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## On Solving Transportation Problem Based on Interval Valued Pythagorean Octagonal Neutrosophic Fuzzy Number

R. Narmada Devi<sup>1</sup> and S. Sowmiya<sup>2</sup>

<sup>1</sup> Associate Professor, Department of Mathematics, Vel Tech Rangarajan Dr. Sanguthala R&D Institute of Science and Technology, Chennai, Tamil Nadu, India;

<sup>2</sup> Research Scholar, Department of Mathematics, Vel Tech Rangarajan Dr. Sanguthala R&D Institute of Science and Technology, Chennai, Tamil Nadu, India;

**Abstract:** The Neutrosophic Set is an extension of the fuzzy set and the Intuitionistic Fuzzy Set which can be deal with imperfect, inconsistent, and indeterminate data in all the related problems. This article proposed the approach has considered a transportation problem based on Interval Valued Pythagorean Octagonal Neutrosophic Fuzzy Number with the numerical illustration.

**Keyword:** Pythagorean Fuzzy Set (PFS), Neutrosophic Fuzzy Set (NFS), Pythagorean Neutrosophic Fuzzy Set (PNFS), Pythagorean Octagonal Neutrosophic Fuzzy Number (PONFN), Interval Valued Pythagorean Octagonal Neutrosophic Fuzzy Number (IVPONFN).

### Introduction

In 1975, L.A.Zadeh[58] was discovered the notion of Fuzzy Set theory. The degree of membership function was suggested and deeply discussed in fuzzy set (FS) theory. Fuzzy Set theory has been applied in various fields like Homoeopathic verdict, Computer Science, and Fuzzy Algebra. In 1986, Atanassov [10] developed the idea of Intuitionistic Fuzzy Set (IFS) in which degree of membership as well as the degree of non-membership function are discussed. Generalization of fuzzy set theory is called the Intuitionistic Fuzzy Set. Intuitionistic Fuzzy Set theory applied in Engineering, Management Science and Computer Science [1, 6, 7, 26, 27, 19, 61, 47, 48, 49, 50, 51, 52, 40].

Atanassov also presented mathematical operations such as algebraic product, sum, union, intersection and complement [12, 9]. Pseudo fixed topics of all operators defined over the Intuitionistic Fuzzy Set [11] is also developed by him. In 1986, many scholars [7] have completed works in the field of Intuitionistic Fuzzy Set and its presentations. Many scholars [25, 35, 53, 57] further extended the concept of Intuitionistic Fuzzy Sets to introduce Interval Valued Intuitionistic Fuzzy Sets (IVIFSs), which enhances greatly the representation ability of uncertainty than IFSs. However, the domain of Intuitionistic Fuzzy Sets and Interval Valued Intuitionistic Fuzzy Sets which are used to indicate the certain

criterion does or does not belong to some fuzzy concepts.

Yager [54-56] developed the Pythagorean Fuzzy Set (PFS), which gives the accurate solutions in ambiguous and imprecise environments. When compared to FS and IFS, the Pythagorean fuzzy number becomes a more comprehensive computational model. Late, Smarandache [45] introduced the Neutrosophic Set and Neutrosophic probability and their logic which consists of three logics such as truth, indeterminacy, and falsity-membership degree. Interval Valued Fuzzy Sets were implemented by Zadeh [59]. An interval-valued membership function defines an Interval Valued Fuzzy Set (IVFS). IVFSs are a subset of L-fuzzy sets [23] and type-2 fuzzy sets [20].

The Interval Valued Pythagorean Fuzzy Set (IVPFS) is an extension of PFS [36]. Numerous real-world issues related to decision-making can be expressed using the interval number within  $[0, 1]$ . Set's membership as well as its absence degrees to have an interval value Interval Valued Pythagorean Fuzzy Sets (IVPFS). It should be noted that when the upper and lower limits of the interval values are identical, IVPFS becomes PFS, indicating that the latter is a special case of the former [60, 37].

The origin of transportation models dates back to 1941 when F.L. Hitchcock published a paper entitled 'The Distribution of a Product from Several Sources to Numerous Localities.' The

above paper did more contribution in finding the solution to transportation problems. In 1947, T.C. Koopmans implemented the article called 'Optimum Utilization of the Transportation System'. Above two contributions are mainly responsible for the development of transportation models which play vital role in shipping industry. Because, each shipping source has a certain capacity and each destination has a certain requirement associated with a certain cost of shipping from the sources to the destinations [39]. Researchers from different fields developed triangular, trapezoidal and pentagonal neutrosophic numbers, and presented the notions, properties along with applications in different fields [15, 17, 18]. The de-neutrosophication technique of pentagonal number and its applications are presented by [14, 16, 13, 21]. Sreeja T.S and Jeyanthi .V presents an application of Octagonal Neutrosophic Number and discuss with a score function [46].

Anandhi .M, and D.Arthi, works with a single valued octagonal neutrosophic number and introduces a new approach for using a score function [8].

Jansi, R., Mohana, K., Smarandache. F, contribute his work with properties of Pythagorean Neutrosophic Set [24].

Singh A, Bhat S.A represents a score and accuracy function for Neutrosophic Sets [44].

Scientists from different areas investigated the various properties and fluctuations of

## 2. Preliminaries

### Definition 2.1. [54-56]

Consider  $Z$  to be a universal set. Then a Pythagorean Fuzzy Set  $P$ , which is a set of ordered pairs over  $Z$ , is defined as follows:

$$P = \{ (z, \alpha(z), \beta(z)) \mid z \in Z \}$$

where  $\alpha_P(z) : Z \rightarrow [0,1]$  and  $\beta_P(z) : Z \rightarrow [0,1]$  define the degree of membership and non-membership, respectively, of the element  $z \in Z$  to  $P$ , which is a subset of  $z$ , and for every  $z \in Z$ :

$$0 \leq (\alpha_P(z))^2 + (\beta_P(z))^2 \leq 1$$

Suppose  $(\alpha_P(z))^2 + (\beta_P(z))^2 \leq 1$  then there is a degree of indeterminacy of  $z \in Z$  to  $P$  defined by  $\alpha_P(z) : \sqrt{1 - [(\alpha_P(z))^2 + (\beta_P(z))^2]}$  and  $\alpha_P(z) \in [0, 1]$ . In what follows,  $(\alpha_P(z))^2 + (\beta_P(z))^2 = 1$ . Otherwise,  $\alpha_P(z) = 0$  whenever  $(\alpha_P(z))^2 + (\beta_P(z))^2 = 1$ .

neutrosophic numbers and the properties of correlation between these numbers [14, 18]. The applications in decision-making in different fields like phone selection [42-43], games prediction [39], supplier selection [2, 4-5], medical [3], personnel selection [28-29].

Octagonal neutrosophic number and its types are presented by [41] in his recent work. The graphical representation and properties are yet to be defined while dealing with the concept of octagonal neutrosophic number a decision-maker can solve more fluctuations because they have more edges as compare to pentagonal.

Narmada Devi and Sowmiya [32, 33] introduced the Octagonal neutrosophic fuzzy number in game and sequencing problem.

Narmada Devi et al. [34] proposed the suitable waste to energy technology for India using MULTIMOORA method. The majority of WTE options were identified under different MCDMs using various fuzzy sets.

Narmada Devi .R, works with Different types of graphs on neutrosophic concept [30, 31].

The article aims to introduce an Interval Valued Pythagorean Octagonal Neutrosophic Fuzzy Number along with operational rules and score function for IVPONFN. After that, formulate the IVPONFN transportation problem will take place. Suitable examples have given wherever it required.

**Definition 2.2.** [45]

Let  $Z$  be a non-empty set. A Neutrosophic Fuzzy Set  $N$  on  $Z$  is an object of the form:

$$N = \{ (z, \alpha_N(z), \gamma_N(z), \beta_N(z)) : z \in Z \}$$

Where  $\alpha_N(z), \gamma_N(z), \beta_N(z) \in [0,1], 0 \leq \alpha_N(z) + \gamma_N(z) + \beta_N(z) \leq 3$  for all  $z \in Z$ ,  $\alpha_N(z)$ ,  $\gamma_N(z)$ ,  $\beta_N(z)$  are degrees of membership, indeterminacy and non-membership, respectively. Here,  $\alpha_N(z)$  and  $\beta_N(z)$  are dependent component and  $\gamma_N(z)$  is an independent components.

**Definition 2.3.** [36]

Let  $Z$  be a universal set. A Pythagorean Neutrosophic fuzzy set (PNFS) with  $T$  and  $F$  are dependent Neutrosophic components  $D$  on  $Z$  is an object of the form

$$D = \{ (z, \alpha_D(z), \gamma_D(z), \beta_D(z)) : z \in Z \}$$

where  $\alpha_D(z), \gamma_D(z), \beta_D(z) \in [0,1], 0 \leq (\alpha_D(z))^2 + (\gamma_D(z))^2 + (\beta_D(z))^2 \leq 2$ , for all  $z \in Z$ ,  $\alpha_D(z), \gamma_D(z)$  and  $\beta_D(z)$  are degrees of membership, indeterminacy, non-membership, respectively. Here,  $\alpha_D(z)$  and  $\beta_D(z)$  are dependent component and  $\gamma_D(z)$  is an independent components.

**Definition 2.4.** [37, 22]

Let  $Z$  be a universal set. An Interval-Valued Pythagorean Neutrosophic Fuzzy Set (PNFS) with  $T$  and  $F$  are dependent Neutrosophic components  $C$  on  $Z$  is an object of the form

$$C = \{ (z, [\alpha_C^L(z), \alpha_C^U(z)], [\gamma_C^L(z), \gamma_C^U(z)], [\beta_C^L(z), \beta_C^U(z)]) : z \in Z \}$$

Where  $[\alpha_C^L(z), \alpha_C^U(z)], [\gamma_C^L(z), \gamma_C^U(z)], [\beta_C^L(z), \beta_C^U(z)] \in [0, 1]$ ,

$$0 \leq \left[ \frac{\alpha_C^L(z) + \alpha_C^U(z)}{2} \right]^2, \left[ \frac{\gamma_C^L(z) + \gamma_C^U(z)}{2} \right]^2, \left[ \frac{\beta_C^L(z) + \beta_C^U(z)}{2} \right]^2 \leq 2$$

for all  $z \in Z$ ,  $[\alpha_C^L(z), \alpha_C^U(z)]$  is the degree of membership.  $[\gamma_C^L(z), \gamma_C^U(z)]$  is the degree of indeterminacy and  $[\beta_C^L(z), \beta_C^U(z)]$  is the degree of non-membership.

Linguistic term	Membership values	Indeterminacy values	Non – membership values
Extremely Low	[0.1, 0.2]	[0.5, 0.6]	[0.8, 0.9]
Medium	[0.2, 0.4]	[0.4, 0.5]	[0.6, 0.8]
Medium High	[0.4, 0.6]	[0.3, 0.4]	[0.4, 0.6]
Very High	[0.6, 0.8]	[0.2, 0.3]	[0.2, 0.4]
Extremely High	[0.8, 0.9]	[0.1, 0.2]	[0.1, 0.2]

**Table 1. Interval-Valued Pythagorean Neutrosophic Fuzzy Linguistic Table**

### 3. Operations on Interval Valued Pythagorean Octagonal Neutrosophic Fuzzy Number (IVPONFN)

**Definition 3.1**

Let  $p = ([p_a, p_b, p_c, p_d, p_e, p_f, p_g, p_h]; \alpha, \beta, \gamma) = ([p_a, p_b, p_c, p_d, p_e, p_f, p_g, p_h]; [\alpha_1, \alpha_2], [\beta_1, \beta_2], [\gamma_1, \gamma_2])$  be an Interval Valued Pythagorean Octagonal Neutrosophic Fuzzy Number where  $\alpha = [\alpha_1, \alpha_2]$  and  $\beta = [\beta_1, \beta_2]$  and  $\gamma = [\gamma_1, \gamma_2]$  represent an interval valued, hence  $\alpha \subset [0,1]$  And  $\beta \subset [0,1]$  and  $\gamma \subset [0,1]$  such that  $0 \leq \left( \frac{\alpha_1 + \alpha_2}{2} \right)^2 + \left( \frac{\beta_1 + \beta_2}{2} \right)^2 + \left( \frac{\gamma_1 + \gamma_2}{2} \right)^2 \leq 2$ .

**Definition 3.2**

Let  $p_1 = ([p'_a, p'_b, p'_c, p'_d, p'_e, p'_f, p'_g, p'_h]; [\alpha'_1, \alpha'_2], [\beta'_1, \beta'_2], [\gamma'_1, \gamma'_2])$  and  $p_2 = ([p''_a, p''_b, p''_c, p''_d, p''_e, p''_f, p''_g, p''_h]; [\alpha''_1, \alpha''_2], [\beta''_1, \beta''_2], [\gamma''_1, \gamma''_2])$  be any two IVPONFN and  $\delta > 0$ .  
Then

$$\begin{aligned}
 1. \quad p_1 \oplus p_2 &= \begin{cases} [p'_a + p''_a, p'_b + p''_b, p'_c + p''_c, p'_d + p''_d, p'_e + p''_e, p'_f + p''_f, p'_g + p''_g, p'_h + p''_h]; \\ [\sqrt{(\alpha'_1)^2 + (\alpha''_1)^2 - (\alpha'_1 \alpha''_1)^2} \times \sqrt{(\alpha'_2)^2 + (\alpha''_2)^2 - (\alpha'_2 \alpha''_2)^2}, \\ [(\beta'_1 \beta''_1, \beta'_2 \beta''_2)][(\gamma'_1 \gamma''_1, \gamma'_2 \gamma''_2)] \end{cases} \\
 2. \quad p_1 \otimes p_2 &= \begin{cases} [p'_a \times p''_a, p'_b \times p''_b, p'_c \times p''_c, p'_d \times p''_d, p'_e \times p''_e, p'_f \times p''_f, p'_g \times p''_g, p'_h \times p''_h]; \\ [\alpha'_1 \times \alpha''_1, \alpha'_2 \times \alpha''_2] [\sqrt{(\beta'_1)^2 + (\beta''_1)^2 - (\beta'_1 \times \beta''_1)^2}, \\ \sqrt{(\beta'_2)^2 + (\beta''_2)^2 - (\beta'_2 \times \beta''_2)^2}], [\sqrt{(\gamma'_1)^2 + (\gamma''_1)^2 - (\gamma'_1 \times \gamma''_1)^2}, \\ \sqrt{(\gamma'_2)^2 + (\gamma''_2)^2 - (\gamma'_2 \times \gamma''_2)^2}] \end{cases} \\
 3. \quad \delta p_1 &= \begin{cases} [\delta p'_a, \delta p'_b, \delta p'_c, \delta p'_d, \delta p'_e, \delta p'_f, \delta p'_g, \delta p'_h]; [\sqrt{1 - (1 - (\alpha'_1)^2)^\delta}, \sqrt{1 - (1 - (\alpha'_2)^2)^\delta}], \\ [((\beta'_1)^\delta, (\beta'_2)^\delta)][((\gamma'_1)^\delta, (\gamma'_2)^\delta)] \end{cases} \\
 4. \quad p_1^\delta &= \begin{cases} [(p'_a)^\delta, (p'_b)^\delta, (p'_c)^\delta, (p'_d)^\delta, (p'_e)^\delta, (p'_f)^\delta, (p'_g)^\delta, (p'_h)^\delta]; [(\alpha'_1)^\delta, (\alpha'_2)^\delta], \\ [\sqrt{1 - (1 - (\beta'_1)^2)^\delta}, \sqrt{1 - (1 - (\beta'_2)^2)^\delta}], \\ [\sqrt{1 - (1 - (\gamma'_1)^2)^\delta}, \sqrt{1 - (1 - (\gamma'_2)^2)^\delta}] \end{cases}
 \end{aligned}$$

**Definition 3.3**

Let  $p = ([p_a, p_b, p_c, p_d, p_e, p_f, p_g, p_h]; [\alpha_1, \alpha_2], [\beta_1, \beta_2], [\gamma_1, \gamma_2])$  be an Interval Valued Pythagorean Octagonal Neutrosophic Fuzzy Number. Then a Score function S can be defined as follows:

$$S(p) = \frac{1}{32} (p_a + p_b + p_c + p_d + p_e + p_f + p_g + p_h) [2 + (\alpha_1 + \alpha_2) - 2(\beta_1 + \beta_2) - (\gamma_1 + \gamma_2)]$$

**4. Mathematical Formulation of Interval Valued Pythagorean Octagonal Neutrosophic Fuzzy Number (IVPONFN) Transportation problem**

The transportation problem has been given in the form of  $m \times n$  IVPONFN cost table  $[C_{ij}]$  is tabulated below (Table 2):

	$D_1$	$D_2$	$\vdots$	$D_j$	$\vdots$	$D_n$	Quantities
$O_1$	$C_{11}$	$C_{12}$		$C_{1j}$		$C_{1n}$	$\tilde{a}_1$
$\vdots$	$\vdots$	$\vdots$		$\vdots$		$\vdots$	$\vdots$
$O_i$	$C_{i1}$	$C_{i2}$		$C_{ij}$		$C_{in}$	$\tilde{a}_i$
$\vdots$	$\vdots$	$\vdots$		$\vdots$		$\vdots$	$\vdots$
$O_m$	$C_{m1}$	$C_{m2}$		$C_{mj}$		$C_{mn}$	$\tilde{a}_m$
Requirements	$\tilde{b}_1$	$\tilde{b}_2$		$\tilde{b}_j$		$\tilde{b}_n$	

**Table 2: Transportation Cost Matrix**

The cost  $C_{ij}$  are taken as IVPONFN S.

$$\tilde{C}_{ij}^{IPN} = ((\tilde{C}_{ij}^{IPN}, \tilde{C}_{ij}^{IPN}, \tilde{C}_{ij}^{IPN}, \tilde{C}_{ij}^{IPN}) [\mu_{ij}^L, \mu_{ij}^U], [v_{ij}^L, v_{ij}^U], [w_{ij}^L, w_{ij}^U])$$

The target is to minimize the IVPONFN cost induced transportation successfully. Let us presume that there are  $m$  quantities at the sources and  $n$  requirements at the destination. Let  $\tilde{a}_i^{IPN}$  the IVPONFN quantities at  $i$  and  $\tilde{b}_j^{IPN}$  IVPONFN requirement at  $j$  be the unit cost IVPONFN transportation cost from source  $i$  to destination  $j$  and  $\tilde{X}_{ij}$  be the number of units shifted from source  $i$  to destination  $j$ . The IVPONFN transportation problem can be mathematically expressed as

$$\min \tilde{z} = \sum_{i=1}^m \sum_{j=1}^n \tilde{c}_{ij}^{IPN} \tilde{X}_{ij}$$

subject to the constraints,  $\sum_{j=1}^n \tilde{X}_{ij} = \tilde{a}_i, i = 1 \text{ to } m$  and  $\sum_{i=1}^m \tilde{X}_{ij} = \tilde{b}_j, j = 1 \text{ to } n$

The IVPONFN problem is said to be balanced

$$\sum_{j=1}^n \tilde{a}_i = \sum_{j=1}^n \tilde{b}_j$$

(i.e., if the total supply from all the sources is equal to the demand of the requirement)

#### 4.1. A Mathematical approach for IVPONFN:

This section provides step by step procedure for a Mathematical approach to the IVPONFN transportation problem which leads as:

**Step 1:** Using the ranking function described, obtain the rank for each cell of the chosen generalized IVPONFN cost matrix.

**Step 2:** Test the generalized IVPONFN transportation problem is balanced, if it is balanced, Proceed to step 4, otherwise move on to step 3.

**Step 3:** Use zero generalized single-valued dummy rows of dummy columns. To construct a balanced one, Natural number must be added.

**Step 4:** Find the initial basic feasible solution by following the NWC, LCM, VAM approach and if it is degeneracy check the optimality test by following a modified distribution approach to obtain the optimal solution.

**Step 5:** Using generalized IVPONFN cost by adding the optimal generalized IVPONFN cost which minimizes the Transportation cost.

#### 5. Application of Interval Valued Pythagorean Octagonal Neutrosophic Fuzzy Number (IVPONFN)

The above Mathematical approach is illustrated in the following transportation problem, based on IVPONFN. To obtain the best optimal solution. Here the problem is considered as Chemical Factory requirement to get the best optimal solution as well as the optimal decision to the stack holders. A Factory has three branches  $A_1, A_2, A_3$  from which it supplies to three destinations  $D_1, D_2, D_3$ . Among the three branches of 8 members in each branches whose transportation cost between the various destination is considered in terms of Linguistic variable like Extremely Low, Medium, Medium the Mathematical approach to the problem to get the best optimal solution.

High, Very High, Extremely High according to the transportation cost of this branches to the destination and so on. Based on the Linguistic variable of the group membership indeterminacy, non-membership are defined and is given by the following table. Calculate the optimal cost depending on the appropriate. Date giving the chemicals to distribute the destinations shifting cost, quantities available at each branches and quantities required at each destination. Due to uncertain situations, all the costs of the problem as IVPONFN.

Using the proposed ranking function the transportation cost from branches to the destinations has defuzzified as a crisp number and applied

Table 3

	$D_1$	$D_2$	$D_3$	Supply
$A_1$	(2.1, 2.2, 2.3, 2.4, 2.5, 2.7, 2.8, 2.9) [0.2, 0.4] [0.3, 0.4] [0.4, 0.6]	(2.1, 2.2, 2.4, 2.7, 2.9, 3.1, 3.3, 3.5) [0.2, 0.4] [0.3, 0.4] [0.4, 0.6]	(4.1, 4.2, 4.3, 4.4, 4.6, 4.7, 4.8, 5.0) [0.6, 0.8] [0.2, 0.3] [0.2, 0.4]	(1.0, 1.2, 1.3, 1.5, 1.6, 1.8, 2.0, 2.2) [0.2, 0.4] [0.3, 0.4] [0.4, 0.6]
$A_2$	(5.1, 5.2, 5.5, 5.6, 5.7, 5.8, 5.9, 6.0) [0.8, 0.9] [0.2, 0.3] [0.1, 0.2]	(3.1, 3.2, 3.4, 3.5, 3.7, 3.8, 3.9, 4.1) [0.4, 0.6] [0.3, 0.4] [0.4, 0.6]	(4.1, 4.2, 4.3, 4.6, 4.7, 4.9, 5.2, 5.4) [0.6, 0.8] [0.2, 0.3] [0.2, 0.4]	(1.5, 1.7, 1.9, 2.2, 2.5, 2.7, 2.9, 3.2) [0.4, 0.6] [0.3, 0.4] [0.4, 0.6]
$A_3$	(5.3, 5.5, 5.7, 5.9, 6.2, 6.4, 6.5, 6.8) [0.8, 0.9] [0.1, 0.2] [0.1, 0.2]	(6.1, 6.2, 6.3, 6.5, 6.7, 6.9, 7.0, 7.2) [0.8, 0.9] [0.1, 0.2] [0.1, 0.2]	(3.1, 3.3, 3.4, 3.6, 3.7, 3.8, 4.0, 4.2) [0.4, 0.6] [0.3, 0.4] [0.4, 0.6]	(3.0, 3.3, 3.6, 3.8, 4.0, 4.2, 4.5, 5.0) [0.8, 0.9] [0.1, 0.2] [0.1, 0.2]
Demand	(2.0, 2.2, 2.4, 2.5, 2.7, 2.8, 3.2, 3.4) [0.4, 0.6] [0.3, 0.4] [0.4, 0.6]	(2.2, 2.4, 2.6, 2.8, 3.0, 3.3, 3.5, 3.8) [0.6, 0.8] [0.2, 0.3] [0.2, 0.4]	(2.0, 2.5, 3.2, 3.4, 3.5, 3.9, 4.0, 4.5) [0.6, 0.8] [0.2, 0.3] [0.2, 0.4]	

**Solution:**

To convert IVPONFN to crisp number by using a proposed score function  $S(p)$  for the table 3 and it is given as score matrix as below.

	$D_1$	$D_2$	$D_3$	$a_i$
$A_1$	0.12	0.13	2.03	0.79
$A_2$	3.36	0.54	2.10	3.49
$A_3$	4.23	4.63	0.55	27.48
$b_j$	3.98	13.28	15.19	

We have to check Supply = Demand

$$0.79 + 3.49 + 27.48 = 3.98 + 13.28 + 15.19$$

$$31.76 \neq 32.45$$

It is unbalanced transportation problem

Now we add Dummy Row

	$D_1$	$D_2$	$D_3$	$a_i$
	0.12	0.13	2.03	0.79
	3.36	0.54	2.10	3.49
	4.23	4.63	0.55	27.48

0	0	0	0.69
$b_j$			
3.98	13.28	15.19	

(i) North – West Corner Method

**Step 1:**

Consider a North corner is  $C_{11}$   
 $\min(a_1, b_1) = 0.79$  occurred in  $a_1$   
Delete first row.

**Step 2:**

Consider a North corner is  $C_{21}$   
 $\min(a_2, b_1) = 3.19$  occurred in  $b_1$   
Delete first column.

**Step 3:**

Consider a North corner is  $C_{22}$   
 $\min(a_2, b_2) = 0.30$  occurred in  $a_1$   
Delete second row.

**Step 4:**

Consider a North corner is  $C_{32}$   
 $\min(a_3, b_2) = 12.98$  occurred in  $b_2$   
Delete second column.

**Step 5:**

Consider a North corner is  $C_{33}$   
 $\min(a_3, b_3) = 4.50$  occurred in  $a_3$   
Delete third row.

**Step 6:**

Consider the remaining cost is  $C_{43}$  (i.e., 0)

The Optimal allocation for this problem is

0.12	0.79	0.13	2.03	0.79
3.36	3.19	0.54	0.30	3.49
4.23	4.63	12.98	0.55	14.50
3.98	13.28	15.19		27.48

The Optimal Transportation cost is

$$\begin{aligned}
 &= 0.79(0.12) + 3.36(3.19) + 0.54(0.30) + 4.63(12.98) + 0.55(14.50) \\
 &= 0.10 + 10.72 + 0.16 + 60.10 + 7.98 \\
 &= 79.06
 \end{aligned}$$

The Optimal Transportation cost is 79.06



(ii) Least Cost Method

			$a_i$
0.12	0.13	2.03	0.79
3.36	0.54	2.10	3.49
4.23	4.63	0.55	27.48
0	0	0	0.69
$b_j$			
3.98	13.28	15.19	

**Step 1:**

$\min(C_{ij}) = 0$  occurred in  $C_{41}$

$\min(a_4, b_1) = 0.69$  occurred in  $a_4$

Delete fourth row.

**Step 2:**

$\min(C_{ij}) = 0.12$  occurred in  $C_{11}$

$\min(a_1, b_1) = 0.79$  occurred in  $a_1$

Delete first row.

**Step 3:**

$\min(C_{ij}) = 0.54$  occurred in  $C_{22}$

$\min(a_2, b_2) = (3.49, 13.28) = 3.49$  occurred in  $a_2$

Delete second row.

**Step 4:**

$\min(C_{ij}) = 0.55$  occurred in  $C_{33}$

$\min(a_3, b_3) = 15.19$  occurred in  $b_3$

Delete third column.

**Step 5:**

$\min(C_{ij}) = 4.23$  occurred in  $C_{31}$

$\min(a_3, b_3) = 2.50$  occurred in  $b_1$

Delete first column.

**Step 6:**

The remaining cost is 4.63 occurred in  $C_{32}$ .

The Optimal allocation for this problem is

0.12	0.79	0.13	2.03	0.79
------	------	------	------	------

3.36	0.54	2.10	3.49
4.23	4.63	0.55	27.48
3.98	13.28	15.19	

The Optimal Transportation cost is

$$\begin{aligned}
 &= 0.12(0.79) + 0.54(3.49) + 4.23(2.50) + 4.63(9.79) + 0.55(15.19) \\
 &= 0.10 + 1.89 + 10.58 + 45.33 + 8.36 \\
 &= 66.26
 \end{aligned}$$

The Optimal Transportation cost is 66.26

(iii) Vogel's Approximation Method (VAM)

0.12	0.13	2.03	0.79
3.36	0.54	2.10	3.49
4.23	4.63	0.55	27.48
0	0	0	0.69
3.98	13.28	15.19	

Step 1:

Find the Penalty cost namely the difference between the lowest and second lowest cost in each row and each column and choose the maximum penalty

0.12	0.13	2.03	0.79	0.01	0.01	0.01	0.13	0.13
3.36	0.54	2.10	3.49	1.56	2.82	-	-	-
4.23	4.63	0.55	27.48	3.68	0.4	0.40	4.63	-
0	0	0	0.69	0	0	0	0	0
3.98	13.28	15.19						
0.12	0.13	0.55						

0.12	0.13	-
0.12	0.13	-
-	0.13	-
-	0.13	-

**Step 2:**

The Maximum penalty is 3.68 which is occurred in  $a_3$ .  $\min(C_{31}, C_{32}, C_{33}) = 0.55$   
Which is occurred in  $C_{33}$ .  
 $\min(a_3, b_3) = 15.19$  occurred in  $b_3$   
Delete third column.

**Step 3:**

Repeat the procedure the Maximum penalty is 2.82 occurred in  $a_2$ .  
 $\min(C_{21}, C_{22}) = 0.54$  occurred in  $C_{22}$ .  
 $\min(a_2, b_2) = 3.49$  occurred in  $a_2$   
Delete second row.

**Step 4:**

Repeat the procedure the Maximum penalty is 0.40 occurred in  $a_3$ .  
 $\min(C_{31}, C_{32}) = 4.23$  occurred in  $C_{31}$ .  
 $\min(a_3, b_1) = 3.98$  occurred in  $b_1$   
Delete first column.

**Step 5:**

Repeat the procedure the Maximum penalty is 4.63 occurred in  $a_3$ .  
4.63 occurred in  $C_{32}$ .  
 $\min(a_3, b_2) = 8.31$  occurred in  $a_3$   
Delete third row.

**Step 6:**

Repeat the procedure the Maximum penalty is 0.13 occurred in  $a_1$ .  
0.13 is occurred in  $C_{12}$ .  
 $\min(a_1, b_2) = 0.79$  occurred in  $a_1$   
Delete first row.

**Step 7:**

The remaining allocation is 0.69 for  $C_{42}$ .

The optimal allocation is

			$a_i$
0.12	0.13	0.79	0.79
3.36	0.54	3.49	3.49
4.23	3.98	8.31	15.19
3.98	13.28	15.19	27.48
$b_j$			

The Optimal Transportation cost is

$$\begin{aligned}
 &= 0.13(0.79) + 0.54(3.49) + 4.23(3.98) + 4.63(8.31) + 0.55(15.19) \\
 &= 0.10 + 1.89 + 16.84 + 38.48 + 8.36 \\
 &= 65.67
 \end{aligned}$$

The Transportation cost is

**NWC** – 79.06 Rs

**LCM** – 66.26 Rs

**VAM** – 65.67 Rs

### Conclusion

For addressing the situation where inconsistencies and insufficient data exist, Neutrosophic Set will be useful. This article suggests a Mathematical Neutrosophic Approach using ranking function for Transportation Problem. Since this method gives the optimal and accurate solutions, stack holders always use interval valued neutrosophic approach for taking precious decision.

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