



## Neutro-Intelligent Set is a particular case of the Refined Neutrosophic Set

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### Abstract

In this short note we show that the newly introduced concept of Neutro-Intelligent Set (NIS) deserves attention in its applications to the human brain activity, and that NIS is a particular case of the Refined Neutrosophic Set.

**Keywords:** Neutrosophic Logic, Physical Neutrosophy, gravitation, physics constants

### 1. Introduction

In order to simplify the notations, we use Latin descriptive letters, instead of Greek letters, to denote by T the truth (or membership), by I the indeterminacy, and by F the falsehood (or nonmembership).

### 2. Definition of Neutrosophic Set

Let U be a universe of discourse, and A be a non-empty neutrosophic subset of U, defined as follows:

$A = \{x, \langle T_A(x), I_A(x), F_A(x) \rangle, x \in U\}$ , where for all  $x \in U$  one has

$T_A(x), I_A(x), F_A(x) \in [0, 1], 0 \leq T_A(x) + I_A(x) + F_A(x) \leq 3$ .

### 3. Definition of the Neutral Degree of the Neutrosophic Set

Sunny Raza Qureshi [1] has introduced the Neutral Degree ( $N_A$ ) of the Neutrosophic Set, defined as follows:

$$N_A : U \rightarrow [0, 1], N_A(x) = 1 - \frac{T_A(x) + I_A(x) + F_A(x)}{3}, x \in U.$$

### 4. Definition of the Neutro-Intelligent Set

It was a nice idea to extend the neutrosophic set from 3 to 4 components, where for all  $x \in U$ , the original components  $T_A(x)$ ,  $I_A(x)$ ,  $F_A(x)$  remain totally independent from each other, while the fourth component  $N_A(x)$  is totally dependent of the first three components.

Then Sunny Raza Qureshi [1] introduced the Neutro-Intelligent Set (NIS) by adding the neutral Degree to each element, defined as follows:

Let  $U$  be a universe of discourse, and  $A_{NIS}$  be a non-empty subset of  $U$ , defined as follows:

$$A_{NIS} = \{x, \langle T_A(x), I_A(x), N_A(x), F_A(x) \rangle, x \in U\}, \text{ where for all } x \in U$$

$$T_A(x), I_A(x), N_A(x), F_A(x) \in [0, 1], 0 \leq T_A(x) + I_A(x) + F_A(x) \leq 3,$$

$$N_A(x) = 1 - \frac{T_A(x) + I_A(x) + F_A(x)}{3}.$$

### 5. Example of Neutro-Intelligent Set

$A_{RNS} = \{a_1(0.4, 0.2, 0.7, 0.3), a_2(0.7, 0.2, 0.6, 0.3)\}$ , because:

$$T_1 = 0.4, I_1 = 0.2, F_1 = 0.3, \text{ whence the neutral } N_1 = 1 - \frac{T_1 + I_1 + F_1}{3} = 1 - \frac{0.4 + 0.2 + 0.3}{3} = 0.7.$$

$$T_2 = 0.7, I_2 = 0.2, F_2 = 0.3, \text{ whence the neutral } N_2 = 1 - \frac{T_2 + I_2 + F_2}{3} = 1 - \frac{0.7 + 0.2 + 0.3}{3} = 0.6.$$

### 6. Definition of the Refined Neutrosophic Set

In 2013 the neutrosophic theories were extended to the *refined [n-valued] neutrosophic set*, *refined neutrosophic logic*, and *refined neutrosophic probability respectively* [2], i.e. the truth value  $T$  was refined/split into types of sub-truths such as  $T_1, T_2, \dots, T_p$ , similarly indeterminacy  $I$  was refined/split into types of sub-indeterminacies  $I_1, I_2, \dots, I_r$ , and the falsehood  $F$  was refined/split into sub-falsehood  $F_1, F_2, \dots, F_s$ .

Let  $U$  be a universe of discourse, and  $A_{RNS}$  be a non-empty subset of  $U$ , then the Refined Neutrosophic Set is defined as follows:

$$A_{RNS} = \{x, \langle T_{1A}(x), T_{2A}(x), \dots, T_{pA}(x); I_{1A}(x), I_{2A}(x), \dots, I_{rA}(x); F_{1A}(x), F_{2A}(x), \dots, F_{sA}(x) \rangle, x \in U\},$$

where  $p, r, s$  are positive integers, and at least one of them is  $\geq 2$ ,

also for all  $x \in U$ ,

$$T_{1A}(x), T_{2A}(x), \dots, T_{pA}(x); I_{1A}(x), I_{2A}(x), \dots, I_{rA}(x); F_{1A}(x), F_{2A}(x), \dots, F_{sA}(x) \in [0, 1].$$

If one takes the particular case:  $p = 1, r = 2, s = 1$ , one gets  $T, I_1, I_2, F$ , with  $I_1$  = indeterminacy and  $I_2$  = neutrality, one gets the Neutro-Intelligent Set (NIS). The original part of the NIS is that  $I_2$  (neutrality) is taken as dependent from  $T, I$ , and  $F$ .

### 7. Applications

The author [1] has introduced a neutrosophic model of the human brain, the Multi-Phase/State Neutrosophic Set and aggregated it to its Neutro-Intelligent Set forming a Final Phase Neutrosophic Set, to analyze the human mind uncertainty, especially the sentimental and emotional activities.

**Funding:** "This research received no external funding"

**Conflicts of Interest:** "The authors declare no conflict of interest."

## **References**

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