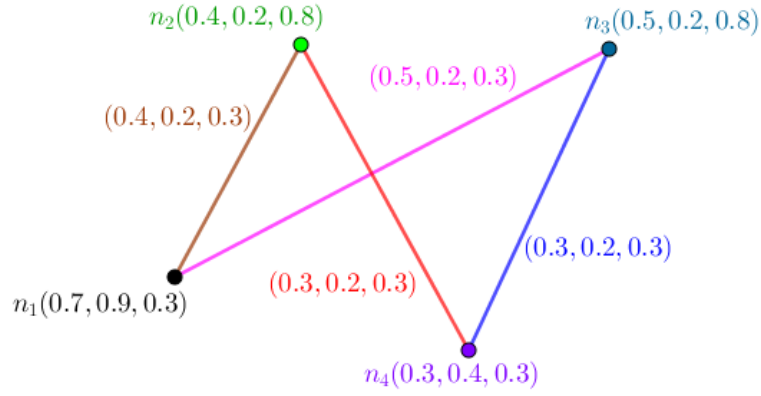


Figure 17. A Neutrosophic Graph in the Viewpoint of its total-dominating number and its neutrosophic total-dominating number.

(v) there are four total-dominating sets

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_4, n_2\}, \\ \{n_4, n_3\},$$

corresponded to total-dominating number as if there's one total-dominating set
corresponded to neutrosophic total-dominating number so as neutrosophic
cardinality is the determiner;

(vi) all total-dominating sets corresponded to total-dominating number are

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_4, n_2\}, \\ \{n_4, n_3\},$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of
neutrosophic vertices [a vertex alongside triple pair of its values is called
neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a
neutrosophic vertex s in S such that s total-dominates n , then the set of
neutrosophic vertices, S is called total-dominating set. The minimum
neutrosophic cardinality between all total-dominating sets is called neutrosophic
total-dominating number and it's denoted by $\mathcal{T}_n(CMC_{\sigma_1, \sigma_2}) = 2.4$ and
corresponded to total-dominating sets are

$$\{n_4, n_2\}.$$

Proposition 3.22. Let $NTG : (V, E, \sigma, \mu)$ be a complete- t -partite-neutrosophic graph
where $t \geq 3$. Then

$$\mathcal{T}_n(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t}) = \min_{x \in V_i, y \in V_j} \sum_{i=1}^3 (\sigma_i(x) + \sigma_i(y)).$$

Proof. Suppose $CMC_{\sigma_1, \sigma_2, \dots, \sigma_t} : (V, E, \sigma, \mu)$ is a complete- t -partite-neutrosophic graph.
Every vertex in a part is total-dominated by another vertex in another part. In the
setting of complete- t -partite, a vertex of dominating set corresponded to dominating
number dominates if and only if it total-dominates since a vertex couldn't dominate
itself. Thus two neighbors are necessary in S . Two vertices from different parts are

neighbors and they total-dominates all vertices. All total-dominating sets corresponded to total-dominating number are

$$\begin{aligned}
& \{n_1^1, n_1^2\}, \{n_1^1, n_1^3\}, \dots, \{n_1^1, n_1^t\}, \\
& \{n_1^1, n_2^2\}, \{n_1^1, n_2^3\}, \dots, \{n_1^1, n_2^t\}, \\
& \dots \\
& \{n_1^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^2\}, \{n_1^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^3\}, \dots, \{n_1^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^t\}, \\
& \{n_2^1, n_1^2\}, \{n_2^1, n_1^3\}, \dots, \{n_2^1, n_1^t\}, \\
& \{n_2^1, n_2^2\}, \{n_2^1, n_2^3\}, \dots, \{n_2^1, n_2^t\}, \\
& \dots \\
& \{n_2^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^2\}, \{n_2^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^3\}, \dots, \{n_2^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^t\}, \\
& \dots \\
& \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_1^2\}, \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_1^3\}, \dots, \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_1^t\}, \\
& \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_2^2\}, \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_2^3\}, \dots, \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_2^t\}, \\
& \dots \\
& \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^2\}, \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^3\}, \dots, \\
& \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^t\},
\end{aligned}$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum neutrosophic cardinality between all total-dominating sets is called neutrosophic total-dominating number and it's denoted by

$$\mathcal{T}_n(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t}) = \min_{x \in V_i, y \in V_j} \sum_{i=1}^3 (\sigma_i(x) + \sigma_i(y))$$

and corresponded to total-dominating sets are

$$\begin{aligned}
& \{n_1^1, n_1^2\}, \{n_1^1, n_1^3\}, \dots, \{n_1^1, n_1^t\}, \\
& \{n_1^1, n_2^2\}, \{n_1^1, n_2^3\}, \dots, \{n_1^1, n_2^t\}, \\
& \dots \\
& \{n_1^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^2\}, \{n_1^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^3\}, \dots, \{n_1^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^t\}, \\
& \{n_2^1, n_1^2\}, \{n_2^1, n_1^3\}, \dots, \{n_2^1, n_1^t\}, \\
& \{n_2^1, n_2^2\}, \{n_2^1, n_2^3\}, \dots, \{n_2^1, n_2^t\}, \\
& \dots \\
& \{n_2^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^2\}, \{n_2^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^3\}, \dots, \{n_2^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^t\}, \\
& \dots \\
& \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_1^2\}, \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_1^3\}, \dots, \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_1^t\}, \\
& \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_2^2\}, \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_2^3\}, \dots, \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_2^t\}, \\
& \dots \\
& \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^2\}, \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^3\}, \dots, \\
& \{n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^1, n_{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})}^t\},
\end{aligned}$$

Thus

$$\mathcal{T}_n(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t}) = \min_{x \in V_i, y \in V_j} \sum_{i=1}^3 (\sigma_i(x) + \sigma_i(y)).$$

□ 937

Proposition 3.23. *Let $NTG : (V, E, \sigma, \mu)$ be a complete-t-partite-neutrosophic graph. Then total-dominating number is equal to dominating number.* 938 939

Proposition 3.24. *Let $NTG : (V, E, \sigma, \mu)$ be a complete-t-partite-neutrosophic graph. Then there are at least $2^{\mathcal{O}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t})-2} - 1$ total-dominating sets.* 940 941

Proposition 3.25. *Let $NTG : (V, E, \sigma, \mu)$ be a complete-t-partite-neutrosophic graph. Then there are at least $|V_1| \times |V_2|$ total-dominating sets corresponded to total-dominating number.* 942 943 944

The clarifications about results are in progress as follows. A complete-t-partite-neutrosophic graph is related to previous result and it's studied to apply the definitions on it. To make it more clear, next part gives one special case to apply definitions and results on it. Some items are devised to make more sense about new notions. A complete-t-partite-neutrosophic graph is related to previous result and it's studied to apply the definitions on it, too. 945 946 947 948 949 950

Example 3.26. There is one section for clarifications. In Figure (18), a complete-t-partite-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows. 951 952 953

- (i) For given two neutrosophic vertices, n and n' , there is either one path with length one or one path with length two between them; 954 955
- (ii) in the setting of complete-t-partite, a vertex of dominating set corresponded to dominating number dominates if and only if it total-dominates since a vertex couldn't dominate itself. Thus two neighbors are necessary in S . Two vertices from different parts are neighbors and they total-dominates all vertices; 956 957 958 959
- (iii) all total-dominating sets corresponded to total-dominating number are 960

$$\begin{aligned} &\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_5\}, \\ &\{n_4, n_2\}, \{n_4, n_3\}, \{n_4, n_5\}, \end{aligned}$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum cardinality between all total-dominating sets is called total-dominating number and it's denoted by $\mathcal{T}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t}) = 2$ and corresponded to total-dominating sets are 961 962 963 964 965 966 967

$$\begin{aligned} &\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_5\}, \\ &\{n_4, n_2\}, \{n_4, n_3\}, \{n_4, n_5\}; \end{aligned}$$

(iv) there are twenty-one total-dominating sets

$$\begin{aligned} &\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_5\}, \\ &\{n_4, n_2\}, \{n_4, n_3\}, \{n_4, n_5\}, \\ &\{n_1, n_2, n_3\}, \{n_1, n_2, n_4\}, \{n_1, n_2, n_5\}, \\ &\{n_1, n_3, n_4\}, \{n_1, n_3, n_5\}, \{n_1, n_5, n_4\}, \\ &\{n_4, n_2, n_3\}, \{n_4, n_2, n_5\}, \{n_4, n_3, n_5\}, \\ &\{n_1, n_2, n_3, n_4\}, \{n_1, n_2, n_3, n_5\}, \{n_1, n_2, n_4, n_5\}, \\ &\{n_1, n_3, n_4, n_5\}, \{n_2, n_3, n_4, n_5\}, \{n_1, n_2, n_3, n_4, n_5\}, \end{aligned}$$

as if it's possible to have one of them as a set corresponded to neutrosophic total-dominating number so as neutrosophic cardinality is characteristic;

(v) there are six total-dominating sets

$$\begin{aligned} &\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_5\}, \\ &\{n_4, n_2\}, \{n_4, n_3\}, \{n_4, n_5\}, \end{aligned}$$

corresponded to total-dominating number as if there's one total-dominating set corresponded to neutrosophic total-dominating number so as neutrosophic cardinality is the determiner;

(vi) all total-dominating sets corresponded to total-dominating number are

$$\begin{aligned} &\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_5\}, \\ &\{n_4, n_2\}, \{n_4, n_3\}, \{n_4, n_5\}. \end{aligned}$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum neutrosophic cardinality between all total-dominating sets is called neutrosophic total-dominating number and it's denoted by $\mathcal{T}_n(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t}) = 2.4$ and corresponded to total-dominating sets are

$$\{n_4, n_2\}, \{n_4, n_5\}.$$

Proposition 3.27. *Let $NTG : (V, E, \sigma, \mu)$ be a wheel-neutrosophic graph. Then*

$$\mathcal{T}_n(WHL_{1, \sigma_2}) = \min_{x \in V} \sum_{i=1}^3 (\sigma_i(c) + \sigma_i(x)).$$

Proof. Suppose $WHL_{1, \sigma_2} : (V, E, \sigma, \mu)$ is a wheel-neutrosophic graph. The argument is elementary. All vertices of a cycle join to one vertex, c . For every vertices, the minimum number of edges amid them is either one or two because of center and the notion of neighbors. In the setting of wheel, a vertex of dominating set corresponded to dominating number dominates as if it doesn't total-dominate since a vertex couldn't dominate itself. Thus two neighbors are necessary in S . Two vertices including center and other vertex are neighbors and they total-dominates all vertices. All total-dominating sets corresponded to total-dominating number are

$$\{n_1(c), n_2\}, \{n_1(c), n_3\}, \{n_1(c), n_4\}, \dots, \{n_1(c), n_{\mathcal{O}(WHL_{1, \sigma_2})-1}\}, \{n_1(c), n_{\mathcal{O}(WHL_{1, \sigma_2})}\}.$$

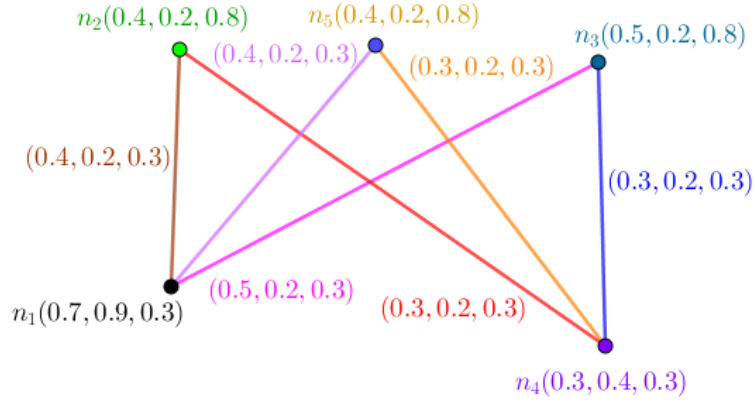


Figure 18. A Neutrosophic Graph in the Viewpoint of its total-dominating number and its neutrosophic total-dominating number.

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum neutrosophic cardinality between all total-dominating sets is called neutrosophic total-dominating number and it's denoted by

$$\mathcal{T}_n(WHL_{1,\sigma_2}) = \min_{x \in V} \sum_{i=1}^3 (\sigma_i(c) + \sigma_i(x))$$

and corresponded to total-dominating sets are

$$\{n_1(c), n_2\}, \{n_1(c), n_3\}, \{n_1(c), n_4\}, \dots, \{n_1(c), n_{\mathcal{O}(WHL_{1,\sigma_2})-1}\}, \{n_1(c), n_{\mathcal{O}(WHL_{1,\sigma_2})}\}.$$

Thus

$$\mathcal{T}_n(WHL_{1,\sigma_2}) = \min_{x \in V} \sum_{i=1}^3 (\sigma_i(c) + \sigma_i(x)).$$

□ 993

Proposition 3.28. Let $NTG : (V, E, \sigma, \mu)$ be a wheel-neutrosophic graph. Then total-dominating number isn't equal to dominating number.

Proposition 3.29. Let $NTG : (V, E, \sigma, \mu)$ be a wheel-neutrosophic graph with center c . Then there are $2^{\mathcal{O}(WHL_{1,\sigma_2})-1} - 1$ total-dominating sets.

Proposition 3.30. Let $NTG : (V, E, \sigma, \mu)$ be a wheel-neutrosophic graph with center c . Then there are $\mathcal{O}(WHL_{1,\sigma_2})$ total-dominating sets corresponded to total-dominating number.

The clarifications about results are in progress as follows. A wheel-neutrosophic graph is related to previous result and it's studied to apply the definitions on it. To make it more clear, next part gives one special case to apply definitions and results on it. Some items are devised to make more sense about new notions. A wheel-neutrosophic graph is related to previous result and it's studied to apply the definitions on it, too.

Example 3.31. There is one section for clarifications. In Figure (19), a wheel-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows.

- (i) For given two neutrosophic vertices, s and n_1 , there's only one edge between them; 1009
- (ii) in the setting of wheel, a vertex of dominating set corresponded to dominating number dominates as if it doesn't total-dominate since a vertex couldn't dominate itself. Thus two neighbors are necessary in S . Two vertices including center and other vertex are neighbors and they total-dominates all vertices; 1010
1011
1012
1013
- (iii) all total-dominating sets corresponded to total-dominating number are 1014

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ \{n_1, n_5\}.$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum cardinality between all total-dominating sets is called total-dominating number and it's denoted by $\mathcal{T}(WHL_{1,\sigma_2}) = 2$ and corresponded to total-dominating sets are 1015
1016
1017
1018
1019
1020
1021

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ \{n_1, n_5\};$$

- (iv) there are fifteen total-dominating sets 1022

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ \{n_1, n_5\}, \{n_1, n_2, n_3\}, \{n_1, n_2, n_4\}, \\ \{n_1, n_2, n_5\}, \{n_1, n_3, n_4\}, \{n_1, n_3, n_5\}, \\ \{n_1, n_4, n_5\}, \{n_1, n_2, n_3, n_4\}, \{n_1, n_2, n_3, n_5\}, \\ \{n_1, n_2, n_4, n_5\}, \{n_1, n_3, n_4, n_5\}, \{n_1, n_2, n_3, n_4, n_5\},$$

as if it's possible to have one of them as a set corresponded to neutrosophic total-dominating number so as neutrosophic cardinality is characteristic; 1023
1024

- (v) there are four total-dominating sets 1025

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ \{n_1, n_5\},$$

corresponded to total-dominating number as if there's one total-dominating set corresponded to neutrosophic total-dominating number so as neutrosophic cardinality is the determiner; 1026
1027
1028

- (vi) all total-dominating sets corresponded to total-dominating number are 1029

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ \{n_1, n_5\}.$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum neutrosophic cardinality between all total-dominating sets is called neutrosophic total-dominating number and it's denoted by $\mathcal{T}_n(WHL_{1,\sigma_2}) = 2.9$ and corresponded to total-dominating sets are 1030
1031
1032
1033
1034
1035
1036
1037

$$\{n_1, n_4\}.$$

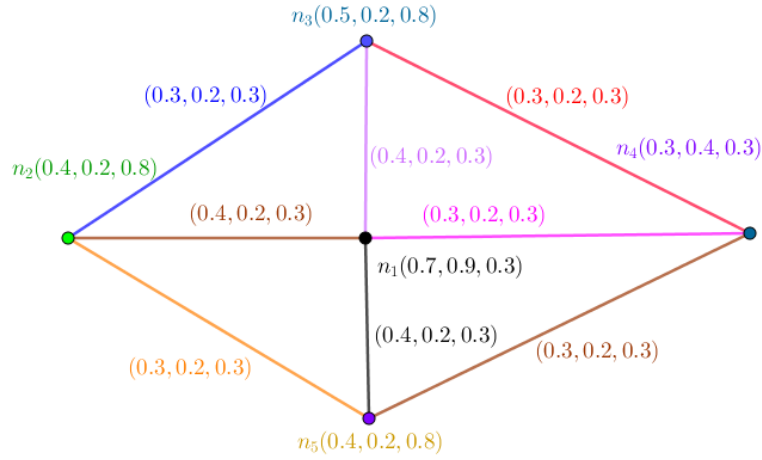


Figure 19. A Neutrosophic Graph in the Viewpoint of its total-dominating number and its neutrosophic total-dominating number.

4 Applications in Time Table and Scheduling

In this section, two applications for time table and scheduling are provided where the models are either complete models which mean complete connections are formed as individual and family of complete models with common neutrosophic vertex set or quasi-complete models which mean quasi-complete connections are formed as individual and family of quasi-complete models with common neutrosophic vertex set.

Designing the programs to achieve some goals is general approach to apply on some issues to function properly. Separation has key role in the context of this style. Separating the duration of work which are consecutive, is the matter and it has importance to avoid mixing up.

Step 1. (Definition) Time table is an approach to get some attributes to do the work fast and proper. The style of scheduling implies special attention to the tasks which are consecutive.

Step 2. (Issue) Scheduling of program has faced with difficulties to differ amid consecutive sections. Beyond that, sometimes sections are not the same.

Step 3. (Model) The situation is designed as a model. The model uses data to assign every section and to assign to relation amid sections, three numbers belong unit interval to state indeterminacy, possibilities and determinacy. There's one restriction in that, the numbers amid two sections are at least the number of the relations amid them. Table (1), clarifies about the assigned numbers to these situations.

Table 1. Scheduling concerns its Subjects and its Connections as a neutrosophic graph in a Model.

Sections of NTG	n_1	$n_2 \cdots$	n_5
Values	$(0.7, 0.9, 0.3)$	$(0.4, 0.2, 0.8) \cdots$	$(0.4, 0.2, 0.8)$
Connections of NTG	E_1	$E_2 \cdots$	E_6
Values	$(0.4, 0.2, 0.3)$	$(0.5, 0.2, 0.3) \cdots$	$(0.3, 0.2, 0.3)$

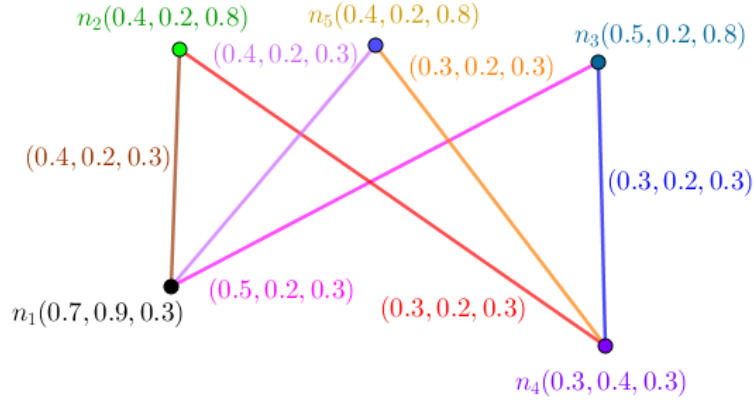


Figure 20. A Neutrosophic Graph in the Viewpoint of its total-dominating number and its neutrosophic total-dominating number

4.1 Case 1: Complete-t-partite Model alongside its total-dominating number and its neutrosophic total-dominating number

Step 4. (Solution) The neutrosophic graph alongside its total-dominating number and its neutrosophic total-dominating number as model, propose to use specific number. Every subject has connection with some subjects. Thus the connection is applied as possible and the model demonstrates quasi-full connections as quasi-possible. Using the notion of strong on the connection amid subjects, causes the importance of subject goes in the highest level such that the value amid two consecutive subjects, is determined by those subjects. If the configuration is star, the number is different. Also, it holds for other types such that complete, wheel, path, and cycle. The collection of situations is another application of its total-dominating number and its neutrosophic total-dominating number when the notion of family is applied in the way that all members of family are from same classes of neutrosophic graphs. As follows, there are five subjects which are represented as Figure (20). This model is strong and even more it's quasi-complete. And the study proposes using specific number which is called its total-dominating number and its neutrosophic total-dominating number. There are also some analyses on other numbers in the way that, the clarification is gained about being special number or not. Also, in the last part, there is one neutrosophic number to assign to this model and situation to compare them with same situations to get more precise. Consider Figure (20). In Figure (20), an complete-t-partite-neutrosophic graph is illustrated. Some points are represented in follow-up items as follows.

- (i) For given two neutrosophic vertices, n and n' , there is either one path with length one or one path with length two between them;
- (ii) in the setting of complete-t-partite, a vertex of dominating set corresponded to dominating number dominates if and only if it total-dominates since a vertex couldn't dominate itself. Thus two neighbors are necessary in S . Two vertices from different parts are neighbors and they total-dominates all vertices;

(iii) all total-dominating sets corresponded to total-dominating number are 1090

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_5\}, \\ \{n_4, n_2\}, \{n_4, n_3\}, \{n_4, n_5\},$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of 1091
neutrosophic vertices [a vertex alongside triple pair of its values is called 1092
neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least 1093
a neutrosophic vertex s in S such that s total-dominates n , then the set of 1094
neutrosophic vertices, S is called total-dominating set. The minimum 1095
cardinality between all total-dominating sets is called total-dominating 1096
number and it's denoted by $\mathcal{T}(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t}) = 2$ and corresponded to 1097
total-dominating sets are 1098

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_5\}, \\ \{n_4, n_2\}, \{n_4, n_3\}, \{n_4, n_5\};$$

(iv) there are twenty-one total-dominating sets 1099

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_5\}, \\ \{n_4, n_2\}, \{n_4, n_3\}, \{n_4, n_5\}, \\ \{n_1, n_2, n_3\}, \{n_1, n_2, n_4\}, \{n_1, n_2, n_5\}, \\ \{n_1, n_3, n_4\}, \{n_1, n_3, n_5\}, \{n_1, n_5, n_4\}, \\ \{n_4, n_2, n_3\}, \{n_4, n_2, n_5\}, \{n_4, n_3, n_5\}, \\ \{n_1, n_2, n_3, n_4\}, \{n_1, n_2, n_3, n_5\}, \{n_1, n_2, n_4, n_5\}, \\ \{n_1, n_3, n_4, n_5\}, \{n_2, n_3, n_4, n_5\}, \{n_1, n_2, n_3, n_4, n_5\},$$

as if it's possible to have one of them as a set corresponded to neutrosophic 1100
total-dominating number so as neutrosophic cardinality is characteristic; 1101

(v) there are six total-dominating sets 1102

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_5\}, \\ \{n_4, n_2\}, \{n_4, n_3\}, \{n_4, n_5\},$$

corresponded to total-dominating number as if there's one total-dominating 1103
set corresponded to neutrosophic total-dominating number so as 1104
neutrosophic cardinality is the determiner; 1105

(vi) all total-dominating sets corresponded to total-dominating number are 1106

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_5\}, \\ \{n_4, n_2\}, \{n_4, n_3\}, \{n_4, n_5\}.$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of 1107
neutrosophic vertices [a vertex alongside triple pair of its values is called 1108
neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least 1109
a neutrosophic vertex s in S such that s total-dominates n , then the set of 1110
neutrosophic vertices, S is called total-dominating set. The minimum 1111
neutrosophic cardinality between all total-dominating sets is called 1112
neutrosophic total-dominating number and it's denoted by 1113
 $\mathcal{T}_n(CMC_{\sigma_1, \sigma_2, \dots, \sigma_t}) = 2.4$ and corresponded to total-dominating sets are 1114

$$\{n_4, n_2\}, \{n_4, n_5\}.$$

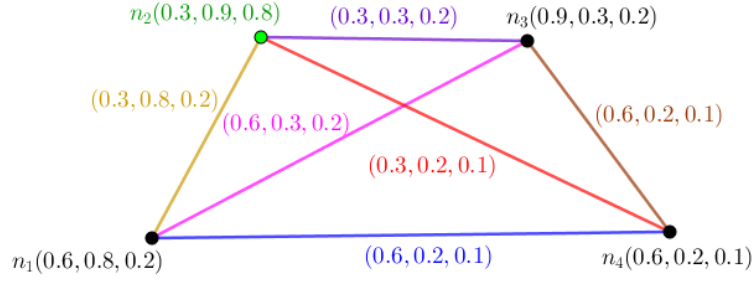


Figure 21. A Neutrosophic Graph in the Viewpoint of its total-dominating number and its neutrosophic total-dominating number

4.2 Case 2: Complete Model alongside its Neutrosophic Graph in the Viewpoint of its total-dominating number and its neutrosophic total-dominating number

Step 4. (Solution) The neutrosophic graph alongside its total-dominating number and its neutrosophic total-dominating number as model, propose to use specific number. Every subject has connection with every given subject in deemed way. Thus the connection applied as possible and the model demonstrates full connections as possible between parts but with different view where symmetry amid vertices and edges are the matters. Using the notion of strong on the connection amid subjects, causes the importance of subject goes in the highest level such that the value amid two consecutive subjects, is determined by those subjects. If the configuration is complete multipartite, the number is different. Also, it holds for other types such that star, wheel, path, and cycle. The collection of situations is another application of its total-dominating number and its neutrosophic total-dominating number when the notion of family is applied in the way that all members of family are from same classes of neutrosophic graphs. As follows, there are four subjects which are represented in the formation of one model as Figure (21). This model is neutrosophic strong as individual and even more it's complete. And the study proposes using specific number which is called its total-dominating number and its neutrosophic total-dominating number for this model. There are also some analyses on other numbers in the way that, the clarification is gained about being special number or not. Also, in the last part, there is one neutrosophic number to assign to these models as individual. A model as a collection of situations to compare them with another model as a collection of situations to get more precise. Consider Figure (21). There is one section for clarifications.

- (i) For given neutrosophic vertex, s , there's an edge with other vertices;
- (ii) in the setting of complete, a vertex of dominating set corresponded to dominating number dominates as if it doesn't total-dominate since a vertex couldn't dominate itself;
- (iii) all total-dominating sets corresponded to total-dominating number are

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ \{n_2, n_3\}, \{n_2, n_4\}, \{n_3, n_4\}.$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least

a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum cardinality between all total-dominating sets is called total-dominating number and it's denoted by $\mathcal{T}(CMT_\sigma) = 2$ and corresponded to total-dominating sets are

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ \{n_2, n_3\}, \{n_2, n_4\}, \{n_3, n_4\};$$

(iv) there are eleven total-dominating sets

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ \{n_2, n_3\}, \{n_2, n_4\}, \{n_3, n_4\}, \\ \{n_1, n_2, n_3\}, \{n_1, n_2, n_4\}, \{n_1, n_3, n_4\}, \\ \{n_2, n_3, n_4\}, \{n_1, n_2, n_3, n_4\},$$

as if it's possible to have one of them as a set corresponded to neutrosophic total-dominating number so as neutrosophic cardinality is characteristic;

(v) there are six total-dominating sets

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ \{n_2, n_3\}, \{n_2, n_4\}, \{n_3, n_4\},$$

corresponded to total-dominating number as if there's one total-dominating set corresponded to neutrosophic total-dominating number so as neutrosophic cardinality is the determiner;

(vi) all total-dominating sets corresponded to total-dominating number are

$$\{n_1, n_2\}, \{n_1, n_3\}, \{n_1, n_4\}, \\ \{n_2, n_3\}, \{n_2, n_4\}, \{n_3, n_4\}.$$

For given vertex n , if $sn \in E$, then s total-dominates n . Let S be a set of neutrosophic vertices [a vertex alongside triple pair of its values is called neutrosophic vertex.]. If for every neutrosophic vertex n in V , there's at least a neutrosophic vertex s in S such that s total-dominates n , then the set of neutrosophic vertices, S is called total-dominating set. The minimum neutrosophic cardinality between all total-dominating sets is called neutrosophic total-dominating number and it's denoted by $\mathcal{T}_n(CMT_\sigma) = 2.3$ and corresponded to neutrosophic total-dominating sets are

$$\{n_3, n_4\}.$$

5 Open Problems

In this section, some questions and problems are proposed to give some avenues to pursue this study. The structures of the definitions and results give some ideas to make new settings which are eligible to extend and to create new study.

Notion concerning its total-dominating number and its neutrosophic total-dominating number are defined in neutrosophic graphs. Thus,

Question 5.1. *Is it possible to use other types of its total-dominating number and its neutrosophic total-dominating number?*

- Question 5.2.** *Are existed some connections amid different types of its total-dominating number and its neutrosophic total-dominating number in neutrosophic graphs?*
- Question 5.3.** *Is it possible to construct some classes of neutrosophic graphs which have “nice” behavior?*
- Question 5.4.** *Which mathematical notions do make an independent study to apply these types in neutrosophic graphs?*
- Problem 5.5.** *Which parameters are related to this parameter?*
- Problem 5.6.** *Which approaches do work to construct applications to create independent study?*
- Problem 5.7.** *Which approaches do work to construct definitions which use all definitions and the relations amid them instead of separate definitions to create independent study?*

6 Conclusion and Closing Remarks

In this section, concluding remarks and closing remarks are represented. The drawbacks of this article are illustrated. Some benefits and advantages of this study are highlighted.

This study uses two definitions concerning total-dominating number and neutrosophic total-dominating number arising from total-dominated vertices in neutrosophic graphs assigned to neutrosophic graphs. Minimum number of total-dominated vertices, is a number which is representative based on those vertices. Minimum neutrosophic number of total-dominated vertices corresponded to total-dominating set is called neutrosophic total-dominating number. The connections of vertices which aren’t clarified by minimum number of edges amid them differ them from each other and put them in different categories to represent a number which is

Table 2. A Brief Overview about Advantages and Limitations of this Study

Advantages	Limitations
1. Total-Dominating Number of Model	1. Connections amid Classes
2. Neutrosophic Total-Dominating Number of Model	
3. Minimal Total-Dominating Sets	2. Study on Families
4. Total-Dominated Vertices amid all Vertices	
5. Acting on All Vertices	3. Same Models in Family

called total-dominating number and neutrosophic total-dominating number arising from total-dominated vertices in neutrosophic graphs assigned to neutrosophic graphs. Further studies could be about changes in the settings to compare these notions amid different settings of neutrosophic graphs theory. One way is finding some relations amid all definitions of notions to make sensible definitions. In Table (2), some limitations and advantages of this study are pointed out.

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