

A Significant Factor Of Fuzzy Neutrosophic Soft Matrices In Decision Making

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Abstract

First some fundamental tasks of fuzzy neutrosophic soft matrix is characterized and presented a new fuzzy neutrosophic soft complement matrix dependent on reference work and the trace of fuzzy neutrosophic soft matrix. A few properties and models are examined. In conclusion, a fuzzy neutrosophic soft matrix for a choice strategy is characterized.

Keywords: Soft set, Fuzzy soft set, Neutrosophic set, Fuzzy neutrosophic soft set, Fuzzy neutrosophic soft matrices, Reference function.

1 Introduction

The Soft set idea is started by Molodtsov [6] for demonstrating vagueness and vulnerability. Maji et al. [7] proposed the idea of fuzzy soft set for certain properties. Neutrosophic soft sets and the idea of neutrosophic set was presented by Florentine[8].

Arockiarani and Sumathi [2] initiated new methods on fuzzy neutrosophic soft matrices. The idea of fuzzy soft set dependent on reference function is proposed by Baruah[5]. The proposed technique is an endeavor to further develop the outcomes utilizing fuzzy neutrosophic soft matrix based on reference work and to detail an application of choice strategy.

2 Preliminaries

Some essential definitions are given, which are utilized in this paper.

2.1 Definition

Let X be a universe of discourse, with a generic element in X denoted by x , the neutrosophic set (NS), A is an object having the structure $A = \{ \langle x, (T_A(x), I_A(x), F_A(x)) \rangle, x \in X \}$ where the function defines $T, I, F: X \rightarrow]0, 1]^+$ respectively the degree of membership (or truth), the degree of indeterminacy and the degree of non-membership (or Falsehood) of the component $x \in X$ to

the set A with the property $0 \leq T_A(x) + I_A(x) + F_A(x) \leq 3^+ \dots \dots \dots (1)$

We assume the value from the subset of $[0,1]$. \therefore we read equation (1) as

$0 \leq T_A(x) + I_A(x) + F_A(x) \leq 3$. In brief an component \tilde{a} in the neutrosophic set A, can be read as $\tilde{a} = \langle a^T, a^I, a^F \rangle$, where a^T symbolise the level of Truth, a^I symbolise the level of Indeterminacy, a^F symbolise the level of Falsity, such that $0 \leq a^T + a^I + a^F \leq 3$.

2.2 Example

Assume that the universe of discourse be $U = \{x_1, x_2, x_3\}$, where x_1 indicates the capability, x_2 indicates the reliability, x_3 indicates the cost of price. Suppose A is a Neutrosophic set (NS) of U such that, $A = \{ \langle x_1, (0.4, 0.6, 0.3) \rangle, \langle x_2, (0.2, 0.4, 0.5) \rangle, \langle x_3, (0.3, 0.5, 0.5) \rangle \}$ where for x_1 the level of truthfulness of capability is 0.4, the level of indeterminacy of capability is 0.6 and the level of falsity of capability is 0.3 etc.

2.3 Definition

Let U be an initial universe set and E be a set of parameters. Let $A \subset E$. A pair (F, A) is called a Fuzzy soft set over U, where F is a mapping given by $F: A \rightarrow F^U$, where F^U denotes the collection of all fuzzy subsets of U.

2.4 Definition

Let U be the initial universal set and E be a set of parameter. Consider a non-empty set A, $A \subset E$. The family (F, A) is named as the Fuzzy Neutrosophic Soft sets (FNSS) over U, where F is a mapping given by $F: A \rightarrow P(U)$. Let $P(U)$ signifies the set of all fuzzy neutrosophic sets of U. We assume A as FNSS over U rather than (F, A) .

2.5 Definition

Let $U = \{c_1, c_2, c_3, \dots, c_m\}$ be the universal set and E be the set of parameter given by $E = \{e_1, e_2, e_3, \dots, e_n\}$. Let $A \subset E$. A pair (F, A) be a FNSS over U. Then the subset $U \times E$ is defined by $R_A = \{(u, e); e \in A, u \in F_A(e)\}$ which is called a relation form of (F_A, E) . The function are written by $T_R(A): U \times E \rightarrow [0,1]$, $I_R(A): U \times E \rightarrow [0,1]$ and $F_R(A): U \times E \rightarrow [0,1]$ where $T_R(A)(u, e) \in [0,1]$, $I_R(A)(u, e) \in [0,1]$ and $F_R(A)(u, e) \in [0,1]$ are the level of membership, indeterminacy and non membership value.

If $\{ \langle T_{ij}, I_{ij}, F_{ij} \rangle \} = [\langle T_{ij}(u_i, e_j), I_{ij}(u_i, e_j), F_{ij}(u_i, e_j) \rangle]$

We define a matrix

$$[\langle T_{ij}, I_{ij}, F_{ij} \rangle]_{m \times n} = \begin{pmatrix} \langle T_{11}, I_{11}, F_{11} \rangle & \dots & \langle T_{1n}, I_{1n}, F_{1n} \rangle \\ \langle T_{21}, I_{21}, F_{21} \rangle & \dots & \langle T_{2n}, I_{2n}, F_{2n} \rangle \\ \vdots & & \vdots \\ \langle T_{ij}, I_{ij}, F_{ij} \rangle & \dots & \vdots \\ \vdots & & \vdots \\ \langle T_{m1}, I_{m1}, F_{m1} \rangle & \dots & \langle T_{mn}, I_{mn}, F_{mn} \rangle \end{pmatrix}$$

which is called an $m \times n$ Fuzzy Neutrosophic Soft Matrix (FNSM) of the FNSS (F_A, E) over U .

2.6 Definition

Let $U = \{c_1, c_2, c_3, \dots, c_m\}$ be the universal set and E be the set of parameter given by $E = \{e_1, e_2, e_3, \dots, e_n\}$. Let $A \subset E$. A pair (F, A) be a fuzzy neutrosophic soft set over U . Then the fuzzy neutrosophic soft set (F, A) in a matrix form as $A_{m \times n} = (a_{ij})_{m \times n}$ or $A = (a_{ij})$, $i = 1, 2, \dots, m$, $j = 1, 2, \dots, n$ where

$$(a_{ij}) = \begin{cases} \langle T(c_i, e_j), I(c_i, e_j), F(c_i, e_j) \rangle & \text{if } e_j \in A \\ \langle 0, 0, 1 \rangle & \text{if } e_j \notin A \end{cases}$$

Where $T_j(c_i)$ represents the membership of (c_i) , $I_j(c_i)$ represents the indeterminacy of (c_i) , and $F_j(c_i)$ represents the non-membership of (c_i) in the FNSS (F, A) .

Notation:[10]

Let $F_{m \times n}$ denotes FNSM of order $m \times n$ and F_n denotes FNSM of order $n \times n$.

2.7 Definition

Let $A = \langle a_{ij}^T, a_{ij}^I, a_{ij}^F \rangle \in F_{m \times n}$ then A is called

a) A zero (or) null FNSM denoted by $\tilde{0} = [0, 0, 1]$ if $a_{ij}^T = 0, a_{ij}^I = 0, a_{ij}^F = 1 \forall i \& j$.

It is denoted by ϕ .

b) A universal FNSM denoted by $\tilde{1} = [1, 1, 0]$ if $a_{ij}^T = 1, a_{ij}^I = 1, a_{ij}^F = 0 \forall i \& j$.

It is denoted by J .

3. Operations on fuzzy neutrosophic soft matrix theory:

3.1 Definition

If $A = (a_{ij}) \in F_{m \times n}$, $B = (b_{ij}) \in F_{m \times n}$ then we define $A \cup B$,

$$A \cup B = (c_{ij})_{m \times n} = \{ \langle \max(a_{ij}^T, b_{ij}^T), \max(a_{ij}^I, b_{ij}^I), \min(a_{ij}^F, b_{ij}^F) \rangle \} \quad \forall i \& j.$$

3.2 Definition

If $A = (a_{ij}) \in F_{m \times n}$, $B = (b_{ij}) \in F_{m \times n}$ then we define $A \cap B$,

$$A \cap B = (c_{ij})_{m \times n} = \{ \langle \min(a_{ij}^T, b_{ij}^T), \min(a_{ij}^I, b_{ij}^I), \max(a_{ij}^F, b_{ij}^F) \rangle \} \quad \forall i \& j.$$

3.3 Definition

If $A = (a_{ij}) \in F_{m \times n}$, where $(a_{ij}) = \langle a_{ij}^T, a_{ij}^I, a_{ij}^F \rangle$ then A^c is called complement of A if $A^c = (b_{ij})_{m \times n}$ where $(b_{ij}) = \langle a_{ij}^F, 1 - a_{ij}^I, a_{ij}^T \rangle$.

3.4 Definition

Let $A = \langle a_{ij}^T, a_{ij}^I, a_{ij}^F \rangle \in F_{m \times n}$ and $k \in F = [0, 1]$ define scalar multiplication as

$$kA = \{ \langle \min(k, a_{ij}^T), \min(k, a_{ij}^I), \max(k, a_{ij}^F) \rangle \} \in F_{m \times n}.$$

3.5 Definition

If $A = (a_{ij}) \in F_{m \times n}$, $B = (b_{ij}) \in F_{m \times n}$ then component wise sum and component wise product is determined as

$$A \oplus B = \{ \langle \max(a_{ij}^T, b_{ij}^T), \max(a_{ij}^I, b_{ij}^I), \min(a_{ij}^F, b_{ij}^F) \rangle \mid \forall i \& j. \}$$

$$A \odot B = \{ \langle \min(a_{ij}^T, b_{ij}^T), \min(a_{ij}^I, b_{ij}^I), \max(a_{ij}^F, b_{ij}^F) \rangle \mid \forall i \& j. \}$$

3.6 Properties

1. $[\tilde{A}^c]^c = \tilde{A}$
2. $\tilde{A} \cup \tilde{A} = \tilde{A}$
3. $\tilde{A} \cap \tilde{A} = \phi$
4. $\tilde{A} \cap [0] = [0]$
5. $[\tilde{A} \cup \tilde{B}]^c = \tilde{A}^c \cap \tilde{B}^c$
6. $[\tilde{A} \cap \tilde{B}]^c = \tilde{A}^c \cup \tilde{B}^c$

All the above properties holds for FNSM.

4. Fuzzy neutrosophic complement soft matrix based on reference function:

The above fuzzy neutrosophic complement soft matrix cannot hold for $\tilde{A} \cap \tilde{A}^c \neq \phi$ and $\tilde{A} \cup \tilde{A}^c \neq J$. So we track a new fuzzy neutrosophic complement soft matrix based on reference work.

4.1 Definition

Let $A = [\langle (a_{ij}^T, 0), (a_{ij}^I, 0), (a_{ij}^F, 0) \rangle]_{m \times n} \in F_{m \times n}$. Then $A^{C(N)}$ is known as new fuzzy neutrosophic complement soft matrix if $A^{C(N)} = [\langle (1, a_{ij}^T), (1, a_{ij}^I), (1, a_{ij}^F) \rangle]_{m \times n}$ for all $a_{ij} \in [0, 1]$. Here $a_{ij}^T(x)$, $a_{ij}^I(x)$, $a_{ij}^F(x)$ are the enrolment value and $(0, 0, 0)$ is the reference function and their difference value is known as enrolment value for truth, indeterminate and lie.

4.2 Example

$$\text{Let } A = \begin{bmatrix} \langle (0.3, 0), (0.4, 0), (0.2, 0) \rangle & \langle (0.4, 0), (0.5, 0), (0.6, 0) \rangle \\ \langle (0.4, 0), (0.5, 0), (0.3, 0) \rangle & \langle (0.2, 0), (0.4, 0), (0.6, 0) \rangle \end{bmatrix}$$

Then new Fuzzy Neutrosophic Complement Soft Matrix based on Reference work is

$$A^{C(N)} = \begin{bmatrix} \langle (1, 0.3), (1, 0.4), (1, 0.2) \rangle & \langle (1, 0.4), (1, 0.5), (1, 0.6) \rangle \\ \langle (1, 0.4), (1, 0.5), (1, 0.3) \rangle & \langle (1, 0.2), (1, 0.4), (1, 0.6) \rangle \end{bmatrix}$$

4.3. Operations on fuzzy neutrosophic complement soft matrix on the basis of reference function:

Let A and B be $F_{m \times n}$ where $A = (a_{ij})_{m \times n}$, $a_{ij} = (\langle \mu_{j1}^{T, I, F}(c_i), \mu_{j2}^{T, I, F}(c_i) \rangle)$ and

$B = (b_{ij})_{m \times n}$, $b_{ij} = (\langle \chi_{j1}^{T, I, F}(c_i), \chi_{j2}^{T, I, F}(c_i) \rangle)$. To keep away from degenerate cases we consider $\min(\langle \mu_{j1}^{T, I, F}(c_i), \chi_{j1}^{T, I, F}(c_i) \rangle) \geq \max(\langle \mu_{j2}^{T, I, F}(c_i), \chi_{j2}^{T, I, F}(c_i) \rangle) \forall i \& j$.

The function of sum (+) between A and B be declared as $A + B = C$ where $C = (c_{ij})_{m \times n}$,

$c_{ij} = \max(\langle \mu_{j1}^{T,I,F}(c_i), \chi_{j1}^{T,I,F}(c_i) \rangle, \min(\mu_{j2}^{T,I,F}(c_i), \chi_{j2}^{T,I,F}(c_i) \rangle)$ where $\mu_{j1}^{T,I,F}$ is the enrolment value and $\chi_{j1}^{T,I,F}$ are the reference function.

4.4 Example

Consider A and $A^{C(N)}$ discussed in example 4.2

Now, $A_{11} = (\langle (0.3, 0), (1, 0.3) \rangle, \langle (0.4, 0), (1, 0.4) \rangle, \langle (0.2, 0), (1, 0.2) \rangle)$ and

$A_{11}^{C(N)} = (\langle (1, 0.3), (0.3, 0) \rangle, \langle (1, 0.4), (0.4, 0) \rangle, \langle (1, 0.2), (0.2, 0) \rangle)$

then $A_{11} \cap A_{11}^{C(N)} = (\langle (0.3, 0), (1, 0.3) \cup (1, 0.3), (0.3, 0) \rangle,$

$\langle (0.4, 0), (1, 0.4) \cup (1, 0.4), (0.4, 0) \rangle, \langle (0.2, 0), (1, 0.2) \cup (1, 0.2), (0.2, 0) \rangle)$

$= \{ \langle (1, 0), (0.3, 0.3) \rangle, \langle (1, 0), (0.4, 0.4) \rangle, \langle (1, 0), (0.2, 0.2) \rangle \}$

$= J$.

Similarly, we can prove for $A \cap A^{C(N)} = \phi$ by taking min instead of max and max instead of min in the above operation.

4.5 Proposition

Let A and B be two FNSCM based on reference function. Then

$$i) \quad (A^{C(N)})^T = (A^T)^{C(N)}$$

$$ii) \quad (A^{C(N)} + B^{C(N)})^T = (A^T)^{C(N)} + (B^T)^{C(N)}$$

Proof:

We have, let $A \in \text{FNSM}_{m \times n}$, then

$$A = [\langle (a_{ij}^T(c_i), [0]_{ij}), (a_{ij}^I(c_i), [0]_{ij}), (a_{ij}^F(c_i), [0]_{ij}) \rangle]$$

$$A^{C(N)} = [\langle ([1]_{ij} a_{ij}^T(c_i)), ([1]_{ij}, a_{ij}^I(c_i)), ([1]_{ij}, a_{ij}^F(c_i)) \rangle]$$

Then

$$[A^{C(N)}]^T = [\langle ([1]_{ji}, a_{ji}^T(c_i)), ([1]_{ji}, a_{ji}^I(c_i)), ([1]_{ji}, a_{ji}^F(c_i)) \rangle]$$

For

$$A^T = [\langle (a_{ji}^T(c_i), [0]_{ji}), (a_{ji}^I(c_i), [0]_{ji}), (a_{ji}^F(c_i), [0]_{ji}) \rangle]$$

$$(A^T)^{C(N)} = [\langle ([1]_{ji}, a_{ji}^T(c_i)), ([1]_{ji}, a_{ji}^I(c_i)), ([1]_{ji}, a_{ji}^F(c_i)) \rangle]$$

$$\text{Hence } (A^{C(N)})^T = (A^T)^{C(N)}.$$

The verification of (ii) is just like the above part (i).

4.6 Trace of a square Fuzzy Neutrosophic Soft Matrix:

Let A be a F_n matrix then the trace of the matrix A is symbolised by $\text{tr}(A)$ is the addition of the leading diagonal elements. Then,

$$\text{tr}(A) = \sum_{i=1}^n a_{ii} = \{ \langle \max \{ a_{ii}^T \}, \max \{ a_{ii}^I \}, \min \{ a_{ii}^F \} \rangle \}$$

4.7 Proposition

Let A and B be two FNSMF $_n$ each of order n . Then $\text{tr}(A + B) = \text{tr}(A) + \text{tr}(B)$

Proof:

$$\text{tr}(A) = \{ \langle \max(a_{ii}^T), \max(a_{ii}^I), \min(a_{ii}^F) \rangle \}$$

$$\text{and } \text{tr}(B) = \{ \langle \max(b_{ii}^T), \max(b_{ii}^I), \min(b_{ii}^F) \rangle \}$$

then $(A+B) = C$ where $C = (c_{ii})$.

$$\text{tr}(c_{ii}) = \{ \langle \max(a_{ii}^T, b_{ii}^T), \max(a_{ii}^I, b_{ii}^I), \min(a_{ii}^F, b_{ii}^F) \rangle \}$$

$$\text{tr}(C) = \text{tr}(A+B)$$

Conversely,

$$\text{tr}(A) + \text{tr}(B) = \{ \langle \max(a_{ii}^T), \max(a_{ii}^I), \min(a_{ii}^F) \rangle \} + \{ \langle \max(b_{ii}^T), \max(b_{ii}^I), \min(b_{ii}^F) \rangle \}$$

$$= \{ \langle \max(a_{ii}^T, b_{ii}^T), \max(a_{ii}^I, b_{ii}^I), \min(a_{ii}^F, b_{ii}^F) \rangle \} \\ = \text{tr}(A+B)$$

Hence the result.

4.8 Proposition

Let $A = [\langle a_{ii}^T, a_{ii}^I, a_{ii}^F \rangle] \in F_n$ be a Fuzzy neutrosophic soft square matrix of order n , if k is a scalar such that $0 \leq k \leq 1$. Then $\text{tr}(kA) = k \text{tr}(A)$.

Proof:

We have

$$\text{tr}(kA) = \{ \langle \max(\min(k, a_{ii}^T), \min(k, a_{ii}^I), \min(k, a_{ii}^F)) \rangle \}$$

$$k \text{tr}(A) = k \{ \langle \max(a_{ii}^T), \max(a_{ii}^I), \min(a_{ii}^F) \rangle \}$$

$$\text{tr}(kA) = k \text{tr}(A)$$

Hence the result.

4.9 Example

$$\text{Let } A = \begin{bmatrix} \langle 0.3, 0.4, 0.2 \rangle & \langle 0.4, 0.6, 0.5 \rangle \\ \langle 0.5, 0.7, 0.3 \rangle & \langle 0.7, 0.4, 0.2 \rangle \end{bmatrix}$$

Here $k = 0.6$

$$(kA)_{11} = \{ \langle \min(0.6, 0.3), \min(0.6, 0.4), \max(0.6, 0.2) \rangle \}$$

$$(kA)_{11} = \langle 0.3, 0.4, 0.6 \rangle$$

$$(kA)_{22} = \{ \langle \min(0.6, 0.7), \min(0.6, 0.4), \max(0.6, 0.2) \rangle \}$$

$$(kA)_{22} = \langle 0.6, 0.4, 0.6 \rangle$$

$$\text{Then } \text{tr}(kA) = \{ \langle \max(0.3, 0.6), \max(0.4, 0.4), \min(0.6, 0.6) \rangle \} \\ = \{ \langle 0.6, 0.4, 0.6 \rangle \}$$

$$\text{tr}(A) = \{ \langle 0.7, 0.4, 0.2 \rangle \}$$

$$k \text{tr}(A) = \{ \langle \min(0.6, 0.7), \min(0.6, 0.4), \max(0.6, 0.2) \rangle \} = \{ \langle 0.6, 0.4, 0.6 \rangle \}$$

Hence shown.

4.10 Proposition

Let $A = [\langle a_{ij}^T, a_{ij}^I, a_{ij}^F \rangle] \in F_n$ be a fuzzy neutrosophic soft square matrix of order n . Then $\text{tr}(A) = \text{tr}(A^T)$ where A^T is a transpose of A .

It can be easily verified.

5. Application of Harmonic mean (A_{HM}) of fuzzy neutrosophic soft matrix in choice

strategy:

An usage of FNSM in choice strategy is presented in this section.

5.1 Definition

Let $A = [a_{ij}^T, a_{ij}^I, a_{ij}^F] \in \text{FNSM}_{m \times n}$, then the harmonic mean of FNSM A denoted by A_{HM} is determined as $A_{HM} = \left(2 \frac{\prod_{i=1}^n a_{ij}^T}{\sum_{i=1}^n a_{ij}^T}, 2 \frac{\prod_{i=1}^n a_{ij}^I}{\sum_{i=1}^n a_{ij}^I}, 2 \frac{\prod_{i=1}^n a_{ij}^F}{\sum_{i=1}^n a_{ij}^F} \right)$

5.2 Definition

The score value of S_i for $U_i \in U$ is defined as $S_i = T_i - I_i F_i$.

5.3 Algorithm

1. Build a FNSS (F,A) over U.
2. Build the fuzzy neutrosophic soft matrix of (F,A).
3. Calculate harmonic mean A_{HM} .
4. Evaluate the score value S_i .
5. Finally, find optimum = max (S_i), Then we conclude with the suitable value U_i .

5.4 Example

Assume there are five distributors $U = \{u_1, u_2, u_3, u_4, u_5\}$ whose centre capabilities are assessed by means of component $E = \tilde{X} = \{e_1, e_2, e_3\}$ where e_1 = degree of development innovation, e_2 = the degree of capacity of the administration and e_3 = degree of administration. Suppose a company wants to select the good distributor according to the centre capabilities. A fuzzy neutrosophic soft set is given by

$(F,A) =$

$\{ \{F(e_1) = \{(u_1, 0.6, 0.7, 0.3), (u_2, 0.8, 0.3, 0.2), (u_3, 0.7, 0.5, 0.3), (u_4, 0.7, 0.4, 0.3), u_5, 0.5, 0.6, 0.4)\}$
 $\{ \{F(e_2) = \{(u_1, 0.7, 0.7, 0.3), (u_2, 0.6, 0.7, 0.2), (u_3, 0.6, 0.5, 0.5), (u_4, 0.9, 0.6, 0.3), u_5, 0.7, 0.3, 0.2)\}$
 $\{ \{F(e_3) = \{(u_1, 0.6, 0.7, 0.2), (u_2, 0.5, 0.8, 0.2), (u_3, 0.7, 0.8, 0.3), (u_4, 0.7, 0.5, 0.5), u_5, 0.6, 0.6, 0.2)\}$

The matrix representation for the above is given as

$A = \begin{pmatrix} \langle 0.6, 0.7, 0.3 \rangle & \langle 0.7, 0.7, 0.3 \rangle & \langle 0.6, 0.7, 0.2 \rangle \\ \langle 0.8, 0.3, 0.2 \rangle & \langle 0.6, 0.7, 0.2 \rangle & \langle 0.5, 0.8, 0.2 \rangle \\ \langle 0.7, 0.5, 0.3 \rangle & \langle 0.6, 0.5, 0.5 \rangle & \langle 0.7, 0.8, 0.3 \rangle \\ \langle 0.7, 0.4, 0.3 \rangle & \langle 0.9, 0.6, 0.3 \rangle & \langle 0.7, 0.5, 0.5 \rangle \\ \langle 0.5, 0.6, 0.4 \rangle & \langle 0.7, 0.3, 0.2 \rangle & \langle 0.6, 0.6, 0.2 \rangle \end{pmatrix}$

$$\begin{array}{l}
 \left(\begin{array}{ccc}
 0.265 & 0.3267 & 0.045 \\
 0.252 & 0.1867 & 0.0267 \\
 A_{HM} = 0.21 & 0.222 & 0.081 \\
 & 0.383 & 0.16 & 0.081 \\
 & 0.233 & 0.144 & 0.04
 \end{array} \right) \\
 \\
 \left(\begin{array}{l}
 0.25029 \\
 A_{HM} = 0.24701 \\
 \text{Score} \quad 0.192018 \\
 \mathbf{0.37004} \\
 \quad 0.22724
 \end{array} \right)
 \end{array}$$

Here u_4 is the highest value so it is awesome to choose by the dynamic.

6 Conclusions

In this work, new idea of complement of FNSM dependent on reference work and trace of FNSM set up for certain connected properties and models is introduced. At last a utilization of fuzzy neutrosophic soft matrix in choice strategy problem using harmonic mean is discussed.

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